

Concurrent programming: From theory to practice

Concurrent Algorithms 2018

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From theory to practice

Theoretical
(design)

Practical
(design)

Practical
(implementation)

From theory to practice

Theoretical
(design)

Practical
(design)

Practical
(implementation)

- Impossibilities
- Upper/Lower bounds
- Techniques
- System models
- Correctness proofs



**Design
(pseudo-code)**

From theory to practice

Theoretical (design)

- Impossibilities
- Upper/Lower bounds
- Techniques
- System models
- Correctness proofs



**Design
(pseudo-code)**

Practical (design)

- System models
 - shared memory
 - message passing
- **Finite memory**
- Practicality issues
 - re-usable objects
- **Performance**



**Design
(pseudo-code,
prototype)**

Practical (implementation)

From theory to practice

Theoretical (design)

- Impossibilities
- Upper/Lower bounds
- Techniques
- System models
- Correctness proofs



**Design
(pseudo-code)**

Practical (design)

- System models
 - shared memory
 - message passing
- **Finite memory**
- Practicality issues
 - re-usable objects
- **Performance**



**Design
(pseudo-code,
prototype)**

Practical (implementation)

- **Hardware**
- Which atomic ops
- Memory consistency
- Cache coherence
- Locality
- **Performance**
- **Scalability**



**Implementation
(code)**

Outline

- CPU caches
- Cache coherence
- Placement of data
- Graph processing: Concurrent data structures

Outline

- **CPU caches**
- Cache coherence
- Placement of data
- Graph processing: Concurrent data structures

Why do we use caching?

Core



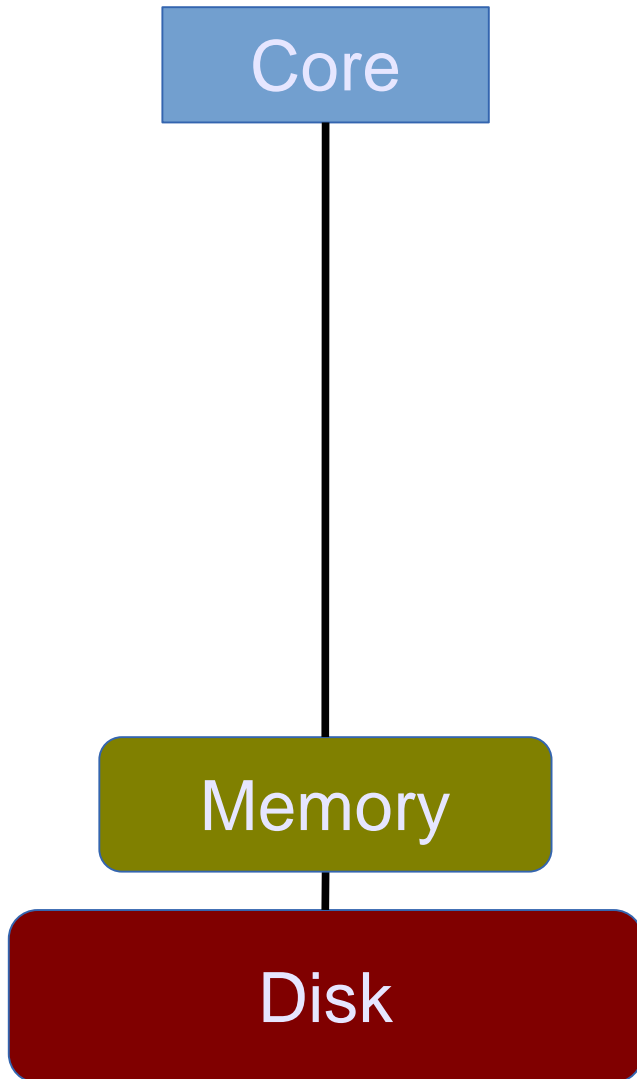
```
graph TD; Core[Core] --- Disk[Disk];
```

- Core freq: 2GHz = 0.5 ns / instr
- Core → Disk = ~ms

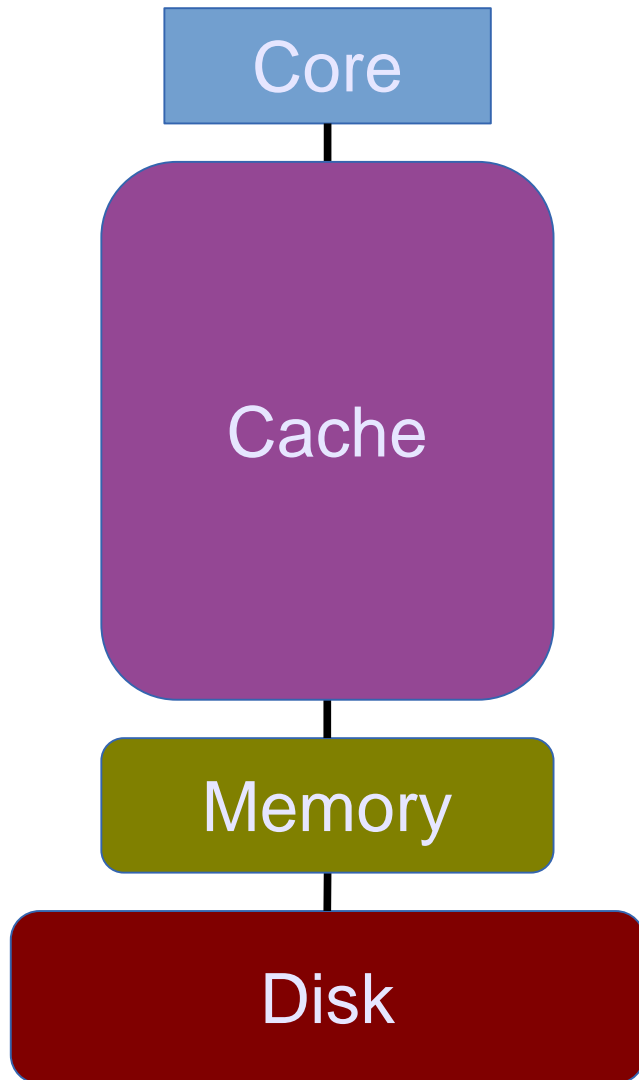
Disk

Why do we use caching?

- Core freq: 2GHz = 0.5 ns / instr
- Core → Disk = ~ms
- Core → Memory = ~100ns

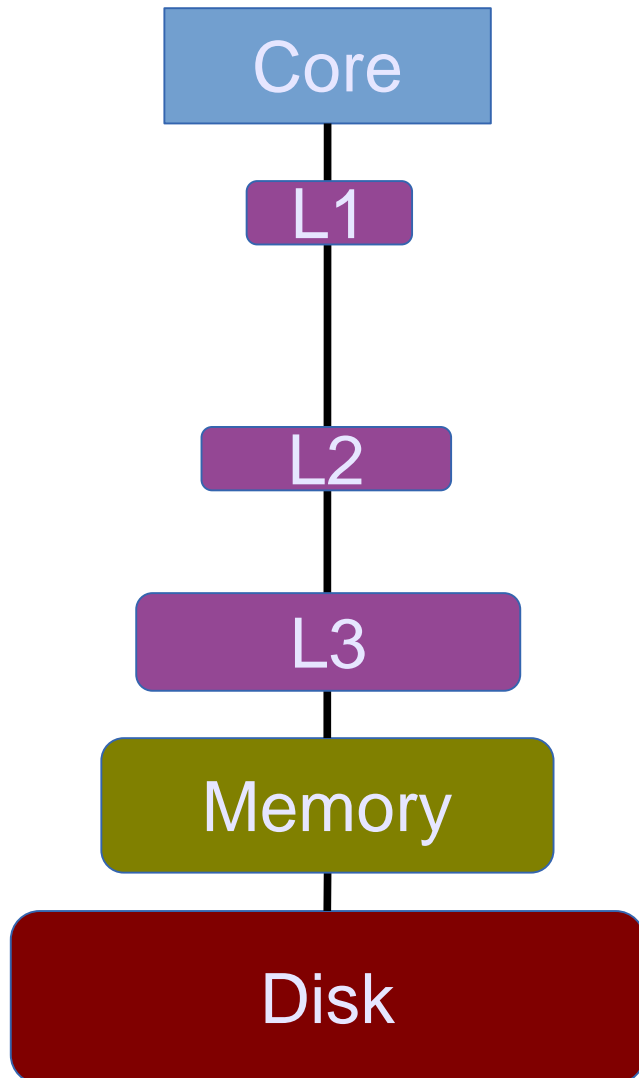


Why do we use caching?



- Core freq: 2GHz = 0.5 ns / instr
- Core → Disk = ~ms
- Core → Memory = ~100ns
- **Cache**
 - Large = slow
 - Medium = medium
 - Small = fast

Why do we use caching?



- Core freq: 2GHz = 0.5 ns / instr
- Core → Disk = ~ms
- Core → Memory = ~100ns
- Cache
 - Core → L3 = ~20ns
 - Core → L2 = ~7ns
 - Core → L1 = ~1ns

Typical server configurations

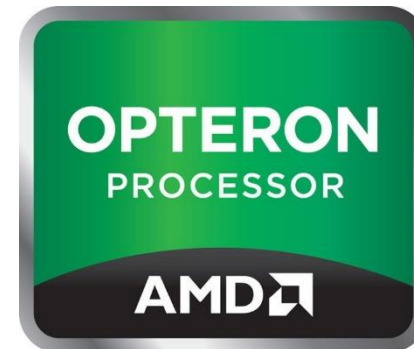
- **Intel Xeon**

- 12 cores @ 2.4GHz
- L1: 32KB
- L2: 256KB
- L3: 40MB
- Memory: 128GB



- **AMD Opteron**

- 12 cores @ 2.4GHz
- L1: 64KB
- L2: 512KB
- L3: 20MB
- Memory: 128GB



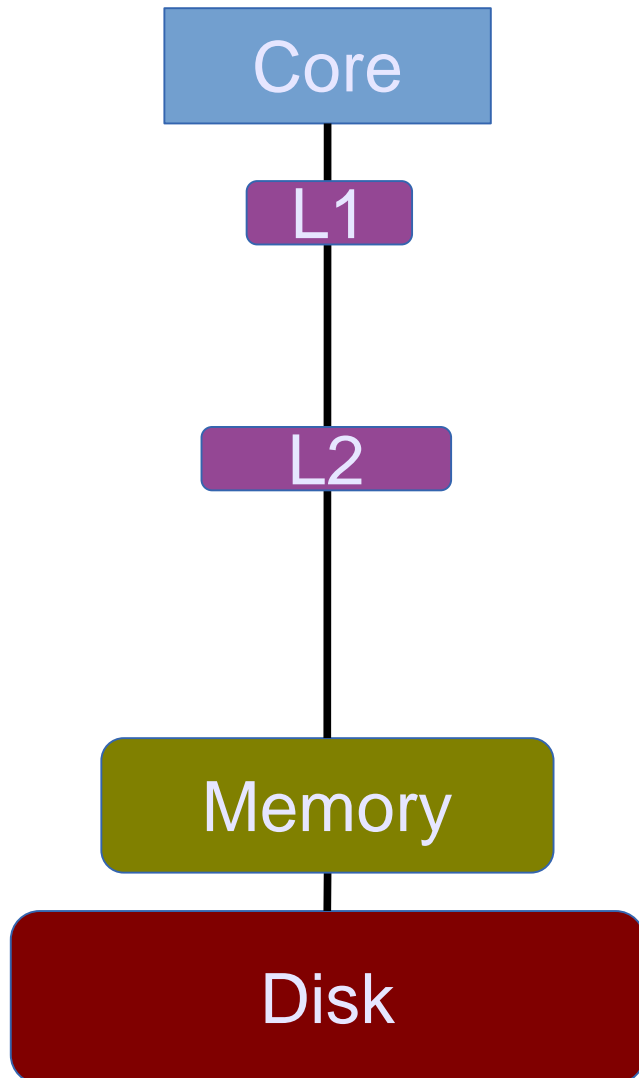
Experiment

Throughput of accessing some memory,
depending on the memory size

Outline

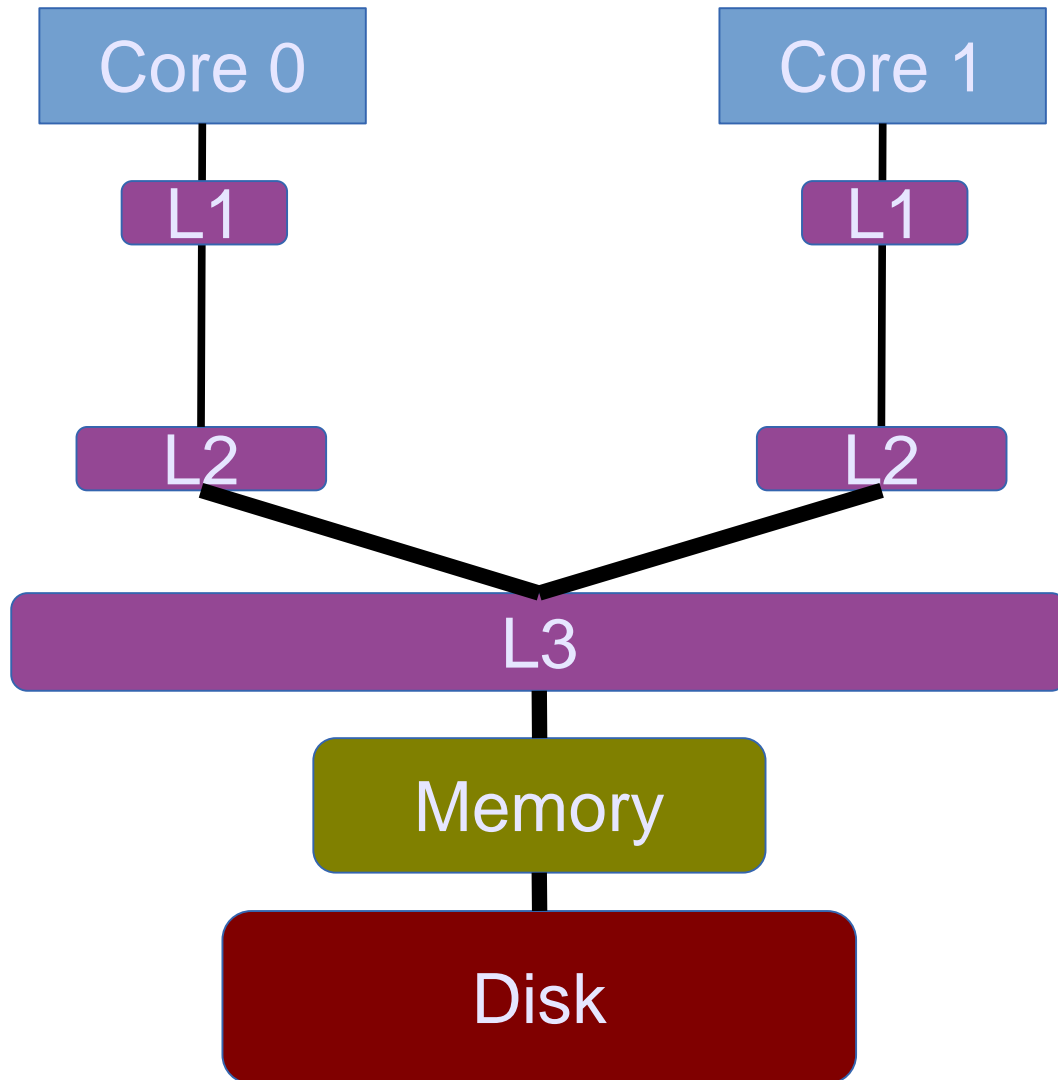
- CPU caches
- **Cache coherence**
- Placement of data
- Graph processing: Concurrent data structures

Until ~2004: single-cores



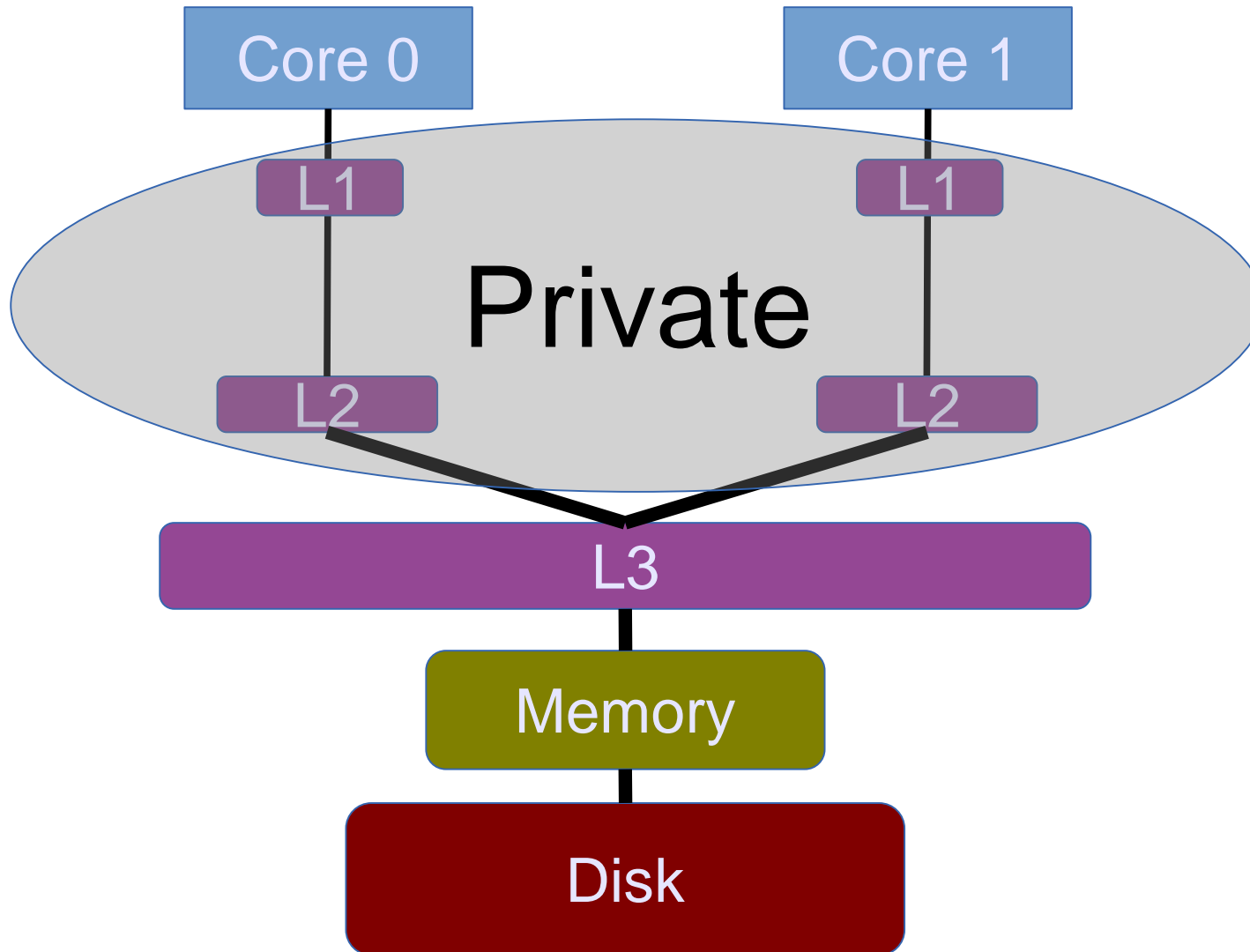
- Core freq: 3+GHz
- Core → Disk
- Core → Memory
- Cache
 - Core → L3
 - Core → L2
 - Core → L1

After ~2004: multi-cores



- Core freq: ~2GHz
- Core → Disk
- Core → Memory
- Cache
 - Core → **shared L3**
 - Core → L2
 - Core → L1

Multi-cores with private caches

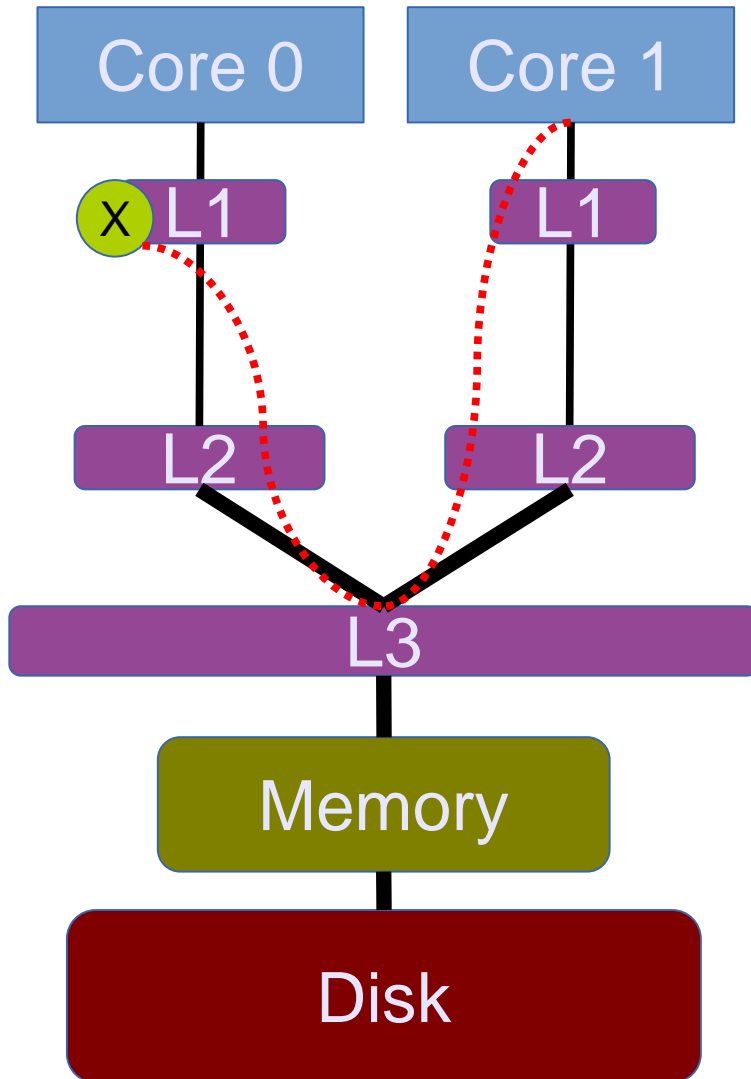


=
multiple
copies

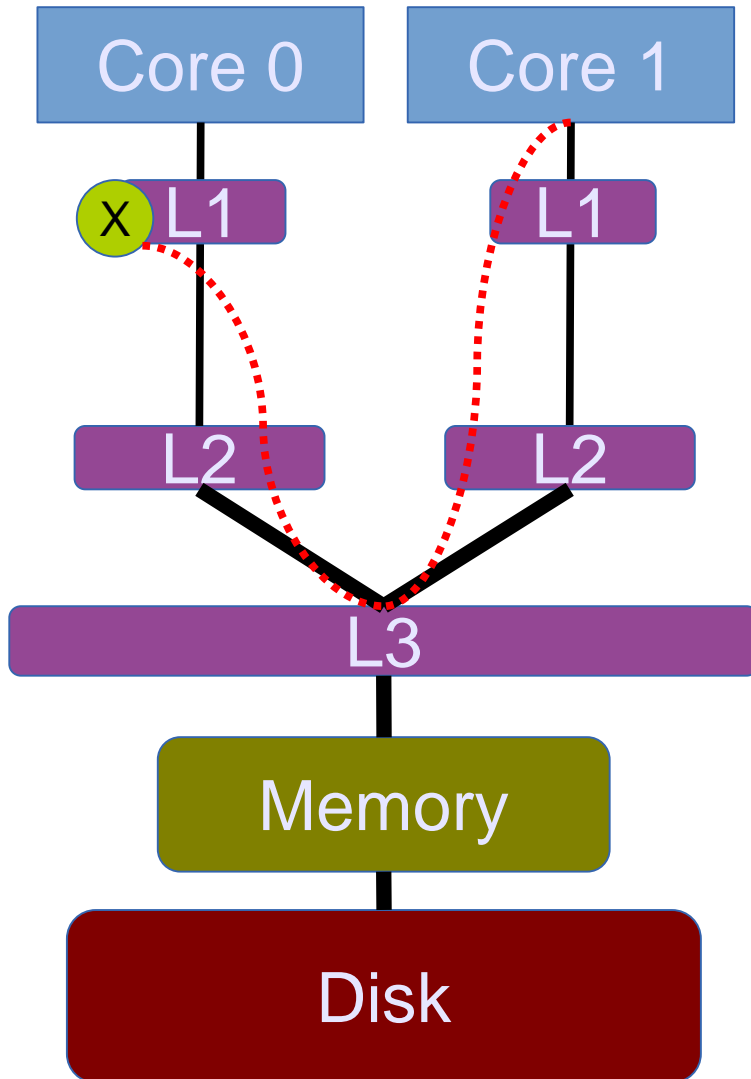
Cache coherence for consistency

Core 0 has **X** and Core 1

- wants to write on **X**
- wants to read **X**
- did Core 0 write or read **X**?



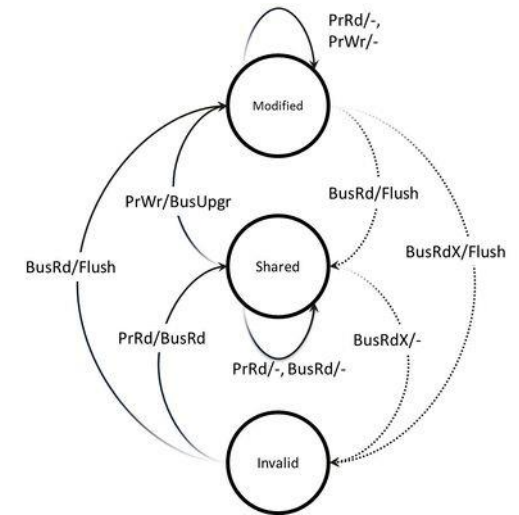
Cache coherence principles



- To perform a **write**
 - invalidate all readers, or
 - previous writer
- To perform a **read**
 - find the latest copy

Cache coherence with MESI

- A state diagram
- State (per cache line)
 - **Modified**: the only dirty copy
 - **Exclusive**: the only clean copy
 - **Shared**: a clean copy
 - **Invalid**: useless data



The ultimate goal for scalability

- Possible states
 - **Modified**: the only dirty copy
 - **Exclusive**: the only clean copy
 - **Shared**: a clean copy
 - **Invalid**: useless data
- **Which state is our “favorite”?**

The ultimate goal for scalability

- Possible states

- **Modified**: the only dirty copy
- **Exclusive**: the only clean copy

- **Shared**: a clean copy

- **Invalid**: useless data

= threads can keep the data close (L1 cache)

= faster

Experiment

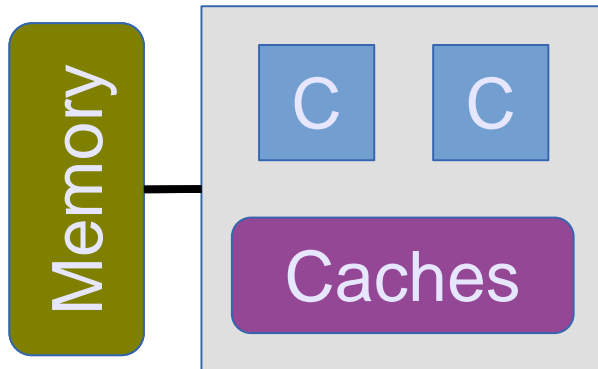
The effects of false sharing

Outline

- CPU caches
- Cache coherence
- **Placement of data**
- Graph processing: Concurrent data structures

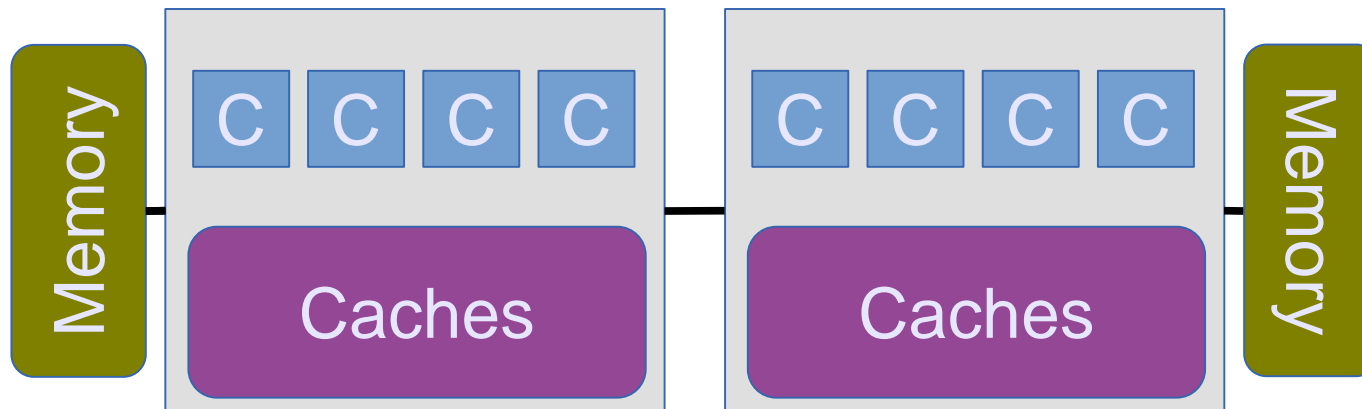
Uniformity vs. non-uniformity

- Typical **desktop** machine



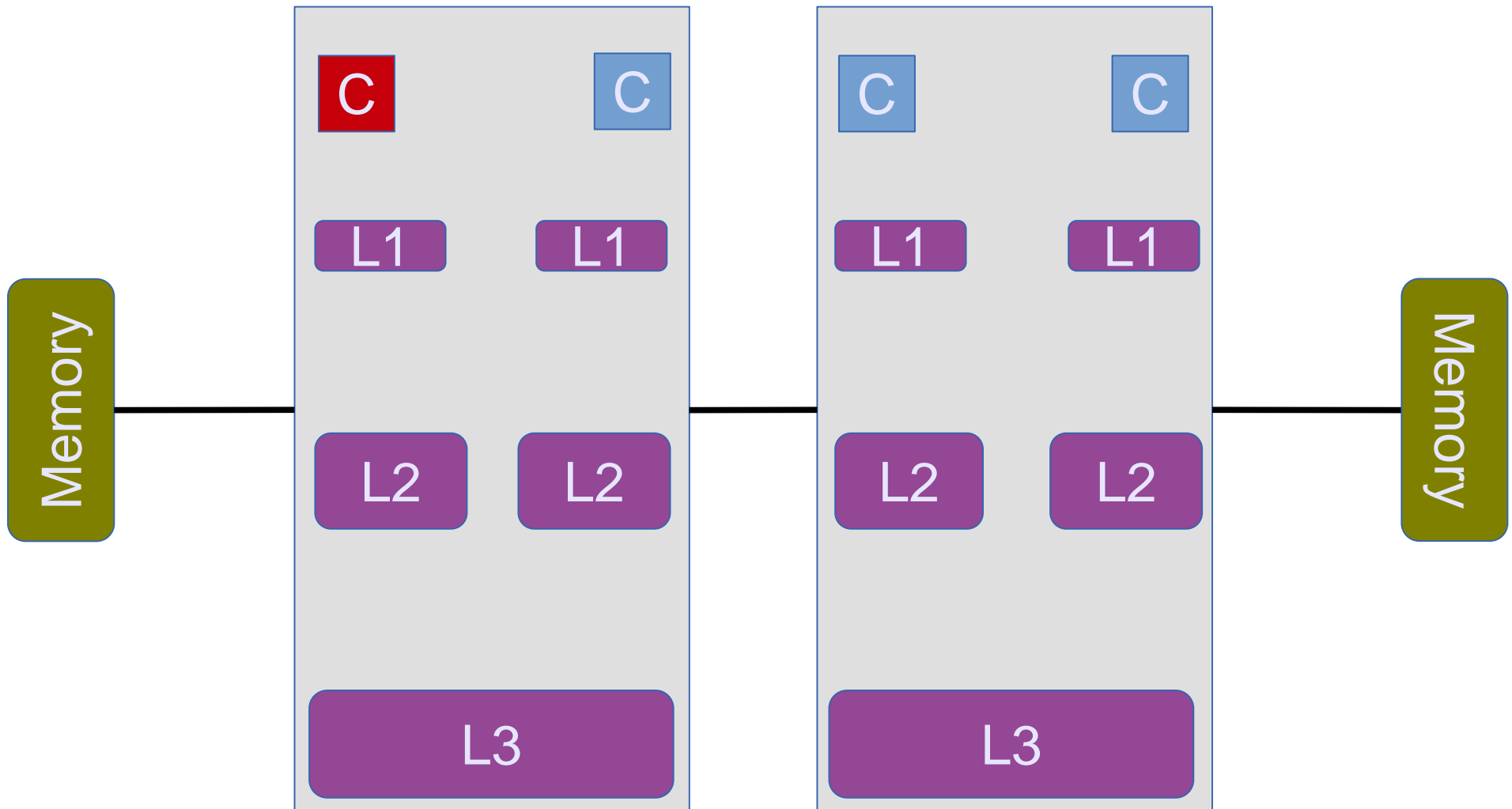
= Uniform

- Typical **server** machine

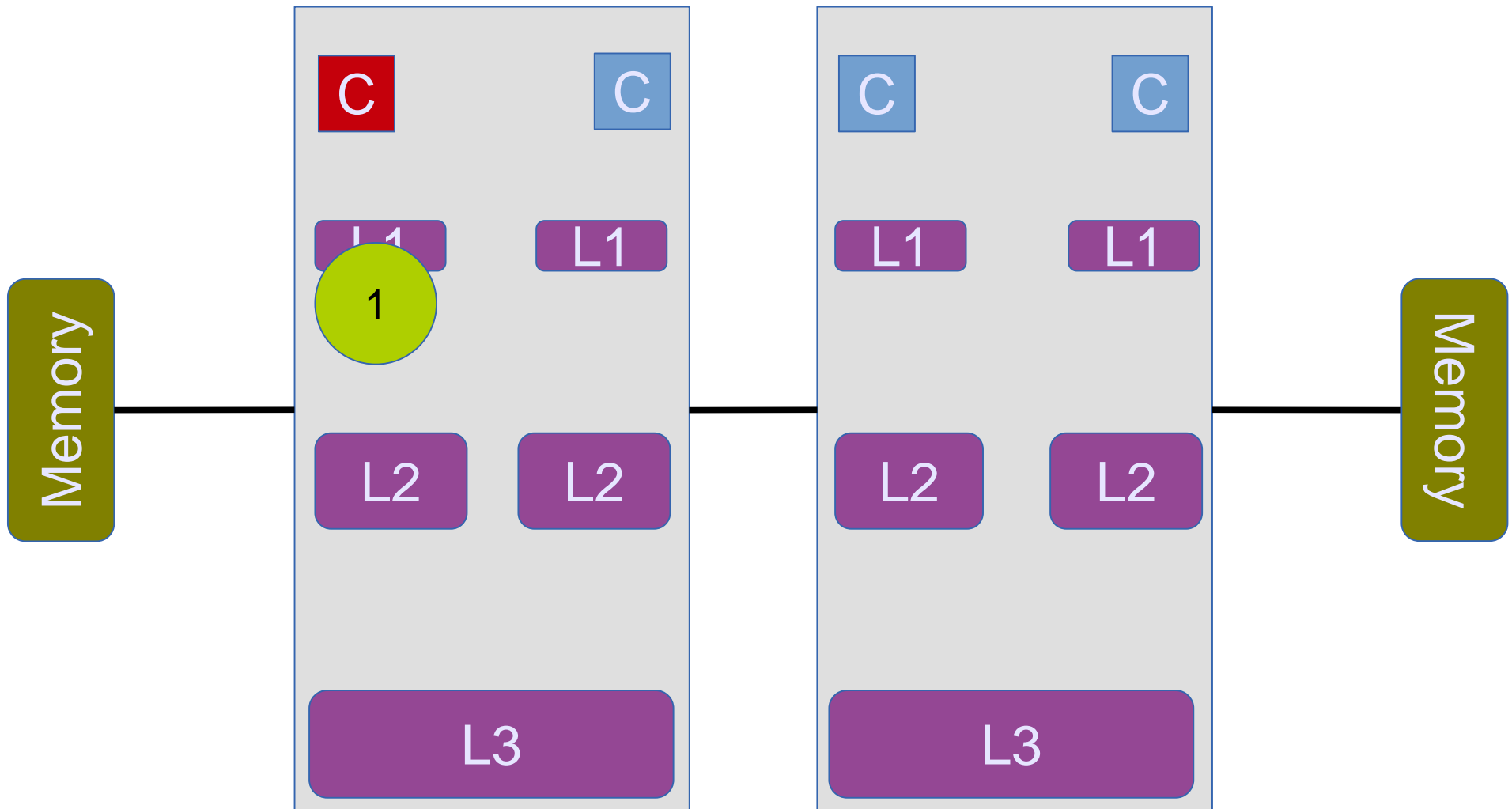


= non-Uniform

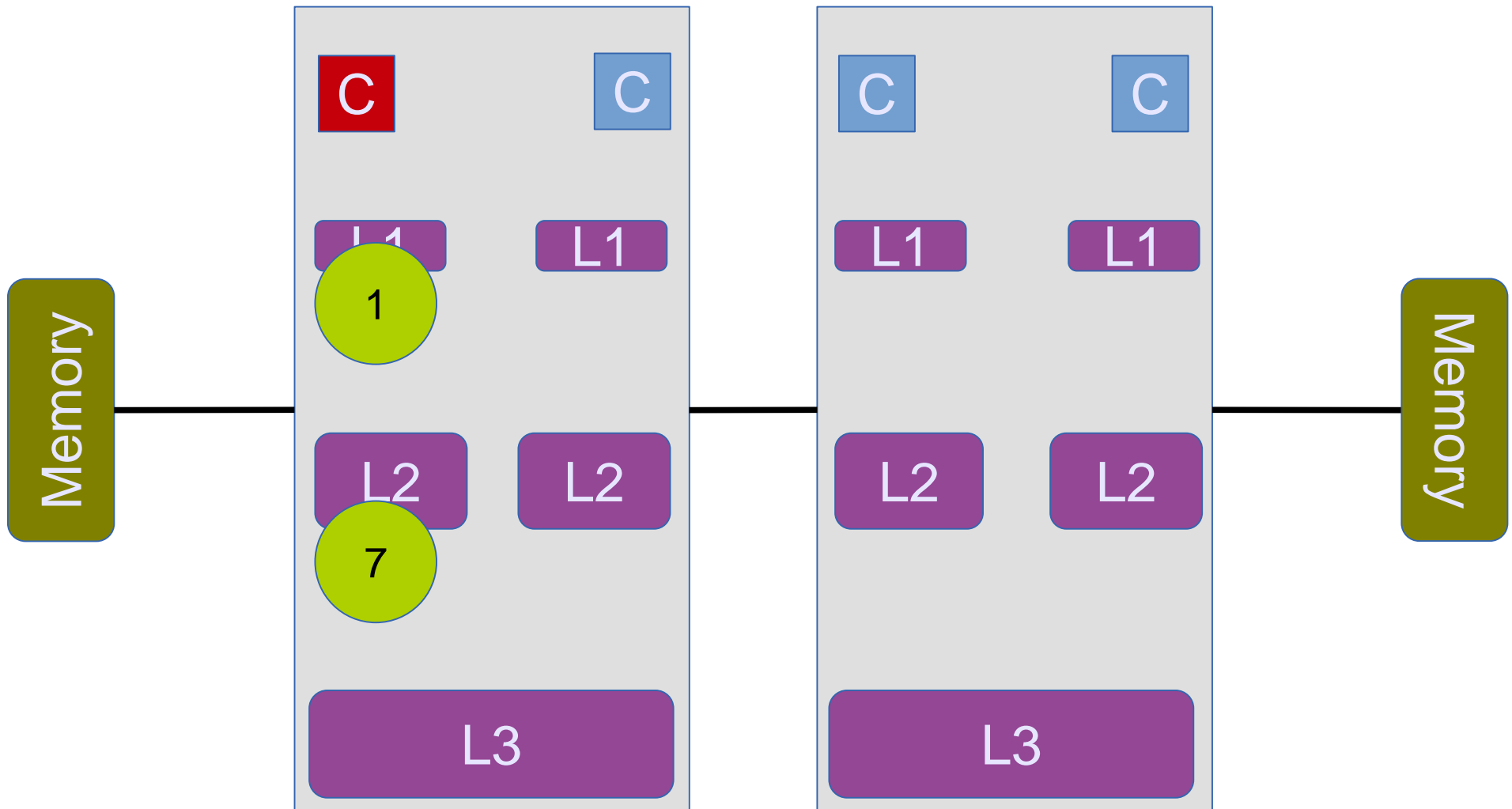
Latency (ns) to access data



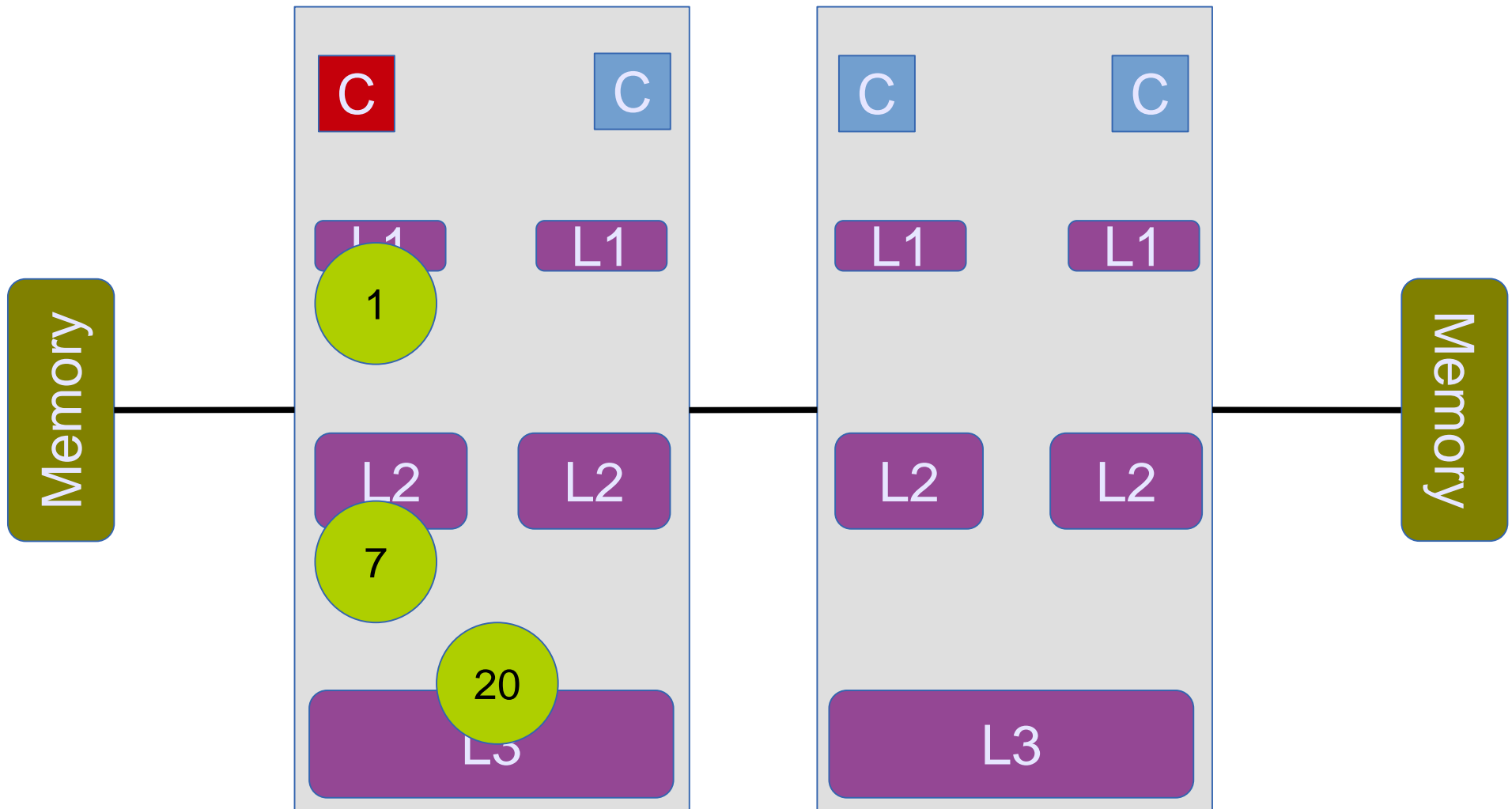
Latency (ns) to access data



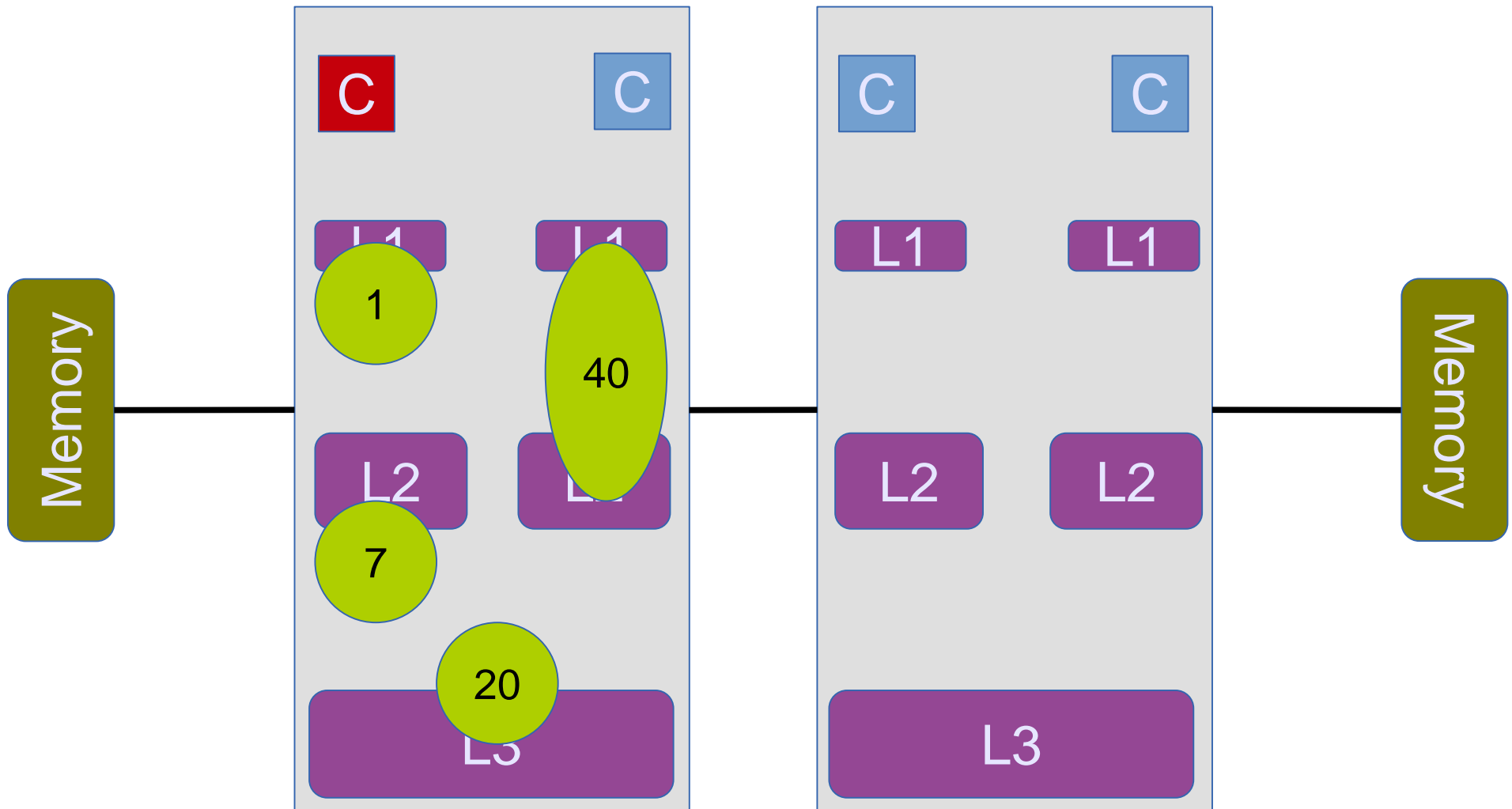
Latency (ns) to access data



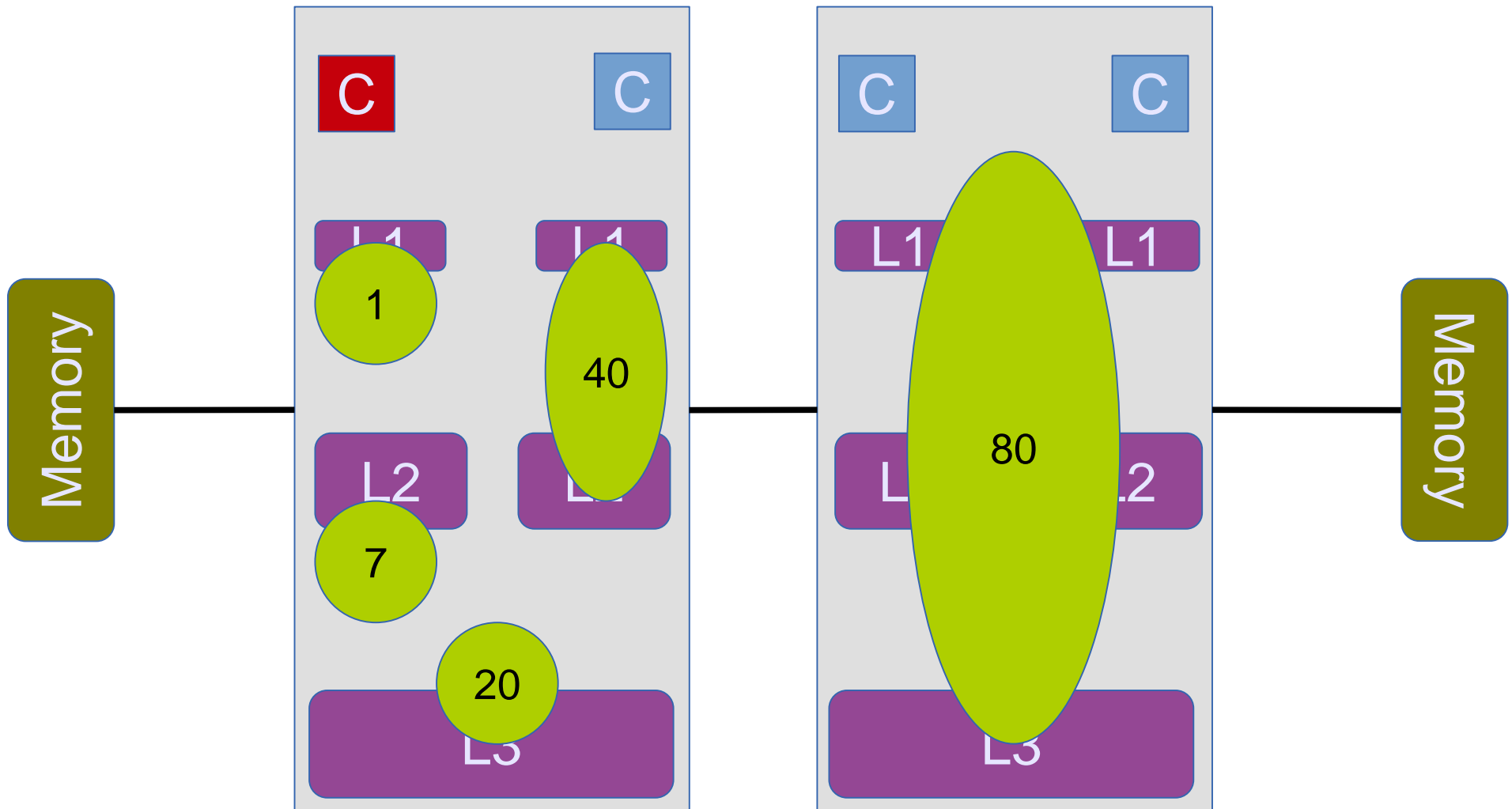
Latency (ns) to access data



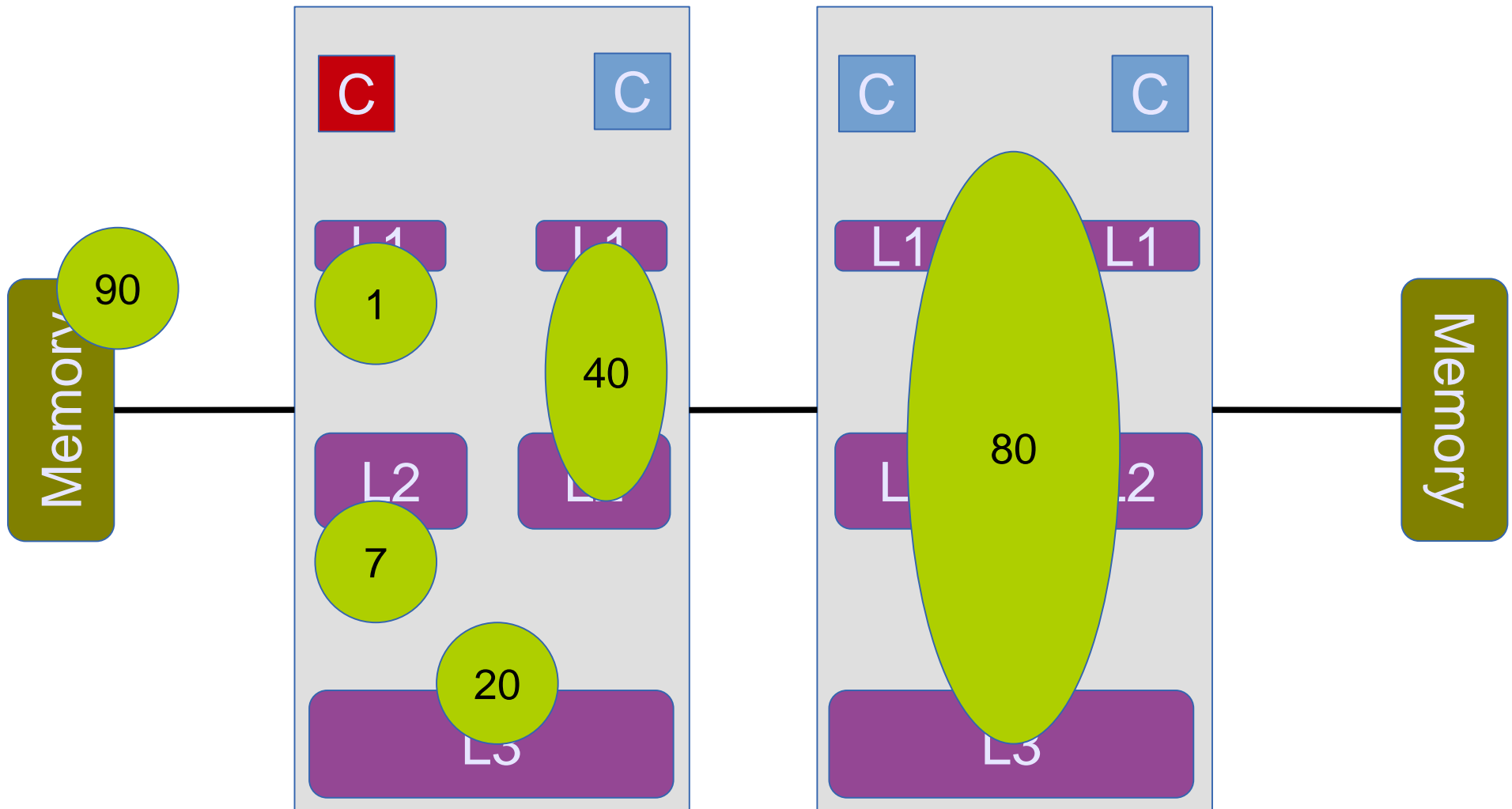
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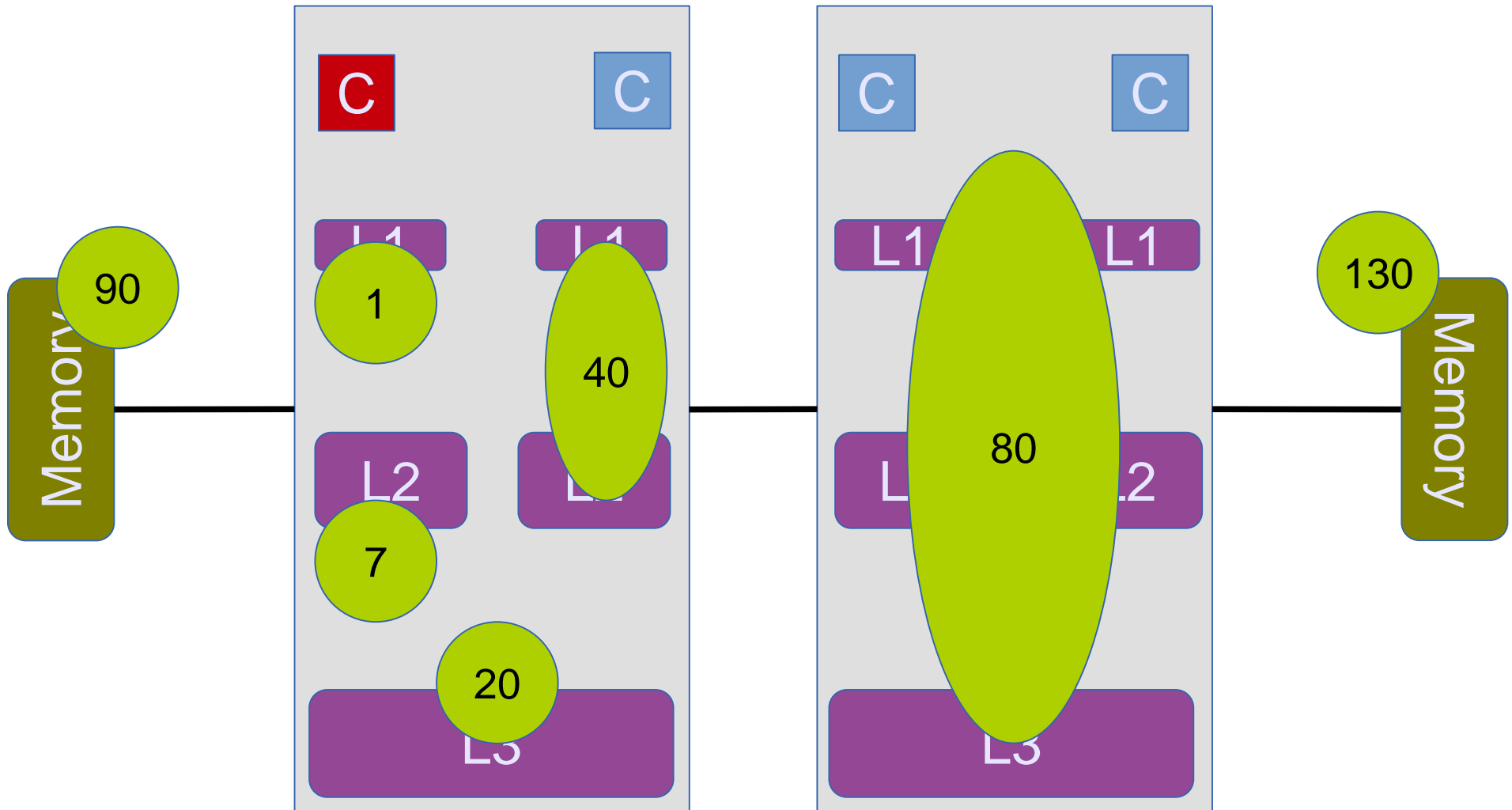
Latency (ns) to access data



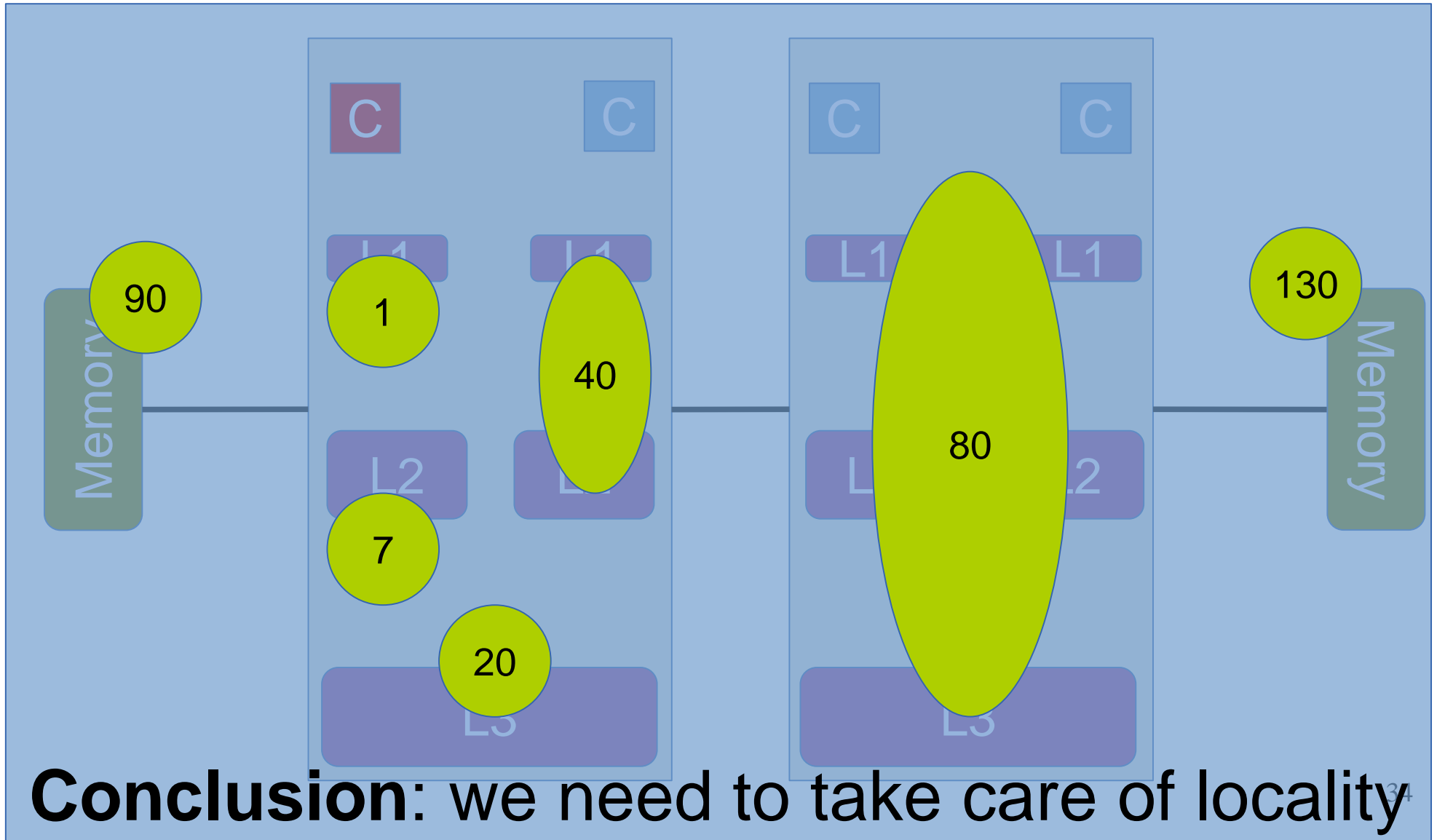
Latency (ns) to access data



Latency (ns) to access data



Latency (ns) to access data



Experiment

The effects of locality

Experiment

The effects of locality

```
vtrigona $ ./test_locality -x0 -y1  
Size:      8 counters = 1 cache lines  
Thread 0 on core : 0  
Thread 1 on core : 2  
Number of threads: 2  
Throughput : 104.27 Mop/s
```

```
vtrigona $ ./test_locality -x0 -y10  
Size:      8 counters = 1 cache lines  
Thread 0 on core : 0  
Thread 1 on core : 10  
Number of threads: 2  
Throughput : 43.16 Mop/s
```

Same memory node

Different memory nodes

Outline

- CPU caches
- Cache coherence
- Placement of data
- **Graph processing: Concurrent data structures**

Graph processing

Relational view

People
Table

Name	Likes
Vasilis	Breaking bad
Rachid	Dexter
Vasilis	Dexter

Series
Table

Name	Similar
Breaking bad	Dexter
Dexter	Breaking bad

Graph processing

Relational view

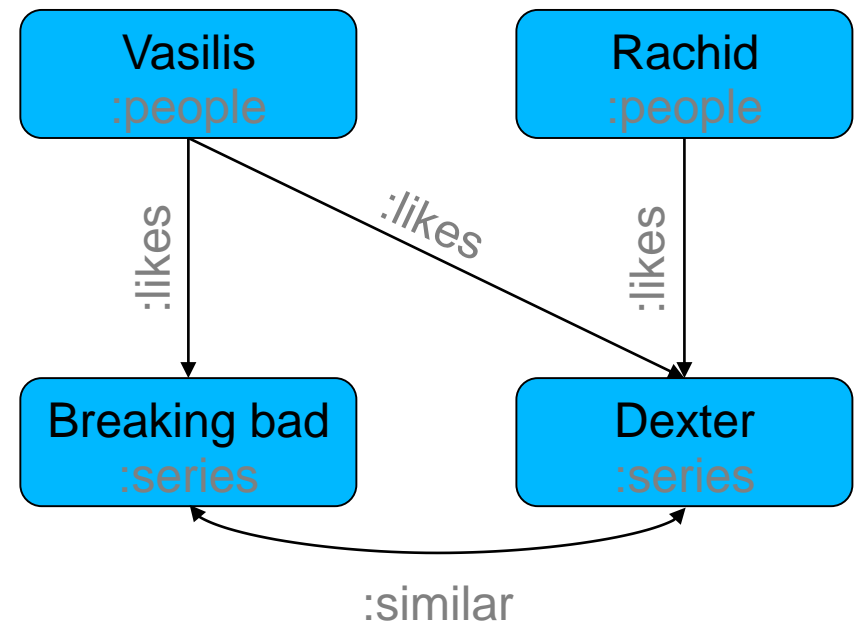
People
Table

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Series
Table

Name	Similar
Breaking bad	Dexter
Dexter	Breaking bad

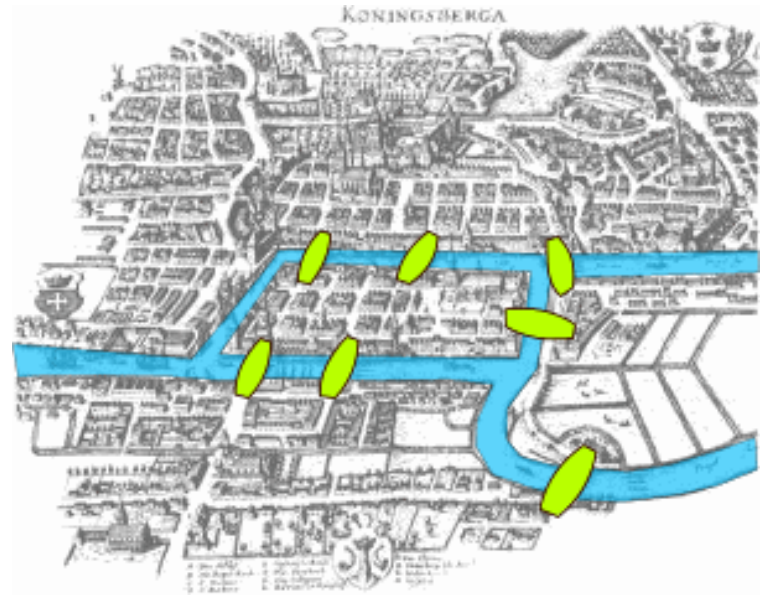
Graph view



Graphs keep the connections among entities materialized

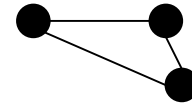
Graph analytics

- Graphs have been studied in Math for centuries
 - Since Euler's "Seven Bridges of Königsberg", 1736
- **Repeatedly traverse your graph and calculate math properties**
- Classic graph problems
 - Graph isomorphism
 - Travelling salesman's problem
 - Max flow, min cut
 - ...
- More recent developments
 - Pagerank
 - Infomap



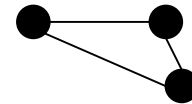
Graph queries

- **Graph pattern matching**
 - Query graphs to find sub-graphs that match a pattern
e.g., triangle counting
- Essentially: SQL for graphs



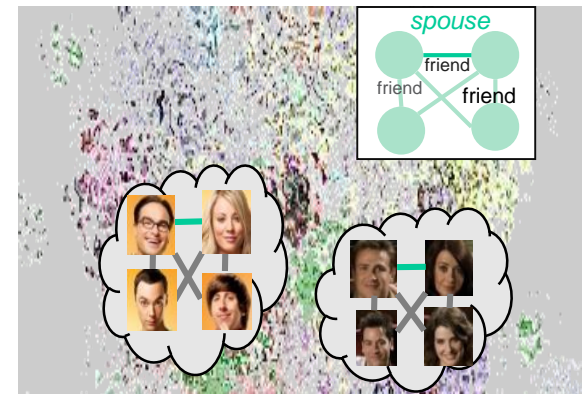
Graph queries

- **Graph pattern matching**
 - Query graphs to find sub-graphs that match a pattern
e.g., triangle counting



- Essentially: SQL for graphs
- Example: Friends of my friends

```
SELECT p1, p3, COUNT(p2)
MATCH (p1)-[:friend]->(p2)->[:friend]->(p3),
      ! (p1)-[:friend]->(p3)
WHERE p1.country = p2.country
GROUP BY p1, p3
ORDER BY COUNT(p2) DESC
```



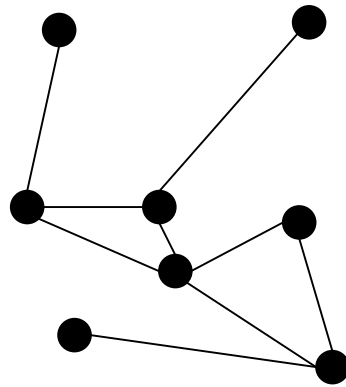
Graph processing frequently involves both analytics and queries

Dissecting a graph processing system

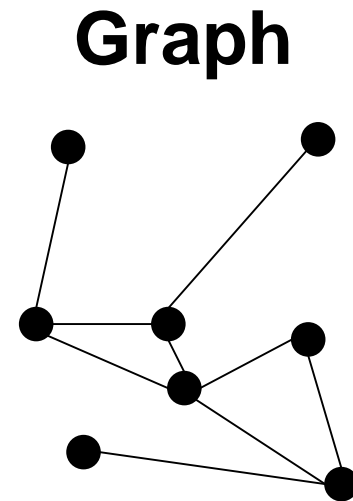
with a focus on (concurrent) data structures

Architecture of a graph processing system

Graph



Architecture of a graph processing system



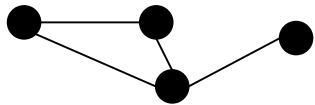
Tons of other data and metadata to store

Graph

tmp graph structure

↓
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Vasilis”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

Vasilis → 0	0 → Vasilis
Rachid → 1	1 → Rachid
Breaking bad → 2	2 → Breaking bad
Dexter → 3	3 → Dexter

labels

:likes, :people, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

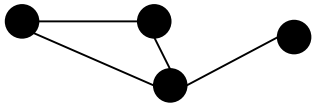
number_of_references: X

Graph

tmp graph structure

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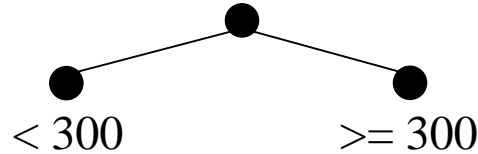
"Vasilis", {people, male}, 33, Zurich
 "Rachid", {people, male}, ??, Lausanne

lifetime management

number_of_references: X

Runtime

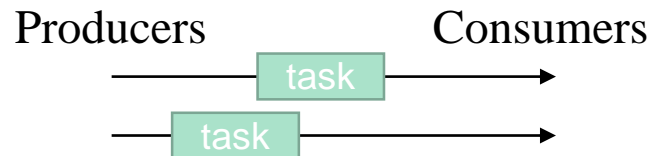
indices / metadata



buffer management

1MB 1MB 1MB 1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...

↓ ↓ ↓ ↓

1 2 3 4

{people, male} → {2,4}

renaming (ids)

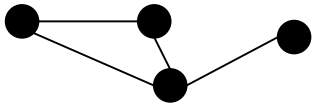
used used used

Graph

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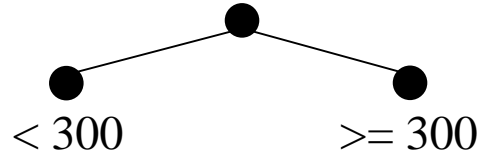
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lifetime management

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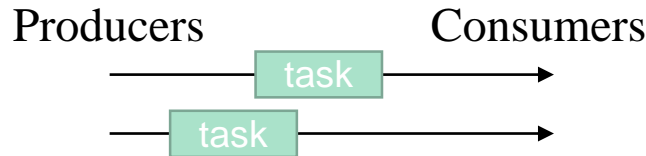
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buffer management



task / job scheduling



labels

:likes, :people, :similar, :male ...

↓ ↓ ↓ ↓
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{people, male} → {2,4}

renaming (ids)



Operations

group by / join

Vasilis, Breaking bad	→	Vasilis, 2
Rachid, Dexter		Rachid, 1
Vasilis, Dexter		

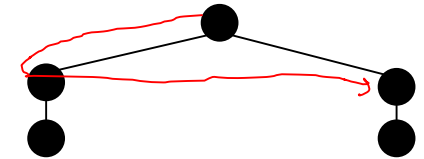
distinct

Vasilis	→	Vasilis
Rachid		Rachid
Vasilis		

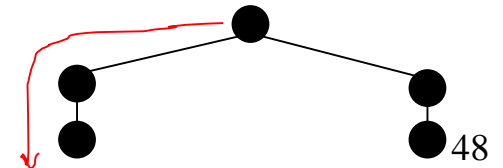
limit (top k)

11 12 0 9 8 13	→	32
8 9 11 23 32 9		23
1 2 3 5 7 3 2 0		13

BFS



DFS

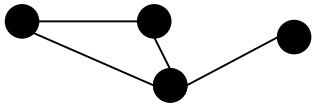


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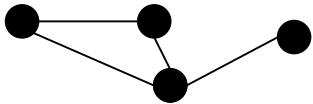
- tmp graph structure
 - append only
 - dynamic schema

Graph

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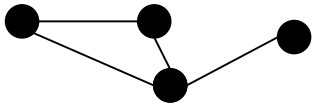
- tmp graph structure
 - append only
 - dynamic schema→ **segmented table**

Graph

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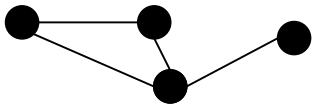
- tmp graph structure
 - append only
 - dynamic schema
 - **segmented table**
- Classic graph structures

Graph

tmp graph structure

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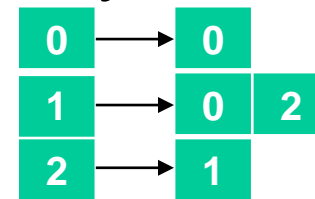
- tmp graph structure
 - append only
 - dynamic schema→ **segmented table**

- Classic graph structures

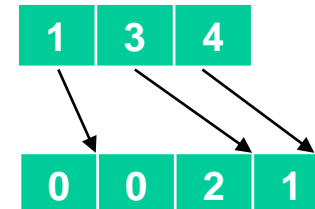
1. connectivity matrix

	0	1	2
0	x		
1	x		x
2		x	

2. adjacency list



3. compressed source row (CSR)



Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
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graph structure



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labels

:likes, :people, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
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lifetime management

number_of_references: X

- Mapping user ids to internal ids
 - create once
 - read-only after

Graph

tmp graph structure

“Vasilis”, “Breaking bad”, :likes

“Rachid”, “Dexter”, :likes

“Vasilis”, “Breaking bad”, :similar

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segmented buffer

graph structure



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Dexter → 3	3 → Dexter

labels

:likes, :people, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich

“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

- Mapping user ids to internal ids
 - create once
 - read-only after
- **hash map, lock-free reads**

Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

Vasilis → 0	0 → Vasilis
Rachid → 1	1 → Rachid
Breaking bad → 2	2 → Breaking bad
Dexter → 3	3 → Dexter

labels

:likes, :people, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

- Mapping user ids to internal ids
 - create once
 - read-only after
 - **hash map, lock-free reads**
- Mapping internal ids to user ids
 - create once
 - read-only after
 - fixed key range: [0, N}

Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

Vasilis → 0	0 → Vasilis
Rachid → 1	1 → Rachid
Breaking bad → 2	2 → Breaking bad
Dexter → 3	3 → Dexter

labels

:likes, :people, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

- Mapping user ids to internal ids
 - create once
 - read-only after
 - **hash map, lock-free reads**
- Mapping internal ids to user ids
 - create once
 - read-only after
 - fixed key range: [0, N]
 - **(sequential) array**

Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

hash map/array
Vasilis → 0 0 → Vasilis
Rachid → 1 1 → Rachid
Breaking bad → 2 2 → Breaking bad
Dexter → 3 3 → Dexter

labels

:likes, :people, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

- Storing labels
 - usually a small enumeration e.g., person, female, male
 - storing strings is expensive
“person” → ~ 7 bytes
 - comparing strings is expensive

Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

hash map/array
Vasilis → 0 0 → Vasilis
Rachid → 1 1 → Rachid
Breaking bad → 2 2 → Breaking bad
Dexter → 3 3 → Dexter

labels

:likes, :people, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

- Storing labels
 - usually a small enumeration e.g., person, female, male
 - storing strings is expensive
“person” → ~ 7 bytes
 - comparing strings is expensive
→ **dictionary encoding**, e.g.,
 - person → 0
 - female → 1
 - male → 2
- Ofc, **hash map** to
 - store those
 - translate during runtime

Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

Vasilis → 0 0 → Vasilis
Rachid → 1 1 → Rachid
Breaking bad → 2 2 → Breaking bad
Dexter → 3 3 → Dexter

labels

:likes, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

• Property

- one type per property, e.g., int
- 1:1 mapping with vertices/edges

Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

Vasilis → 0 0 → Vasilis
Rachid → 1 1 → Rachid
Breaking bad → 2 2 → Breaking bad
Dexter → 3 3 → Dexter

labels

:likes, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

• Property

- one type per property, e.g., int
 - 1:1 mapping with vertices/edges
- **(sequential) arrays**

Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

Vasilis → 0 0 → Vasilis
Rachid → 1 1 → Rachid
Breaking bad → 2 2 → Breaking bad
Dexter → 3 3 → Dexter

labels

:like, :love, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

- Property
 - one type per property, e.g., int
 - 1:1 mapping with vertices/edges
 - **(sequential) arrays**
- Lifetime management (and other counters)
 - cache coherence: atomic counters can be expensive

Graph

tmp graph structure

↓
segmented buffer
“Vasilis”, “Breaking bad”, :likes
“Rachid”, “Dexter”, :likes
“Dexter”, “Breaking bad”, :similar
“Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

hash map/array
Vasilis → 0 0 → Vasilis
Rachid → 1 1 → Rachid
Breaking bad → 2 2 → Breaking bad
Dexter → 3 3 → Dexter

labels

dictionary
:likes {people, male}, ...

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

lifetime management

number_of_references: X

- Property
 - one type per property, e.g., int
 - 1:1 mapping with vertices/edges→ **(sequential) arrays**

- Lifetime management (and other counters)

- cache coherence: atomic counters can be expensive

- Two potential solutions

1. **approximate counters**
2. **stripped counters**

Thread local: counter[0] counter[1] counter[2]

```
increment(int by) { counter[my_thread_id] += by; }
```

```
int value() {
```

```
    int sum = 0;
```

```
    for (int i = 0; i < num_threads; i++) { sum += counter[i]; }
```

```
    return sum;
```

```
}
```

Graph

tmp graph structure

“Vasilis”, “Breaking bad”, :likes

“Rachid”, “Dexter”, :likes

“Dexter”, “Breaking bad”, :similar

“Breaking bad”, “Dexter”, :similar

segmented buffer

graph structure



user-ids - internal ids

Vasilis → 0 0 → Vasilis
Rachid → 1 1 → Rachid
Breaking bad → 2 2 → Breaking bad
Dexter → 3 3 → Dexter

hash map / array

labels

dictionary (= map)

properties

“Vasilis”, {people, male}, 33, Zurich
“Rachid”, {people, male}, ??, Lausanne

array

lifetime management

number_of_references: X

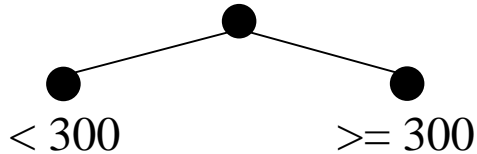
stripped counter

Score

Structure	# Usages
array / buffer	5
map	2

Runtime

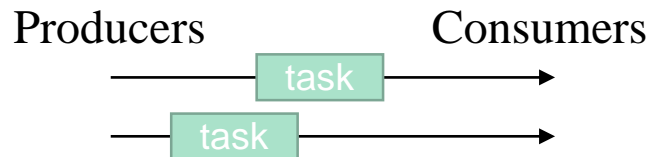
indices / metadata



buffer management

1MB 1MB 1MB 1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...

↓ ↓ ↓ ↓
1 2 3 4

{people, male} → {2,4}

renaming (ids)

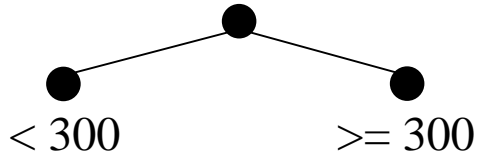
used used used

• Indices

- Used for speeding up “queries”
 - Which vertices have label :person?
 - Which edges have value > 1000?

Runtime

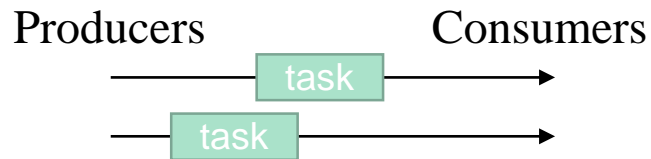
indices / metadata



buffer management

1MB 1MB 1MB 1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...

↓ ↓ ↓ ↓
1 2 3 4

{people, male} → {2,4}

renaming (ids)

used used used

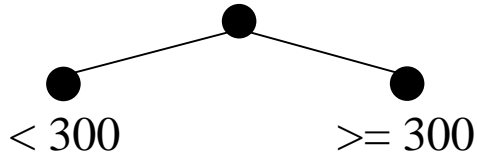
• Indices

- Used for speeding up “queries”
 - Which vertices have label :person?
 - Which edges have value > 1000?

→ **maps, trees**

Runtime

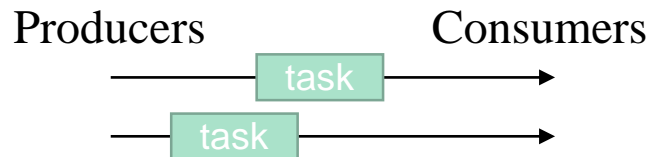
indices / metadata



buffer management

1MB 1MB 1MB 1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...

↓ ↓ ↓ ↓
1 2 3 4

{people, male} → {2,4}

renaming (ids)

used used used

• Indices

- Used for speeding up “queries”
 - Which vertices have label :person?
 - Which edges have value > 1000?

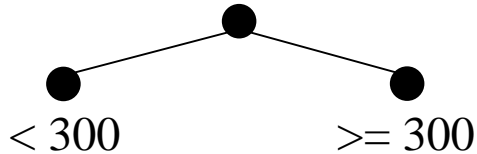
→ **maps, trees**

• Buffer management

- In “real” systems, resource management is very important
- buffer pools
 - no order
 - insertions and deletions
 - no keys

Runtime

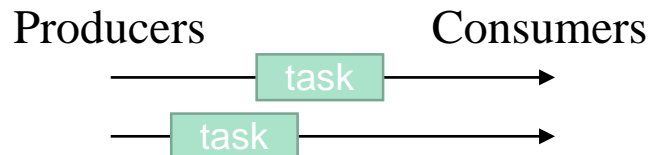
indices / metadata



buffer management

1MB 1MB 1MB 1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...

↓ ↓ ↓ ↓
1 2 3 4

{people, male} → {2,4}

renaming (ids)

used used used

• Indices

- Used for speeding up “queries”
 - Which vertices have label :person?
 - Which edges have value > 1000?

→ **maps, trees**

• Buffer management

- In “real” systems, resource management is very important
- buffer pools
 - no order
 - insertions and deletions
 - no keys

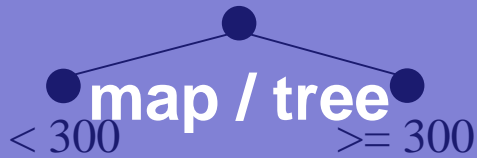
→ Fixed num object pool: **array**

→ Otherwise: **list**

→ Variable-sized elements: **heap**

Runtime

indices / metadata



buffer management

array

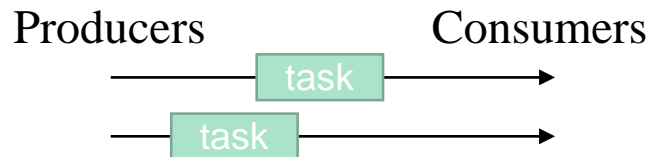
1MB

1MB

1MB

1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...



{people, male} → {2,4}

renaming (ids)

used

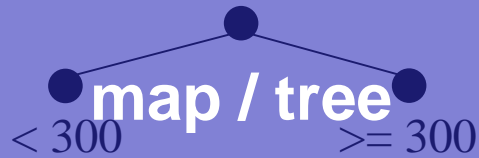
used

used

- Task and job scheduling
 - producers create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements

Runtime

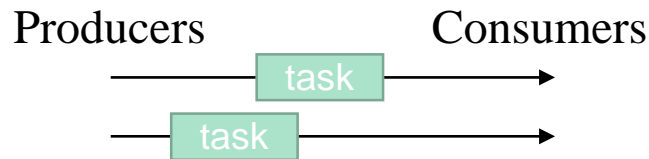
indices / metadata



buffer management



task / job scheduling



labels

:likes, :people, :similar, :male ...



{people, male} → {2,4}

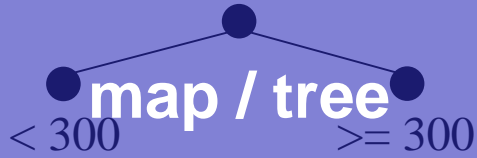
renaming (ids)

used used used

- Task and job scheduling
 - producers create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements→ **queues**
- Storing / querying sets of labels
 - set equality expensive
 - usually common groups
e.g., {person, female}, {person, male}

Runtime

indices / metadata

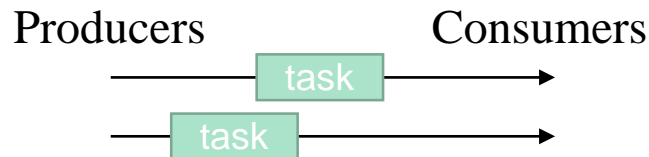


buffer management

array



task / job scheduling



labels

:likes, :people, :similar, :male ...



{people, male} → {2,4}

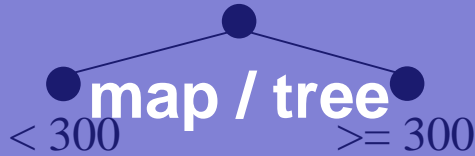
renaming (ids)

used used used

- Task and job scheduling
 - producers create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements→ **queues**
- Storing / querying sets of labels
 - set equality expensive
 - usually common groups
e.g., {person, female}, {person, male}→ 2-level **dictionary** encoding
 - {person, female} → 0
 - {person, male} → 1

Runtime

indices / metadata

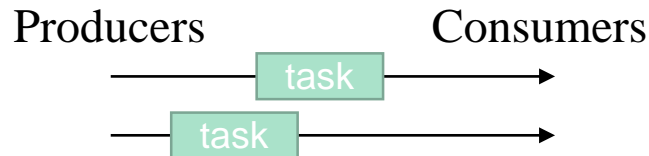


buffer management

array



task / job scheduling



labels

:likes, :people, :similar, :male ...



{people, male} → {2,4}

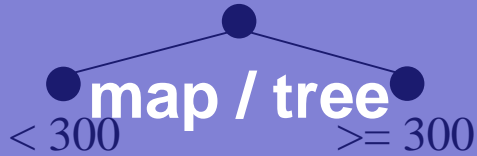
renaming (ids)

used used used

- Task and job scheduling
 - producers create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements→ **queues**
- Storing / querying sets of labels
 - set equality expensive
 - usually common groups
e.g., {person, female}, {person, male}→ 2-level **dictionary** encoding
 - {person, female} → 0
 - {person, male} → 1
- Giving unique ids (renaming)

Runtime

indices / metadata

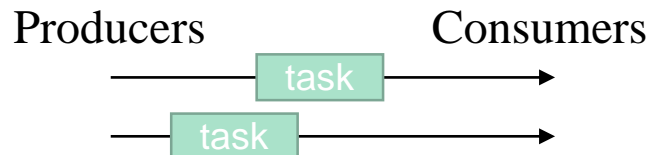


buffer management

array



task / job scheduling



labels

:likes, :people, :similar, :male ...



{people, male} → {2,4}

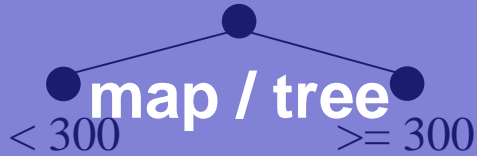
renaming (ids)

used used used

- Task and job scheduling
 - produces create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements→ **queues**
- Storing / querying sets of labels
 - set equality expensive
 - usually common groups
e.g., {person, female}, {person, male}→ 2-level **dictionary** encoding
 - {person, female} → 0
 - {person, male} → 1
- Giving unique ids (renaming)
→ **tree, map, set, counter, other?**

Runtime

indices / metadata



buffer management



task / job scheduling



labels

:likes, :people, :similar, :male ...

dictionary (= map)

{people, male} → {2,4}

renaming (ids)

used **map / tree / set** used

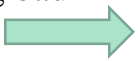
Score

Structure	# Usages
array / buffer	6
map	5
tree / heap	2
set	1
queue	1

Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter



Vasilis, 2
Rachid, 1

distinct


Vasilis
Rachid
Vasilis



Vasilis
Rachid

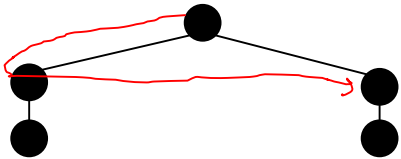
limit (top k)

11 12 0 9 8 13
8 9 11 23 32 9
1 2 3 5 7 3 2 0

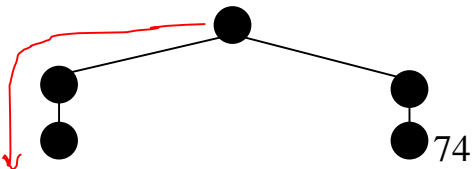


32
23
13

BFS



DFS



- Group by
 1. Mapping from keys to values
 2. Atomic value aggregations
e.g., COUNT, SUM, MAX
- insertion only

Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter → Vasilis, 2
Vasilis, Dexter Rachid, 1

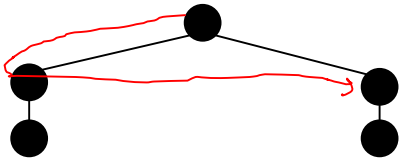
distinct

Vasilis
Rachid
Vasilis → Vasilis
Rachid

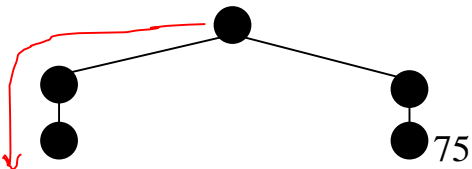
limit (top k)

11 12 0 9 8 13 → 32
8 9 11 23 32 9 23
1 2 3 5 7 3 2 0 13

BFS



DFS

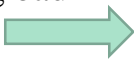


- Group by
 1. Mapping from keys to values
 2. Atomic value aggregations
e.g., COUNT, SUM, MAX
 - insertion only
- hash map
- atomic inc / sum / max, etc.

Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter



Vasilis, 2
Rachid, 1

distinct


Vasilis
Rachid
Vasilis



Vasilis
Rachid

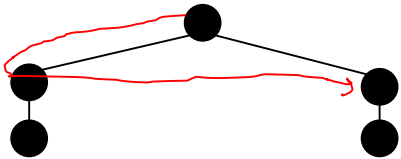
limit (top k)

11 12 0 9 8 13
8 9 11 23 32 9
1 2 3 5 7 3 2 0

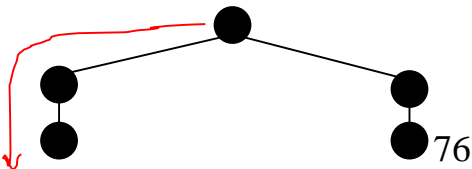


32
23
13

BFS



DFS



- Group by
 1. Mapping from keys to values
 2. Atomic value aggregations
e.g., COUNT, SUM, MAX
 - insertion only


→ hash map

→ atomic inc / sum / max, etc.
- Join
 - create a map of the small table
 - insertion phase, followed by
 - probing phase

Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter



Vasilis, 2
Rachid, 1

distinct


Vasilis
Rachid
Vasilis



Vasilis
Rachid

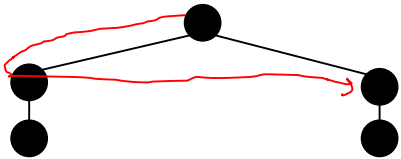
limit (top k)

11 12 0 9 8 13
8 9 11 23 32 9
1 2 3 5 7 3 2 0

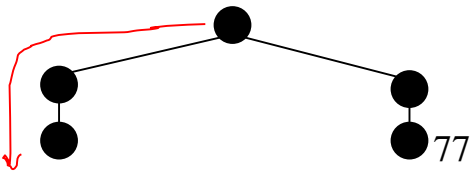


32
23
13

BFS



DFS



- Group by
 1. Mapping from keys to values
 2. Atomic value aggregations
e.g., COUNT, SUM, MAX
 - insertion only

→ hash map

→ atomic inc / sum / max, etc.
- Join
 - create a map of the small table
 - insertion phase, followed by
 - probing phase

→ hash map, lock-free probing

Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter

→

Vasilis, 2
Rachid, 1

map / atomics

distinct

Vasilis
Rachid
Vasilis

→

Vasilis
Rachid

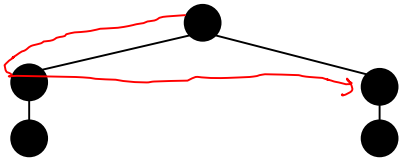
limit (top k)

11 12 0 9 8 13
8 9 11 23 32 9
1 2 3 5 7 3 2 0

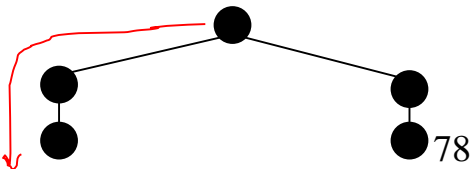
→

32
23
13

BFS



DFS



- Distinct
 - can be solved with sorting, or

Operations

group by / join

Vasilis, Breaking bad → Vasilis, 2
Rachid, Dexter → Rachid, 1
Vasilis, Dexter → Vasilis, 1

map / atomics

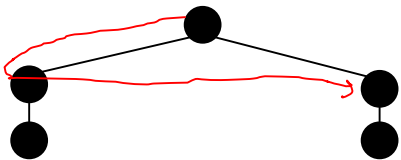
distinct

Vasilis
Rachid
Vasilis → Vasilis
Rachid

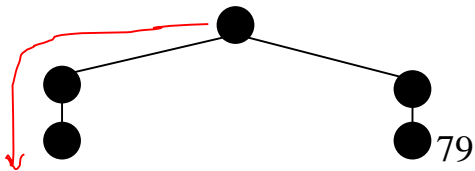
limit (top k)

11 12 0 9 8 13 → 32
8 9 11 23 32 9 → 23
1 2 3 5 7 3 2 0 → 13

BFS



DFS



- Distinct
 - can be solved with sorting, or → **hash set**

Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter

map / atomics

Vasilis, 2
Rachid, 1

distinct

Vasilis
Rachid
Vasilis

→

Vasilis
Rachid

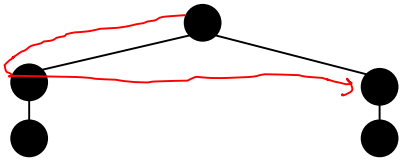
limit (top k)

11 12 0 9 8 13
8 9 11 23 32 9
1 2 3 5 7 3 2 0

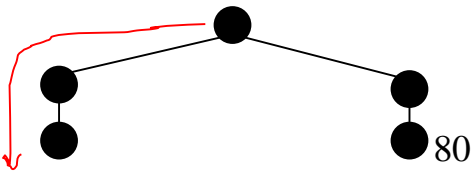
→

32
23
13

BFS



DFS



- Distinct
 - can be solved with sorting, or
→ **hash set**
- Limit (top k)
 - can be solved with sorting, or
 - different specialized structures

Operations

group by / join

Vasilis, Breaking bad → Vasilis, 2
Rachid, Dexter → Rachid, 1
Vasilis, Dexter → Vasilis, 1

map / atomics

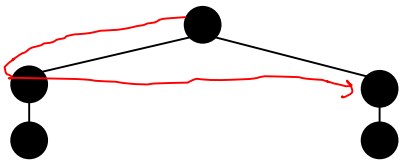
distinct

Vasilis
Rachid
Vasilis → Vasilis
Rachid

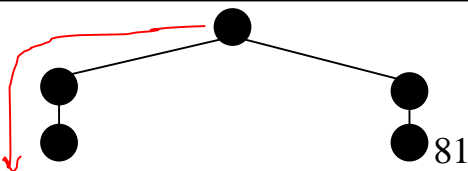
limit (top k)

11 12 0 9 8 13 → 32
8 9 11 23 32 9 → 23
1 2 3 5 7 3 2 0 → 13

BFS



DFS



- Distinct
 - can be solved with sorting, or
→ **hash set**
- Limit (top k)
 - can be solved with sorting, or
 - different specialized structures
→ **tree**
→ **heap**
→ **~ list**
→ **array** (e.g., 2 elements only)
→ **register** (1 element only)

Operations

group by / join

Vasilis, Breaking bad → Vasilis, 2
Rachid, Dexter → Rachid, 1
Vasilis, Dexter → Vasilis, 1

map / atomics

distinct

Vasilis → Vasilis
Rachid → Rachid
Vasilis → Rachid

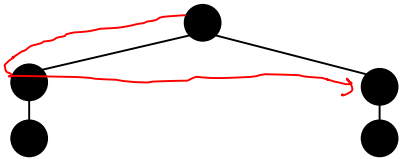
hash set

limit (top k)

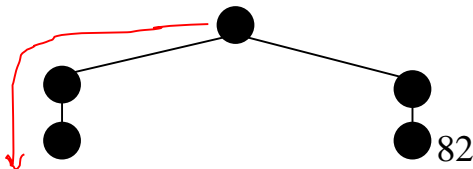
11 12 0 9 8 13 → 32
8 9 11 22 32 9 → 23
1 2 3 5 7 3 2 0 → 13

tree / heap / list

BFS

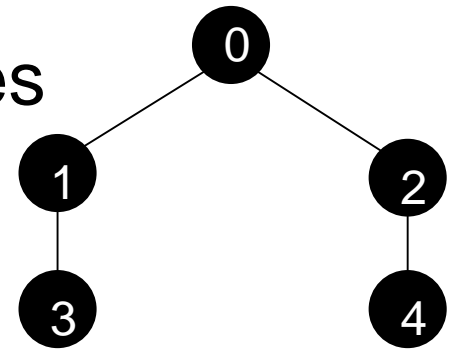


DFS



Breadth-first search (BFS)

- FIFO order
- track visited vertices



Operations

group by / join

Vasilis, Breaking bad → Vasilis, 2
Rachid, Dexter → Rachid, 1
Vasilis, Dexter → Vasilis, 1

map / atomics

distinct

Vasilis → Vasilis
Rachid → Rachid
Vasilis → Rachid

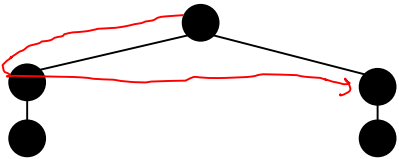
hash set

limit (top k)

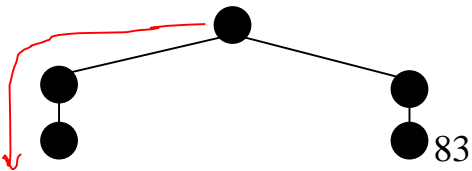
11 12 0 9 8 13 → 32
8 9 11 22 32 9 → 23
1 2 3 5 7 3 2 0 → 13

tree / heap / list

BFS

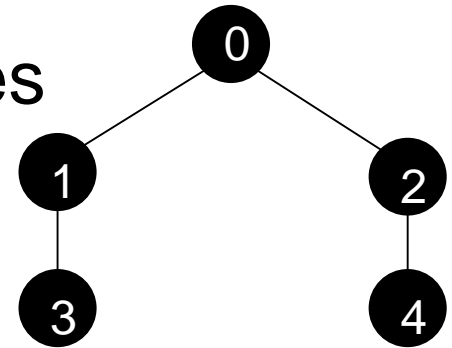


DFS



Breadth-first search (BFS)

- FIFO order
 - track visited vertices
- **queue**
- **set**



Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter

→

Vasilis, 2
Rachid, 1

map / atomics

distinct

Vasilis
Rachid
Vasilis

→

Vasilis
Rachid

hash set

limit (top k)

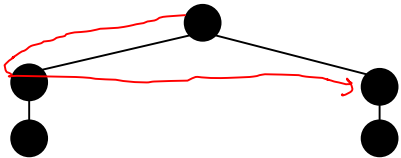
11 12 0 9 8 13
8 9 11 22 32 9
1 2 3 5 7 3 2 0

→

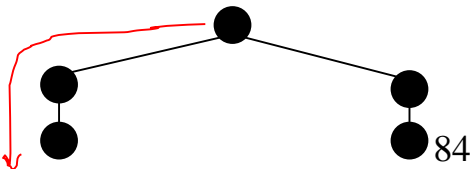
32
23
13

tree / heap / list

BFS

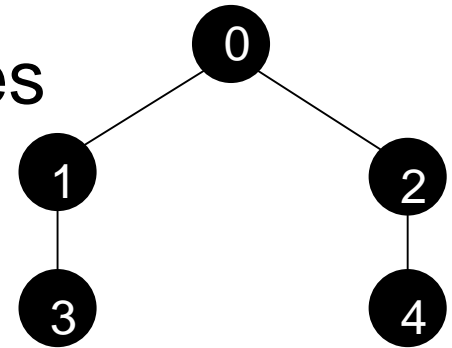


DFS



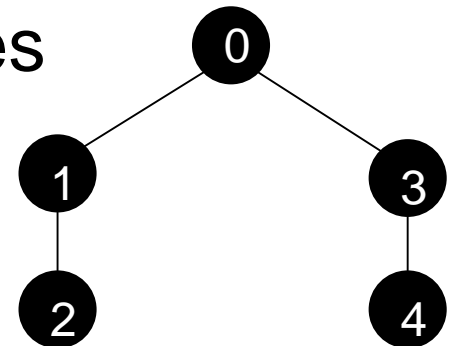
• Breadth-first search (BFS)

- FIFO order
 - track visited vertices
- **queue**
- **set**



• Depth-first search (DFS)

- LIFO order
- track visited vertices



Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter

→

Vasilis, 2
Rachid, 1

map / atomics

distinct

Vasilis
Rachid
Vasilis

→

Vasilis
Rachid

hash set

limit (top k)

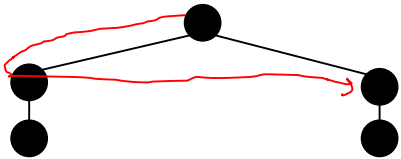
11 12 0 9 8 13
8 9 11 22 32 9
1 2 3 5 7 3 2 0

→

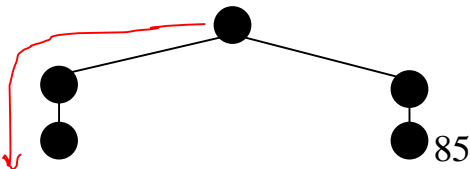
32
23
13

tree / heap / list

BFS

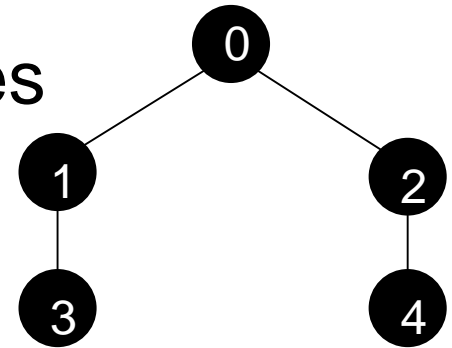


DFS



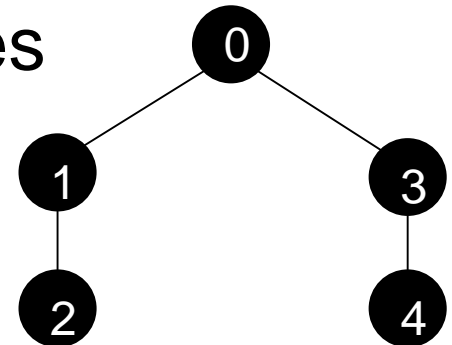
Breadth-first search (BFS)

- FIFO order
 - track visited vertices
- **queue**
- **set**



Depth-first search (DFS)

- LIFO order
 - track visited vertices
- **stack**
- **set**



Operations

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter

Vasilis, 2
Rachid, 1

map / atomics

distinct

Vasilis
Rachid
Vasilis

Vasilis
Rachid

hash set

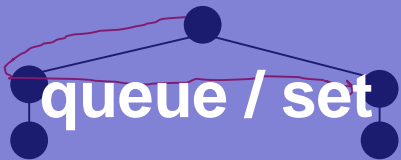
limit (top k)

11 12 0 9 8 13
8 9 11 22 32 9
1 2 3 5 7 3 2 0

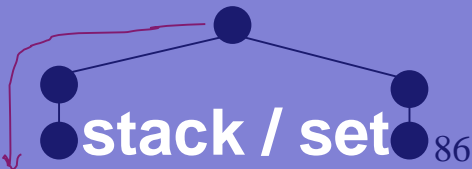
32
23
13

tree / heap / list

BFS



DFS



Score

Structure	# Usages
array / buffer	7
map	6
set	4
tree / heap	3
queue	2
stack	1
list	1

Graph

tmp graph structure



segmented buffer

“Vasilis”, “Breaking bad”, :likes
 “Rachid”, “Dexter”, :likes
 “Dexter”, “Breaking bad”, :similar
 “Breaking bad”, “Dexter”, :similar

graph structure



user-ids - internal ids

Vasilis → 0 0 → Vasilis
 Rachid → 1 1 → Rachid
 Breaking bad → 2 2 → Breaking bad
 Dexter → 3 3 → Dexter

hash map / array

labels

:likes, :people, :similar, ...

properties

“Vasilis”, {people, male}, 33, Zurich
 “Rachid”, {people, male}, ??, Lausanne

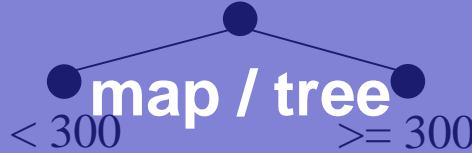
array

lifetime management

number_of_references: X
 stripped counter

Runtime

indices / metadata



buffer management



task / job scheduling



labels

:likes, :people, :similar, :male ...



{people, male} → {2,4}

renaming (ids)



Operations

group by / join

Vasilis, Breaking bad
 Rachid, Dexter
 Vasilis, Dexter

map / atomics

distinct

Vasilis
 Rachid
 Vasilis

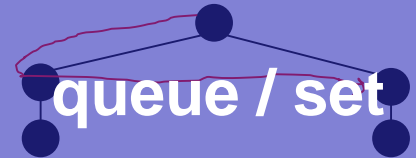
hash set

limit (top k)

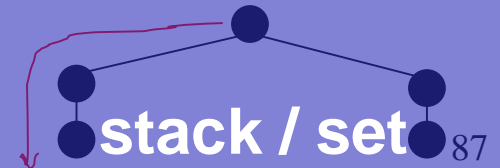
11 12 0 9 8 13
 8 9 11 12 32 9
 1 2 3 5 7 3 2 0

tree / heap / list

BFS



DFS



87

Conclusions

- Both theory and practice are necessary for
 - Designing, and
 - Implementing fast / scalable data structures
- Hardware plays a huge role on implementations
 - How and which memory access patterns to use
- **(Concurrent) Data structures**
 - **The backbone of every system**
 - **An “open” and challenging area or research**