## Implementing Consensus with Timing Assumptions

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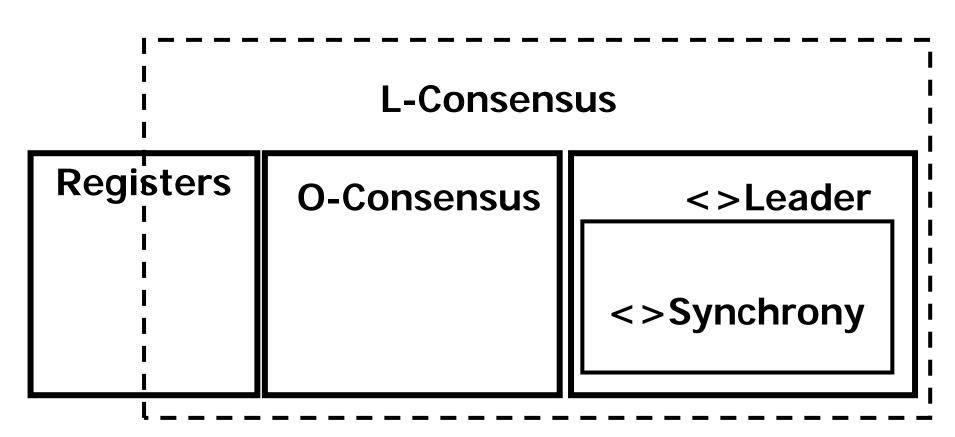


## A Modular Approach

```
We implement Wait-free Consensus (Consensus)
  through:
  Lock-free Consensus (L-Consensus)
 and
  Registers
We implement L-Consensus through
  Obstruction-free Consensus (O-Consensus)
 and
 <>Leader (encapsulating timing assumptions and
  sometimes denoted \Omega)
```

## A Modular Approach

#### Consensus



### Consensus

Wait-Free-Termination: If a correct process proposes, it eventually decides

Agreement: No two processes decide differently

Validity: Any value decided must have been proposed

### L-Consensus

Lock-Free-Termination: If a correct process proposes, at least one correct process eventually decides

Agreement: No two processes decide differently

Validity: Any value decided must have been proposed

### O-Consensus

Obstruction-Free-Termination: If a correct process proposes and eventually executes alone, the process eventually decides

Agreement: No two processes decide differently

Validity: Any value decided must have been proposed

## Example 1

## Example 2

## O-Consensus Algorithm (idea)

- A process that is eventually « left alone / scheduled » to execute steps, eventually decides
- Several processes might keep trying to concurrently decide until some (unknown) time: agreement (and validity) should be ensured during this preliminary period

- (1) pi announces its timestamp
- (2) pi selects the value with the highest timestamp
- (3) pi announces the value with its timestamp
- (4) if pi's timestamp is the highest, pi decides

## O-Consensus Algorithm (data)

- Each process pi maintains a timestamp ts, initialized to i and incremented by n
- The processes share an array of register pairs *Reg[1,...,n]*; each element of the array contains two registers:
  - Reg[i]. T contains a timestamp (init to 0)
  - *Reg[i].V* contains a pair (value, timestamp) (init to  $(\bot,0)$ )

# O-Consensus Algorithm (functions)

- To simplify the presentation, we assume two functions applied to Reg[1,..,N]
  - \* highestTsp() returns the highest timestamp among all elements Reg[1].T, Reg[2].T, ..., Reg[N].T
  - \*\* highestTspValue() returns the value with the highest timestamp among all elements Reg[1].V, Reg[2].V, .., Reg[N].V

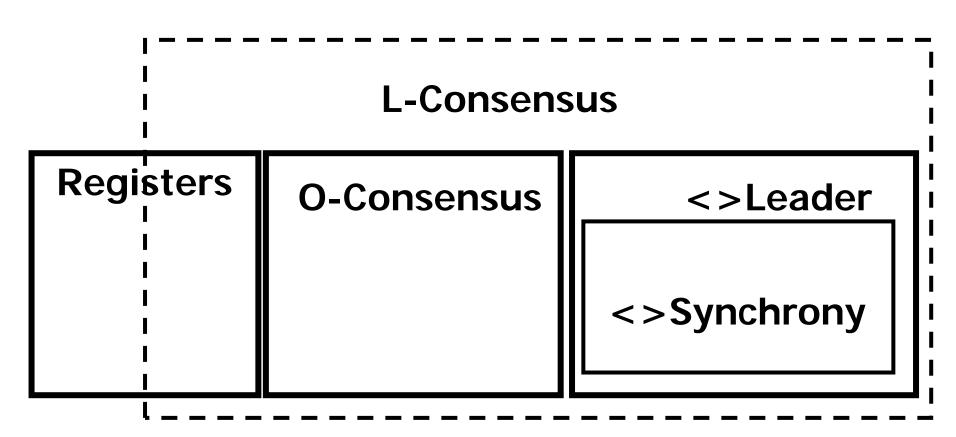
```
propose(v):
while(true)
   Reg[i].T.write(ts);
   val := Reg[1,..,n].highestTspValue();
   \checkmark if val = \bot then val := v;
   Reg[i].V.write(val,ts);
   if ts = Reg[1,..,n].highestTsp() then
         return(val)
   r ts := ts + n
```

- (1) pi announces its timestamp
- (2) pi selects the value with the highest timestamp (or its own if there is none)
- (3) pi announces the value with its timestamp
- (4) if pi's timestamp is the highest, then pi decides (i.e., pi knows that any process that executes line 2 will select pi's value)

```
propose(v):
while(true)
   (1) Reg[i].T.write(ts);
   (2) val := Reg[1,..,n].highestTspValue();
   \checkmark if val = \bot then val := v;
   (3) Reg[i].V.write(val,ts);
   \sim (4) if ts = Reg[1,..,n].highestTsp() then
         return(val)
   r ts := ts + n
```

## A Modular Approach

#### Consensus



#### L-Consensus

- We implement L-Consensus using
- (a) <>leader (leader()) and
- (b) the O-Consensus algorithm
- The idea is to use <>leader to make sure that, eventually, one process keeps executing steps alone, until it decides

#### <> Leader

- One operation *leader()* which does not take any input parameter and returns, as an output parameter, a boolean
- A process considers itself leader if the boolean is true
  - ✓ Property: If a correct process invokes leader, then the invocation returns and eventually, some correct process is permanently the only leader

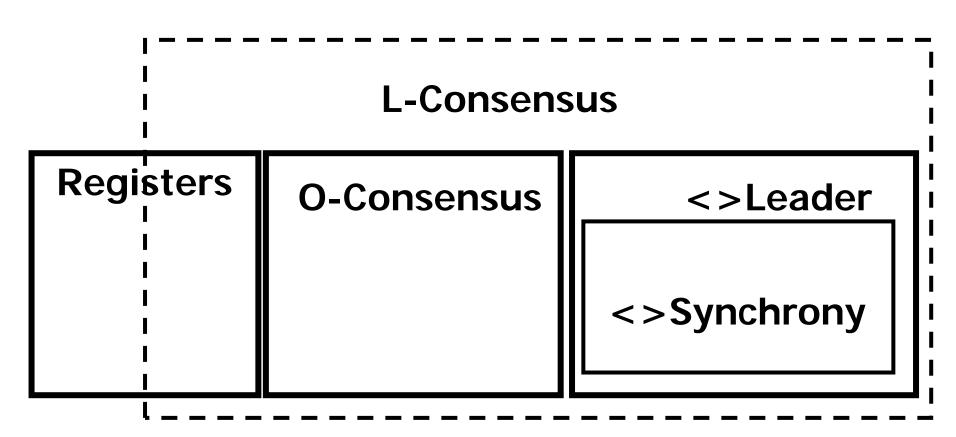
## Example

#### L-Consensus

```
propose(v): while(true)
   f if leader() then
      Reg[i].T.write(ts);
      val := Reg[1,..,n].highestTspValue();
      r if val = \perp then val := v;
      Reg[i].V.write(val,ts);
      r if ts = Reg[1,..,n].highestTsp()
            then return(val)
      r ts := ts + n
```

## A Modular Approach

#### Consensus



# From L-Consensus to Consensus (helping)

 Every process that decides writes its value in a register *Dec* (init to ⊥)

Every process periodically seeks for a value in Dec

#### Consensus

```
propose(v)
while (Dec.read() = \perp)
if leader() then
   Reg[i].T.write(ts);
   val := Reg[1,..,n].highestTspValue();
  r if val = \perp then val := p;
  Reg[i].V.write(val,ts);
  r if ts = Reg[1,..,n].highestTsp()
             then Dec.write(val)
   r ts := ts + n;
return(Dec.read())
```

#### <> Leader

- One operation *leader()* which does not take any input parameter and returns, as an output parameter, a boolean
- A process considers itself leader if the boolean is true
  - ✓ Properties: (a) If a correct process invokes leader(), then the invocation returns and (b) if a correct process keeps invoking leader(), then eventually, some correct process is permanently the only leader

### <>Leader: Algorithm

- We assume that the system is <>synchronous
  - ✓ There is a time after which there is a lower and an upper bound on the delay for a process to execute a local action, a read or a write in shared memory
  - NB. The time after which the system becomes synchronous is called the global stabilization time (GST) and is unknown to the processes
- This model captures the practical observation that concurrent systems are usually synchronous and sometimes asynchronous

# <>Leader: Algorithm (shared variables)

Every process pi elects (stores in a local variable leader) the process with the lowest identity that pi considers as non-crashed:

NB. if pi elects pj, then i = j or j < i

- A process pi that considers itself leader keeps incrementing Reg[i]; pi claims leadership
- NB. Eventually, only the leader increments Reg[]

# <>Leader: Algorithm (local variables)

 Every process periodically increments local variables *clock* and *check*, as well as a local variable *delay* whenever its leader changes

 Process pi maintains *lasti[j]* to record the last value of *Reg[j]* pi has read (pi can hence know whether pj has progressed)

# <>Leader: Algorithm (variables)

The next leader is the one with the smallest id that makes some progress; if no such process pj such that j<i exists, then pi elects itself (noLeader is true)

### <>Leader: Algorithm

leader(): return(leader)

- leader init to self
- check and delay init to 1
- clock, lasti[j] and Reg[j] init to 0;
- Task:

### <>Leader: Algorithm (cont'd)

```
elect():
noLeader := true;
for j = 1 to (i-1) do

√ if (Reg[i].read() > last[j]) then

       last[j] := Reg[j].read();

√ if(leader ≠ pj) then delay:=delay + 2;

✓ check := check + delay;

   ✓ leader:= pj;
   ✓ noLeader := false;

✓ break (for);

• if (noLeader) then leader := self;
```

## Consensus = Registers + <> Leader

- <>Leader has one operation *leader()* which does not take any input parameter and returns, as an output parameter, a boolean (a process considers itself leader if the boolean is true)
  - ✓ Property: If a correct process invokes leader, then the invocation returns and eventually, some correct process is *permanently* the only leader
- <>Leader encapsulates the following synchrony assumption: there is a time after which a lower and an upper bound hold on the time it takes for every process to execute a step (eventual synchrony)

## A Modular Approach

#### Consensus

