

# Concurrent Algorithms (Overview)

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***In short***

***This course is about the principles  
of robust concurrent computing***

# ***Principles***

Certain things are **incorrect** and it is important to understand why  
(at least what correctness means)

Certain things are **impossible** and its important to understand why  
(at least to not try)

# ***WARNING***

- This course is different from the course :  
**Distributed Algorithms**
- shared memory vs message passing
- It does make a lot of sense to take both

Major chip manufacturers have announced what is perceived as a major paradigm shift in computing:

***Multiprocessors vs faster processors***

Maybe Moore was wrong...

Major chip manufacturers have announced a major paradigm shift:

*New York Times, 8 May 2004:*

Intel ... [has] decided to focus its development efforts on «dual core» processors ... with two engines instead of one, allowing for greater efficiency because the processor workload is essentially shared.

The clock speed of a processor cannot be increased without overheating

***But***

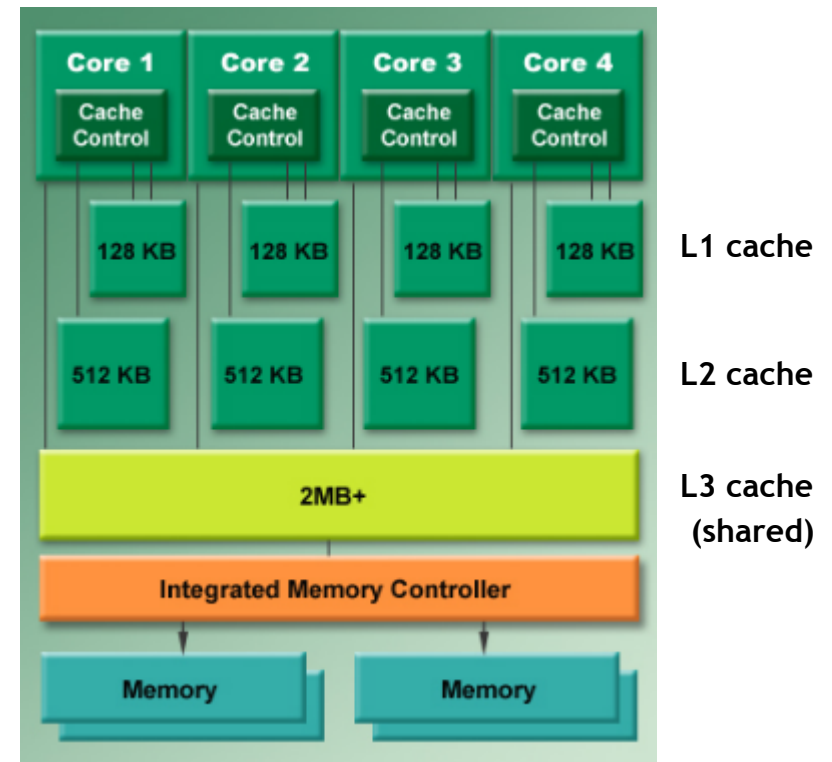
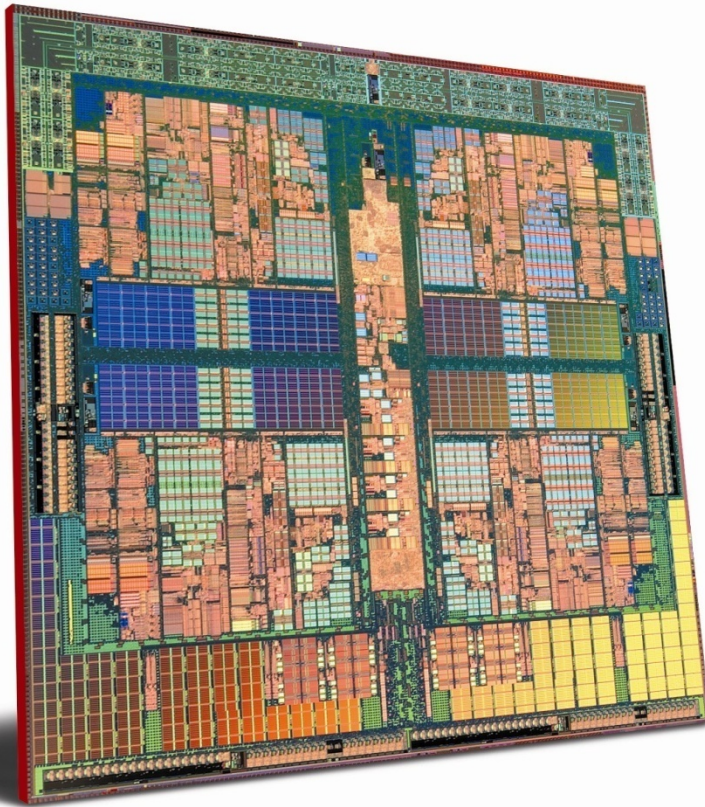
More and more processors can fit in the same space

# ***Multicores **are** almost everywhere***

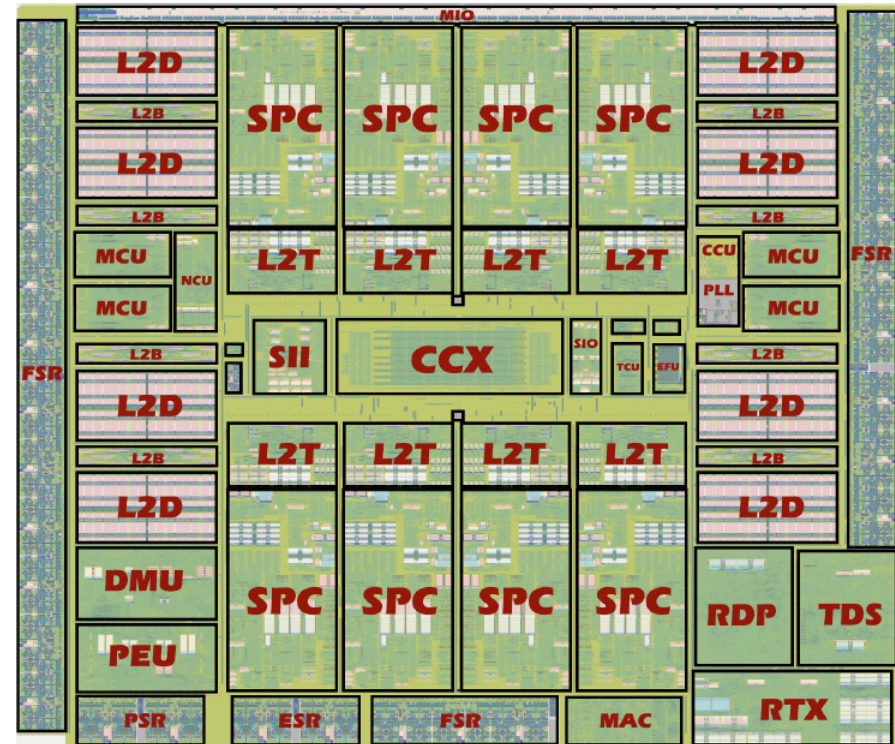
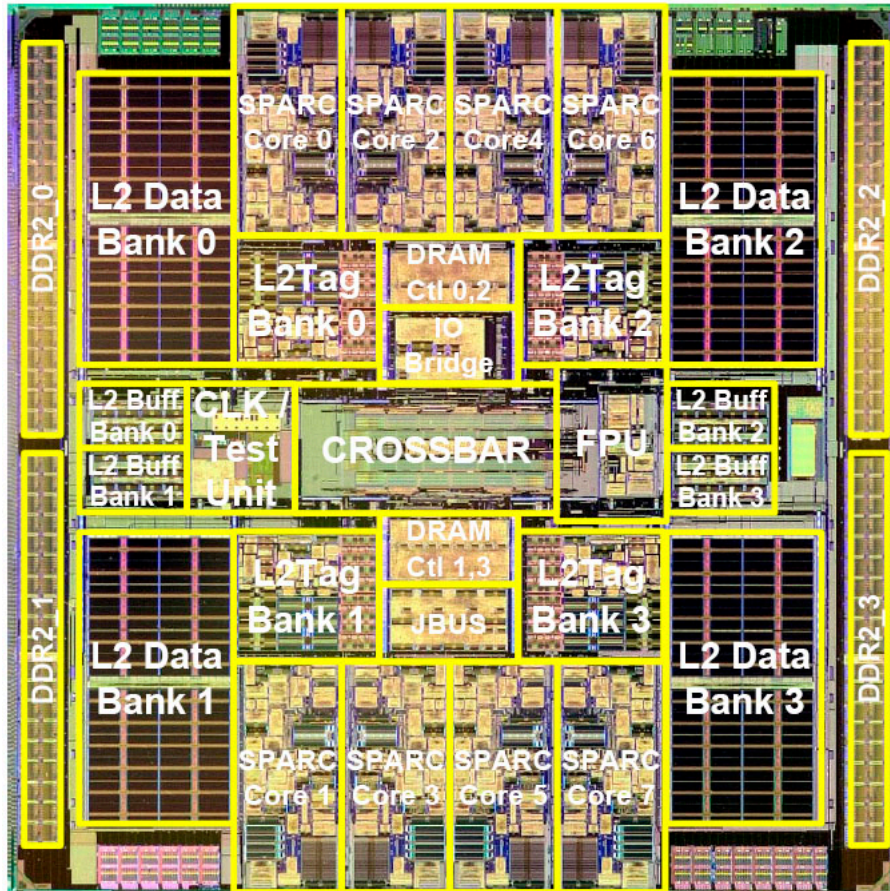
- ☞ **Dual-core** commonplace in laptops
- ☞ **Quad-core** in desktops
- ☞ **Dual quad-core** in servers
- ☞ **All major chip manufacturers produce multicore CPUs**
  - **SUN Niagara** (8 cores, 32 threads)
  - **Intel Xeon** (4 cores)
  - **AMD Opteron** (4 cores)



# AMD Opteron (4 cores)



# SUN's Niagara CPU2 (8 cores)



- |                             |  |
|-----------------------------|--|
| CCX – Crossbar              | L2T – L2 tag arrays                        |
| CCU – Clock control         | MCU – Memory controller                    |
| DMU/PEU – PCI Express       | MIO – Miscellaneous I/O                    |
| EFU – Efuse for redundancy  | PSR – PCI Express SERDES                   |
| ESR – Ethernet SERDES       | RDP/TDS/RTX/MAC – Ethernet                 |
| FSR – FBD SERDES            | SII/SIO – I/O data path to and from memory |
| L2B – L2 write-back buffers | SPC – SPARC cores                          |
| L2D – L2 data arrays        | TCU – Test and control unit                |

# ***Multiprocessors***

- Multiple hardware processors: each executes a series of processes (software constructs) modeling sequential programs
- Multicore architecture: multiple processors are placed on the same chip

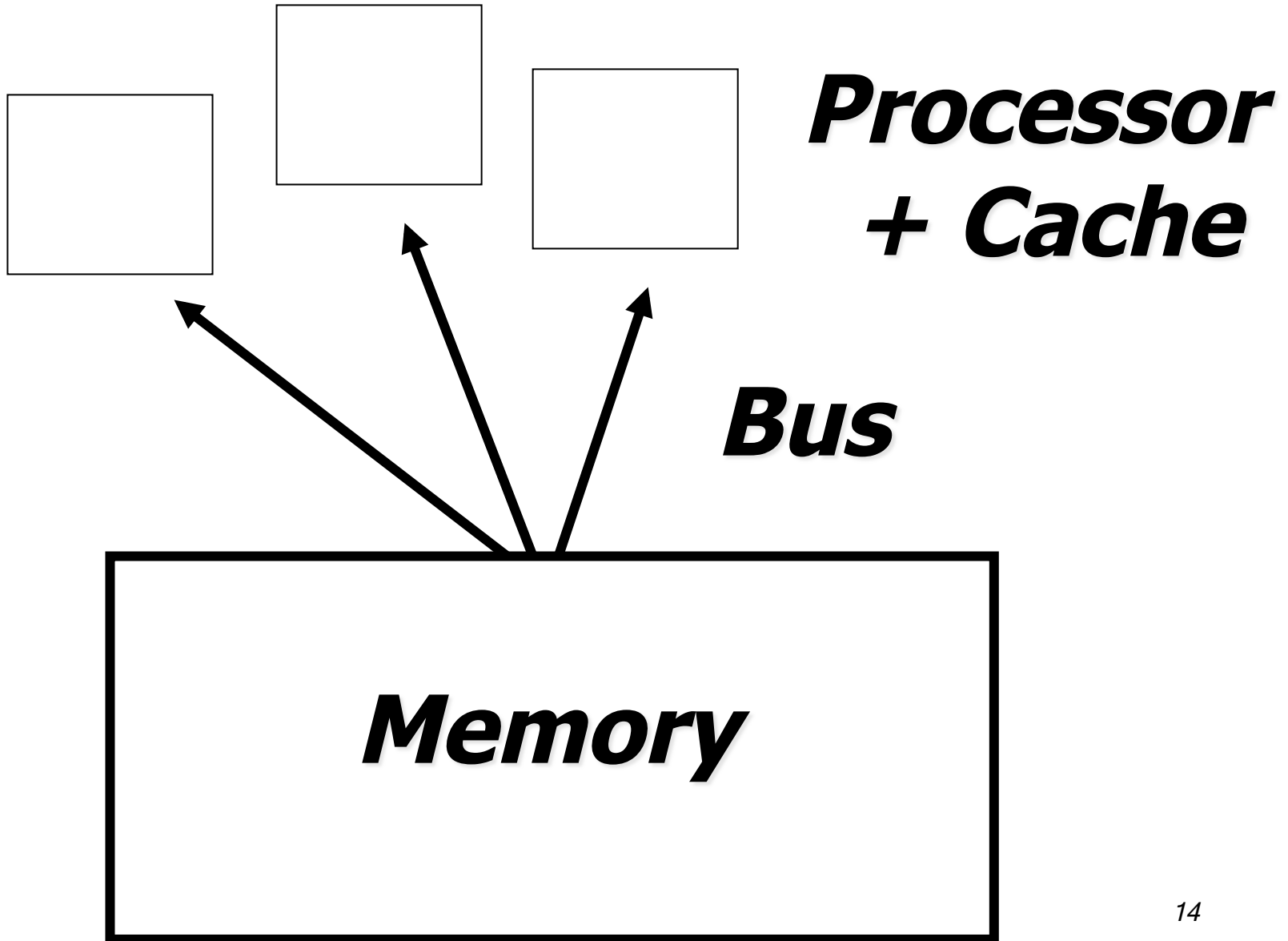
# *Principles of an architecture*

- ☛ Two fundamental components that *fall apart*: **processors** and **memory**
- ☛ The Interconnect links the processors with the memory:
  - ☛ - **SMP** (symmetric): bus (a tiny Ethernet)
  - ☛ - **NUMA** (network): point-to-point network

# *Cycles*

- ☛ The basic unit of time is the cycle: time to execute an instruction
- ☛ This changes with technology but the relative cost of instructions (local vs memory) does not

# Simple view



# ***Hardware synchronization objects***

- The basic unit of communication is the read and write to the memory (through the cache)
- More sophisticated objects are sometimes provided and, as we will see, necessary: C&S, T&S, LL/SC

# ***The free ride is over***

- ☞ Cannot rely on CPUs getting faster in every generation
- ☞ Utilizing more than one CPU core requires concurrency



# ***The free ride is over***

- ☞ One of the biggest future software challenges: **exploiting concurrency**
  - Every programmer will have to deal with it
  - Concurrent programming is hard to get right

Speed will be achieved by having several processors work on independent parts of a task

***But***

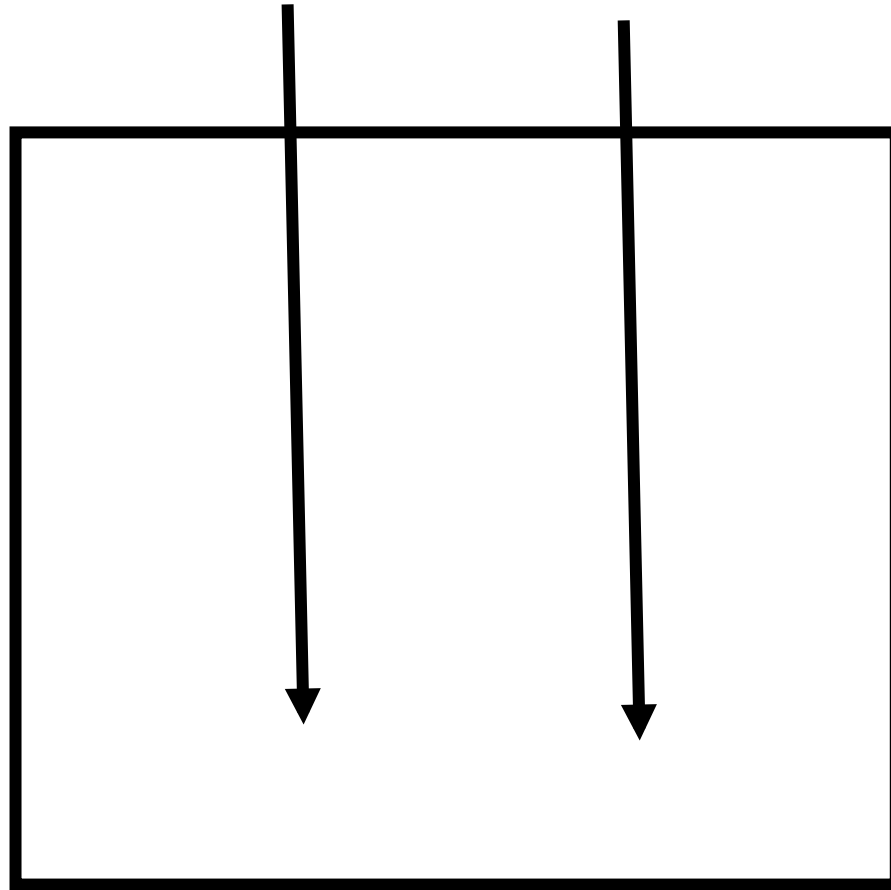
the processors would occasionally need to pause and synchronize

# Why synchronize?

***But***

If the task is indeed common, then pure parallelism is usually impossible and, at best, inefficient

# Concurrent processes



**Shared object**

# Counter

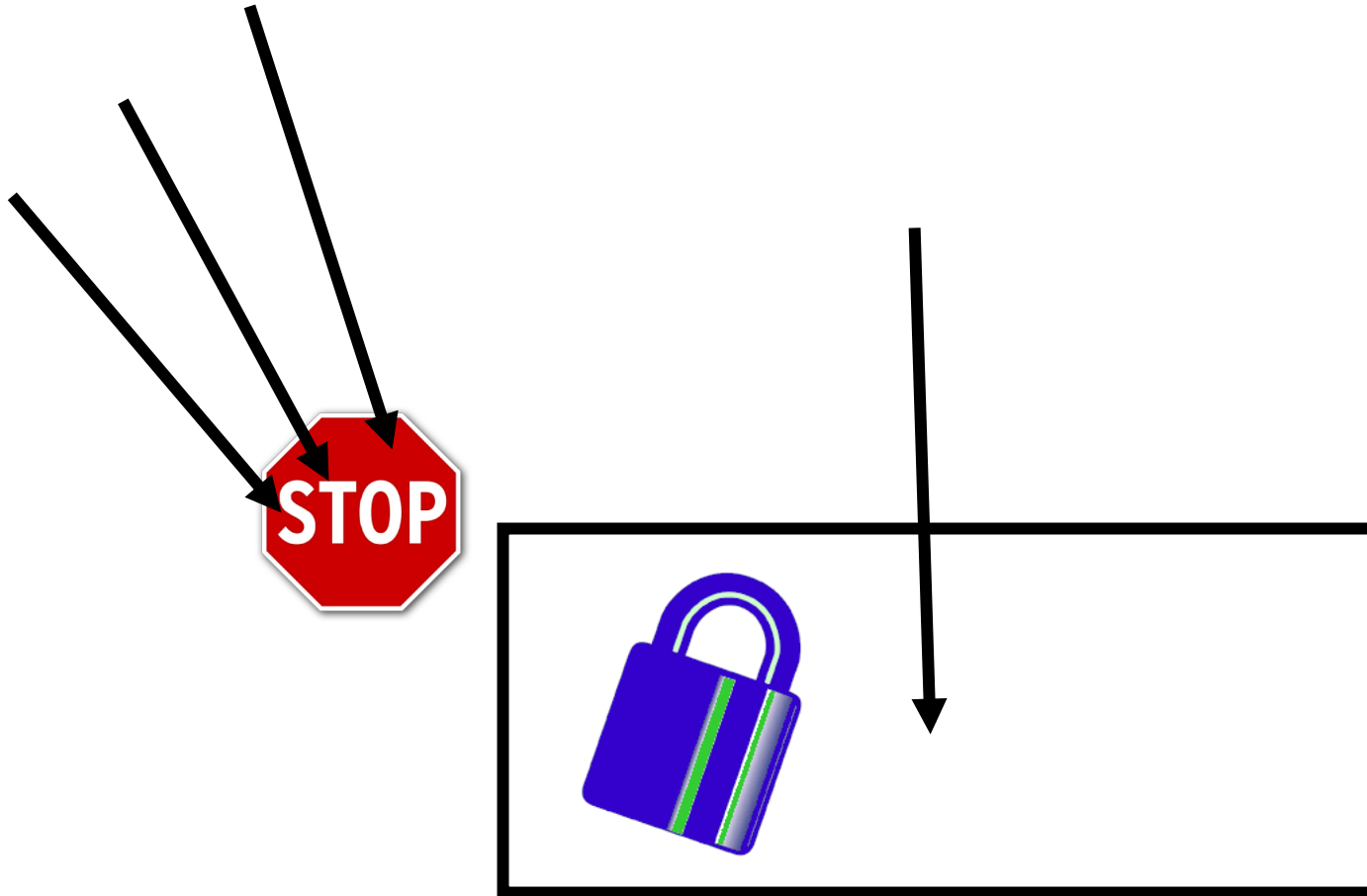
```
public class Counter

private long value;

public Counter(int i) { value = i;}

public long getAndIncrement()
{
return value++;
}
```

# Locking (mutual exclusion)



**Locked object**

# Locking with compare&swap()

- A **Compare&Swap** object maintains a value  $x$ , init to  $\perp$ , and  $y$ ;
- It provides one operation: ***c&s(old,new);***
  - ✓ Sequential spec:
    - $c&s(old,new)$   
{ $y := x$ ; if  $x = old$  then  $x := new$ ; return( $y$ )}

# Locking with compare&swap()

```
lock() {  
  repeat until  
  unlocked = this.c&s(unlocked,locked)  
}
```

```
unlock() {  
  this.c&s(locked,unlocked)  
}
```



# Locking with test&set()

- A ***test&set*** object maintains binary values  $x$ , init to 0, and  $y$ ;
- It provides one operation: ***t&s()***
  - ✓ Sequential spec:
  - ✓  $t\&s() \{y := x; x := 1; \text{return}(y);\}$

# Locking with test&set()

```
lock() {  
  repeat until (0 = this.t&s());  
}
```

```
unlock() {  
  this.setState(0);  
}
```

# Locking with test&set()

```
lock() {  
  while (true)  
  {  
    repeat until (0 = this.getState());  
    if 0 = (this.t&s()) return(true);  
  }  
}
```

```
unlock() {  
    this.setState(0);  
}
```

# Explicit use of a lock

```
Lock l = ...;  
    l.lock();  
    try {  
// access the resource protected by this lock  
    } finally {  
        l.unlock();  
    }
```

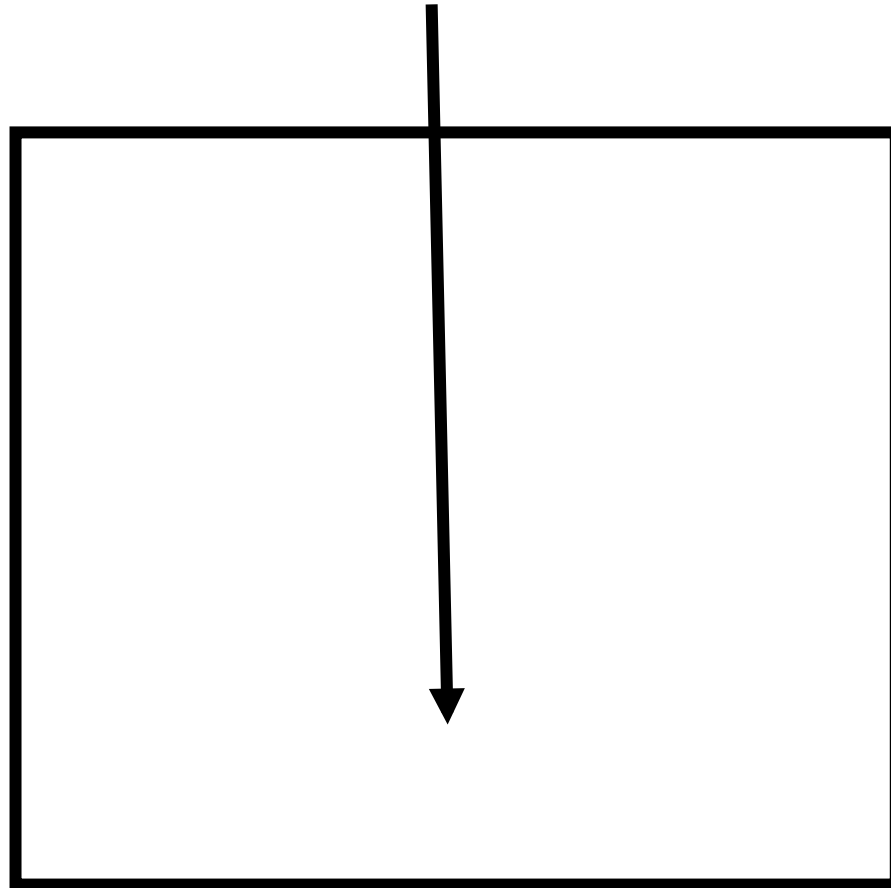
# Implicit use of a lock

```
public class SynchronizedCounter {  
    private int c = 0;  
    public synchronized void increment() {  
        c++;  
    }  
    public synchronized void getAndincrement()  
{  
        c++; return c;  
    }  
    public synchronized int value() {  
        return c;  
    }  
}
```

# Locking (mutual exclusion)

- **Difficult:** 50% of the bugs reported in Java come from the mis-use of « synchronized »
- **Fragile:** a process holding a lock prevents all others from progressing
- **Slow:** the act of locking itself impacts performance

**Locked object**



**One process at a time**

# Processes are asynchronous

- *Page faults*
- *Pre-emptions*
- *Failures*
- *Cache misses, ...*



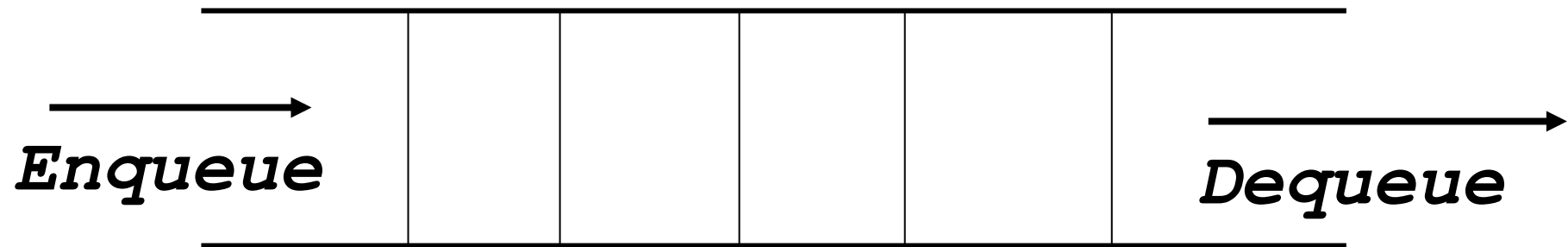
# Processes are asynchronous

- ☛ A cache miss can delay a process by ten instructions
- ☛ A page fault by few millions
- ☛ An os preemption by hundreds of millions...

***Coarse grained locks => slow***

***Fine grained locks => errors***

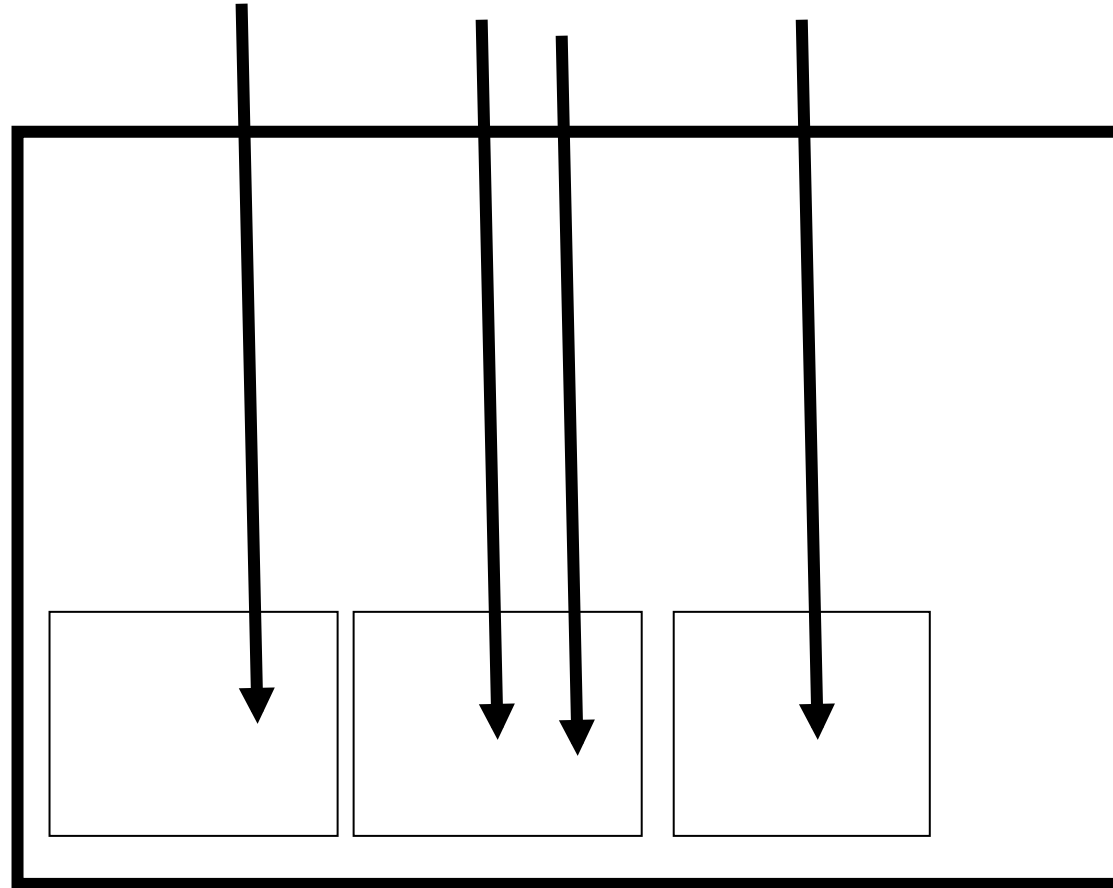
# *Double-ended queue*



# Processes are asynchronous

- *Page faults, pre-emptions, failures, cache misses, ...*
- A process can be delayed by millions of instructions ...

# Alternative to locking?



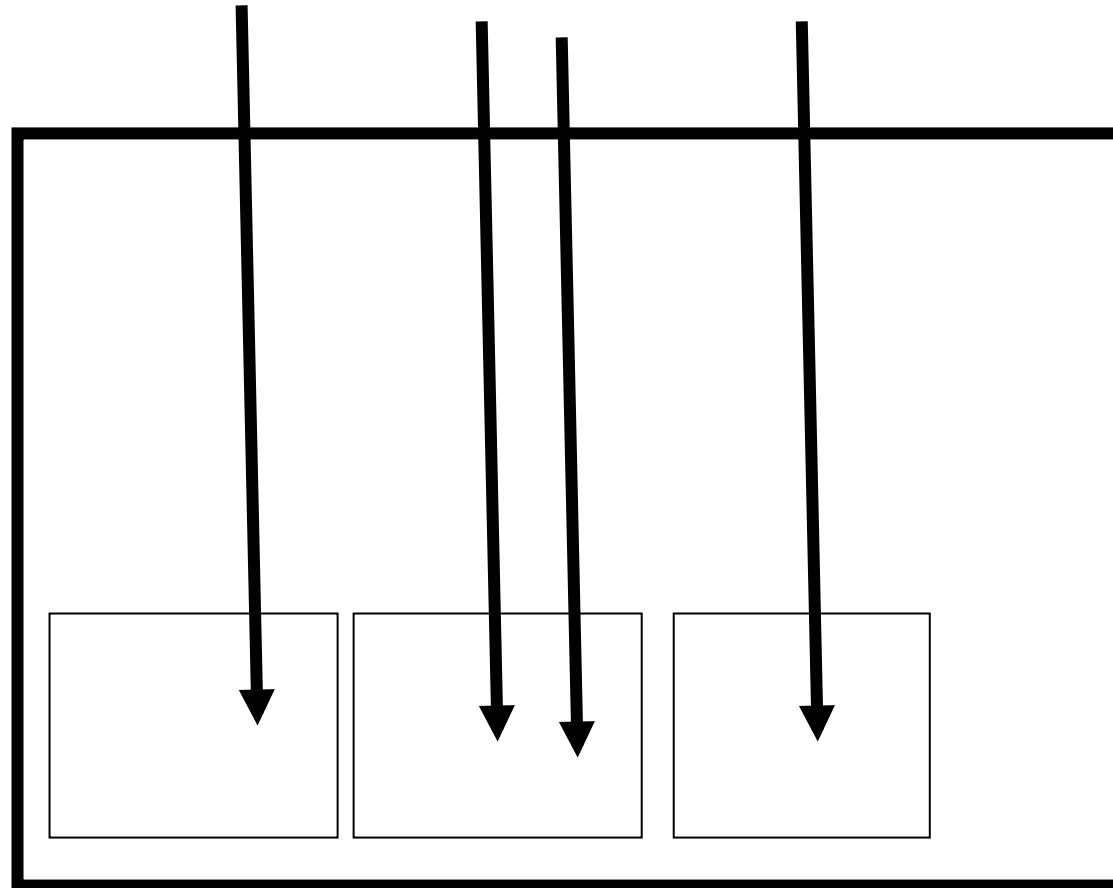
# Wait-free atomic objects

- ***Wait-freedom:*** every process that invokes an operation eventually returns from the invocation (robust ... unlike locking)
- ***Atomicity:*** every operation appears to execute instantaneously (as if the object was locked...)

# In short

This course shows how to  
***wait-free*** implement high-level  
***atomic*** objects out of more  
primitive base objects

# Concurrent processes



**Shared object**



# This course

- *Theoretical but no specific theoretical background*
- *Exercices throughout the semester*
- *Written exam at the end*

# Roadmap

- *Model*
  - *Processes and objects*
  - *Atomicity and wait-freedom*
- *Examples*
- *Content*

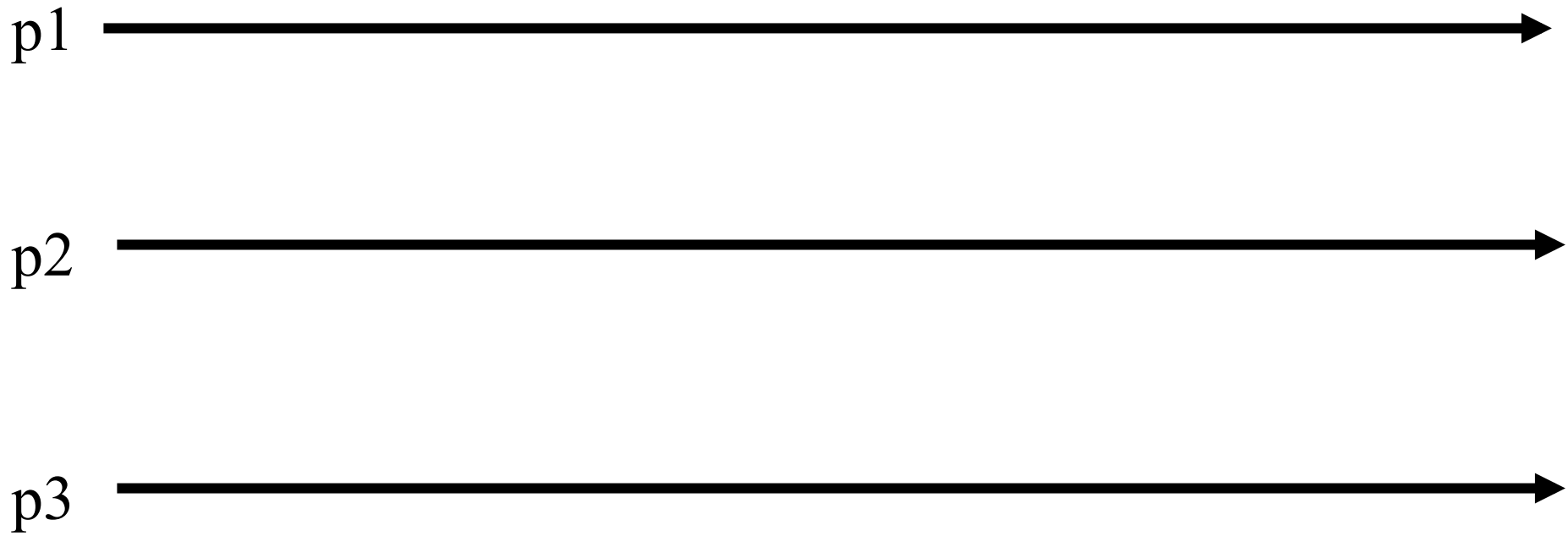
# Processes

- We assume a finite set of processes
- Processes are denoted by  $p_1, \dots, p_N$  or  $p, q, r$
- Processes have unique identities and know each other (unless explicitly stated otherwise)

# Processes

- Processes are ***sequential*** units of computations
- Unless explicitly stated otherwise, we make no assumption on process (relative) speed

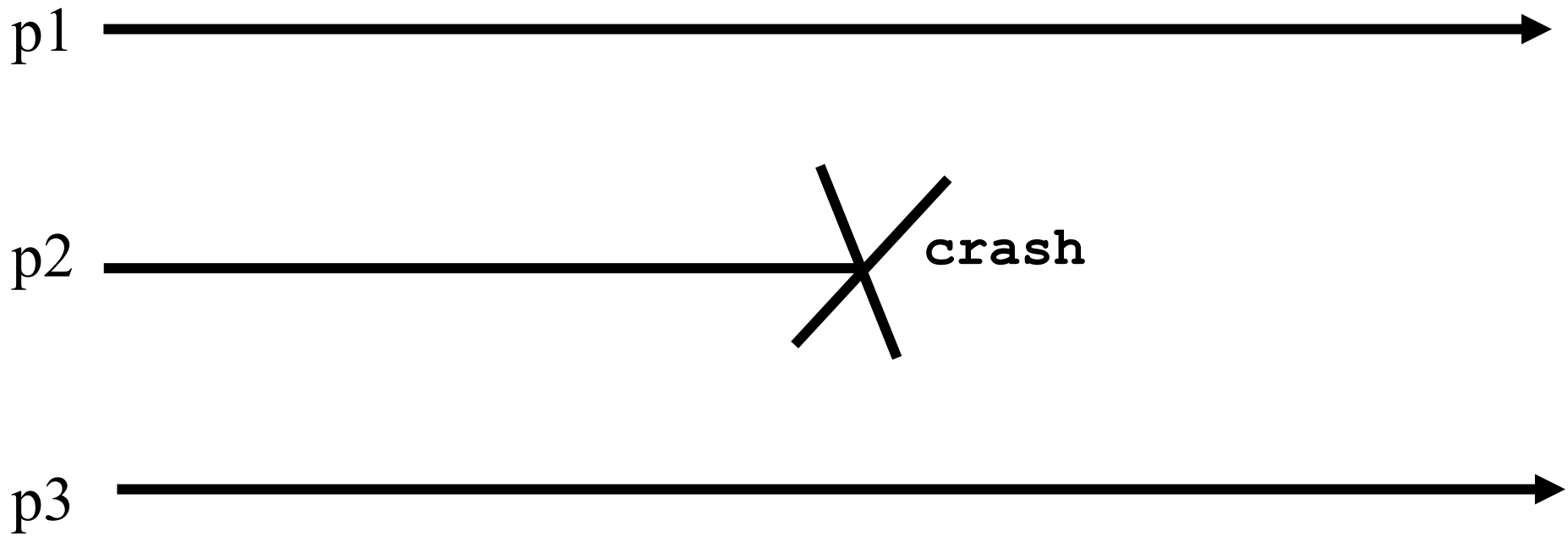
# Processes



# Processes

- A process either executes the algorithm assigned to it or crashes
- A process that crashes does not recover (in the context of the considered computation)
- A process that does not crash in a given execution (computation or run) is called correct (in that execution)

# Processes

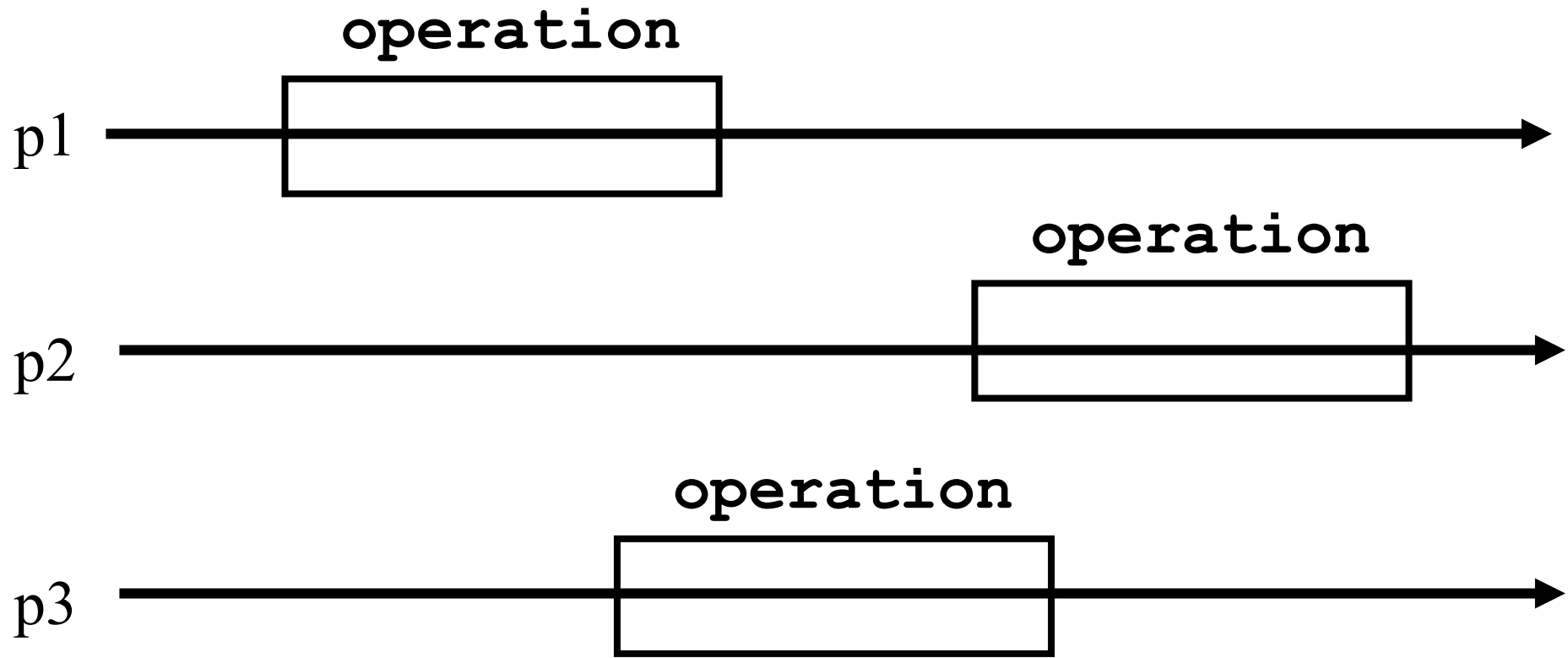


# On objects and processes

- Processes execute local computation or access shared objects through their ***operations***
- Every operation is expected to return a reply



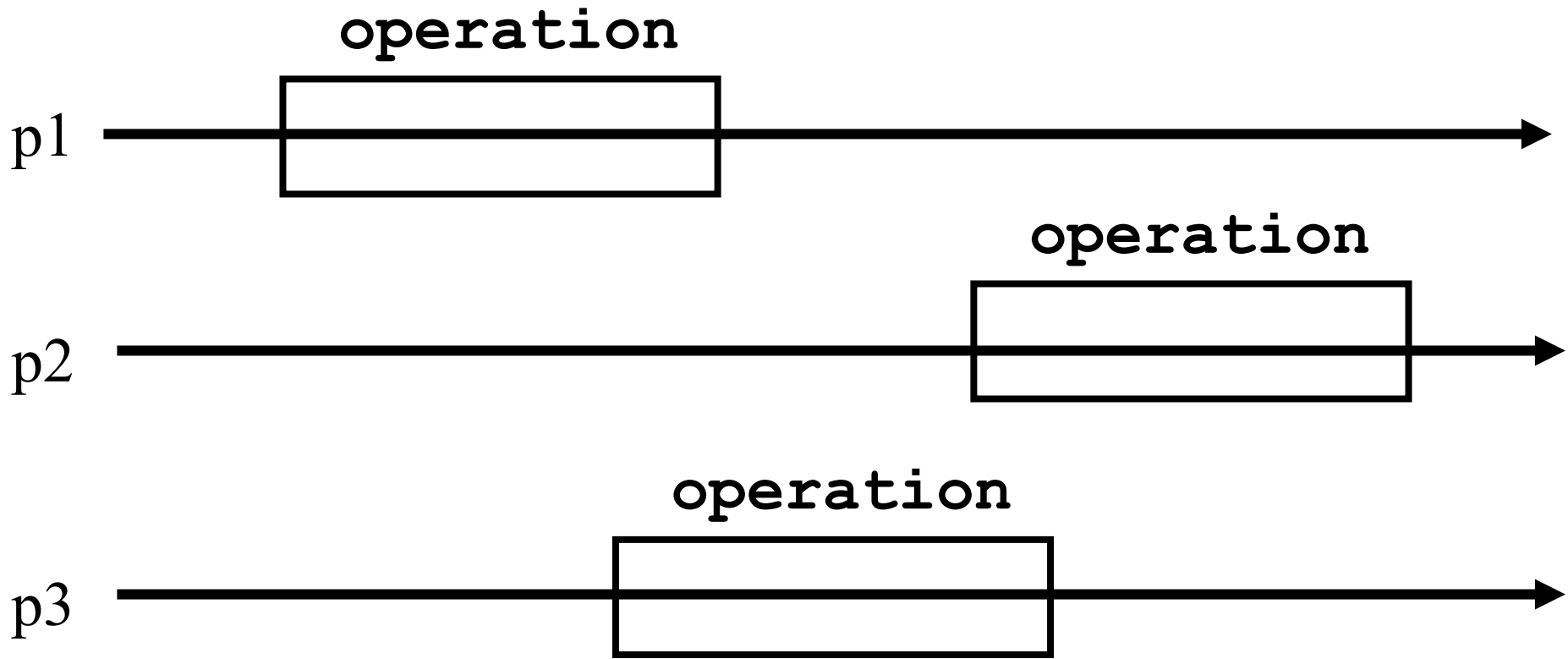
# Processes



# On objects and processes

- ***Sequentiality*** means here that, after invoking an operation  $op_1$  on some object  $O_1$ , a process does not invoke a new operation (on the same or on some other object) until it receives the reply for  $op_1$
- ***Remark.*** Sometimes we talk about operations when we should be talking about operation invocations

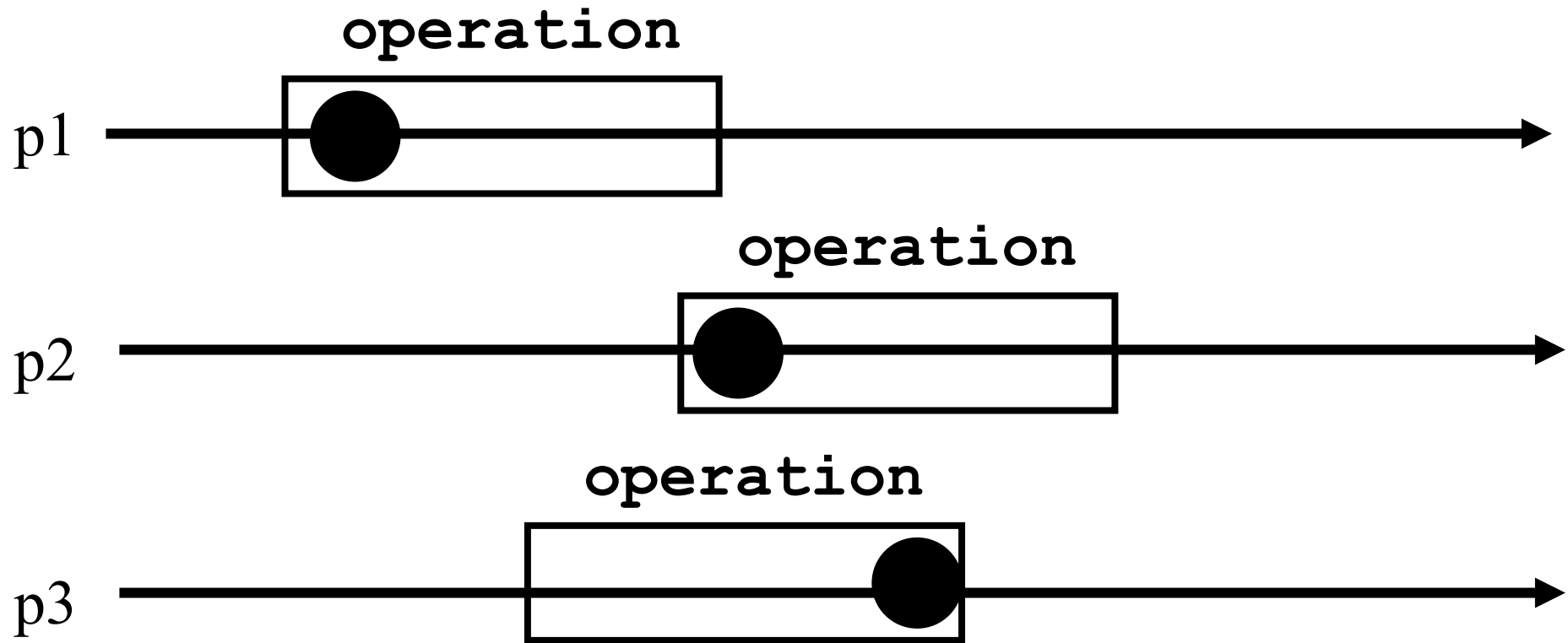
# Processes



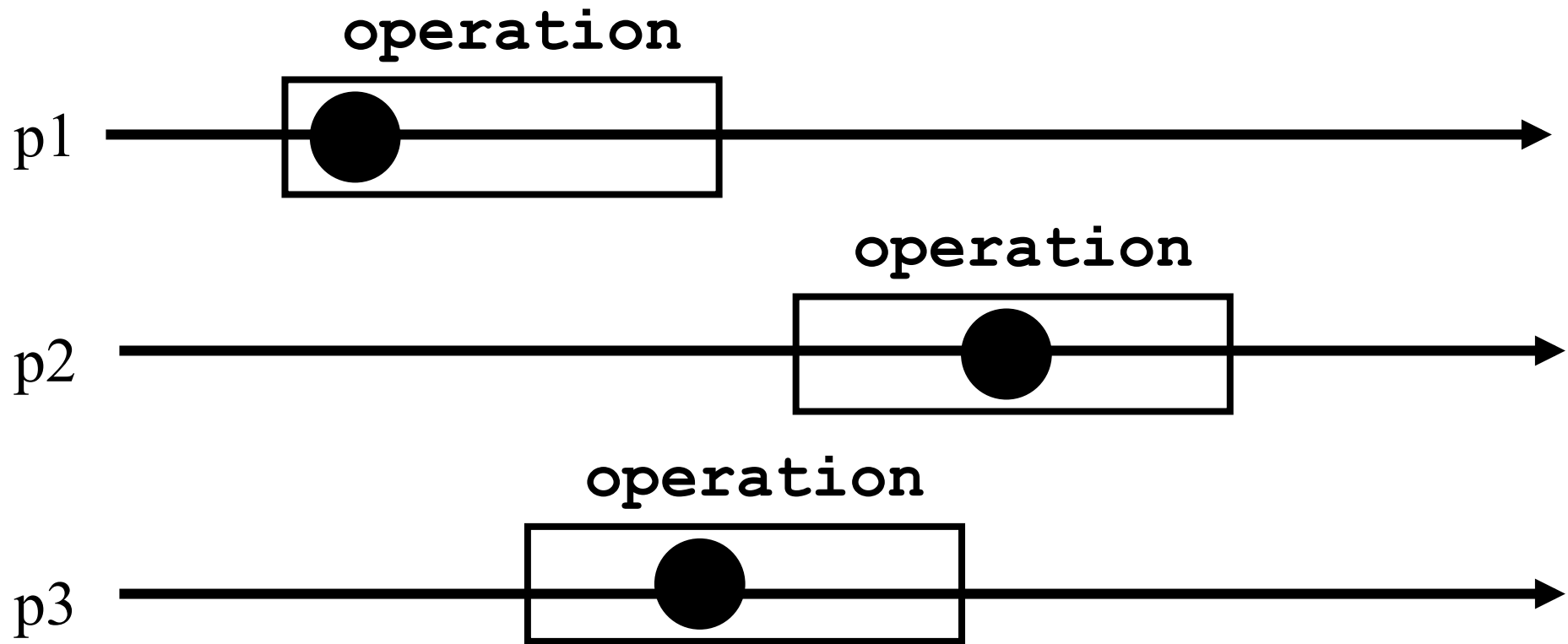
# Atomicity

- Every operation appears to execute at some indivisible point in time (called linearization point) between the invocation and reply time events

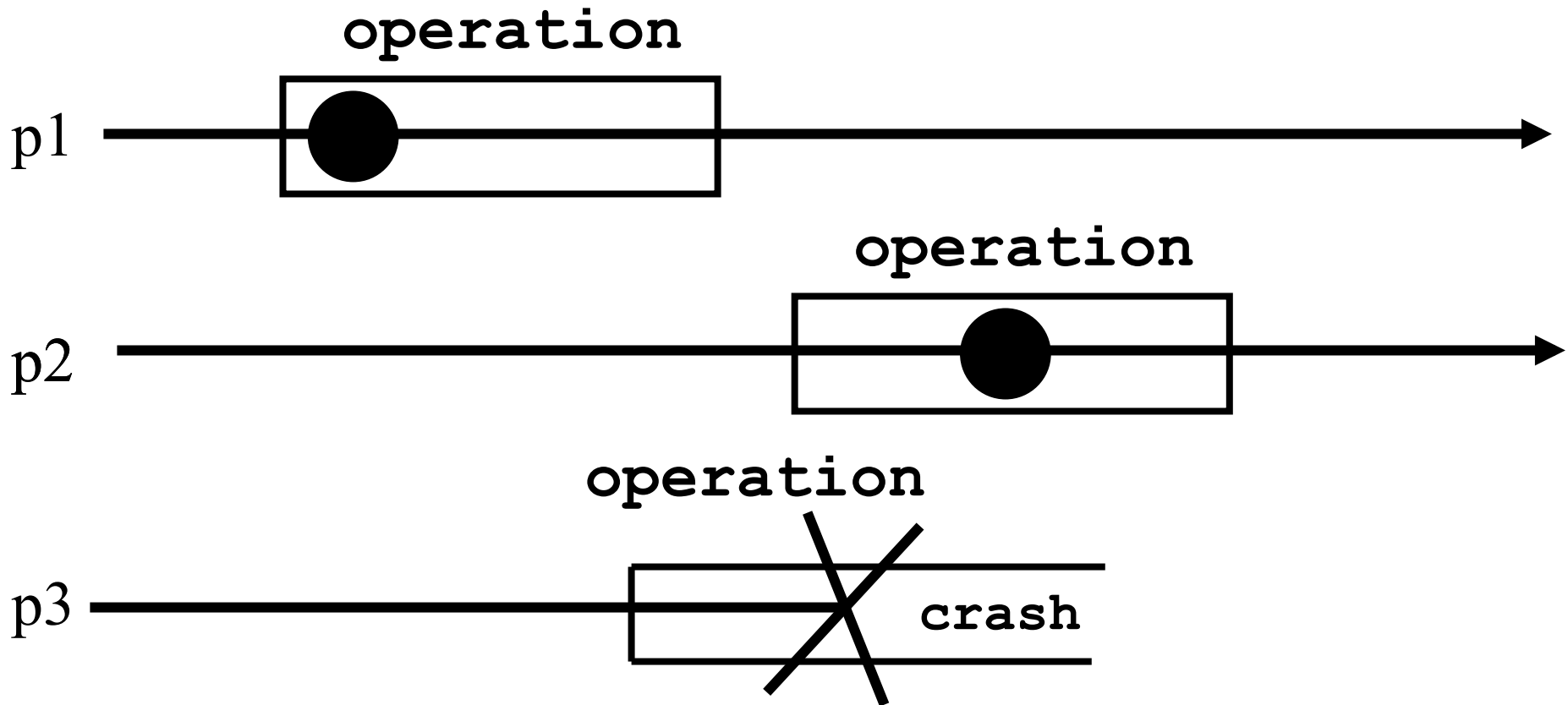
# Atomicity



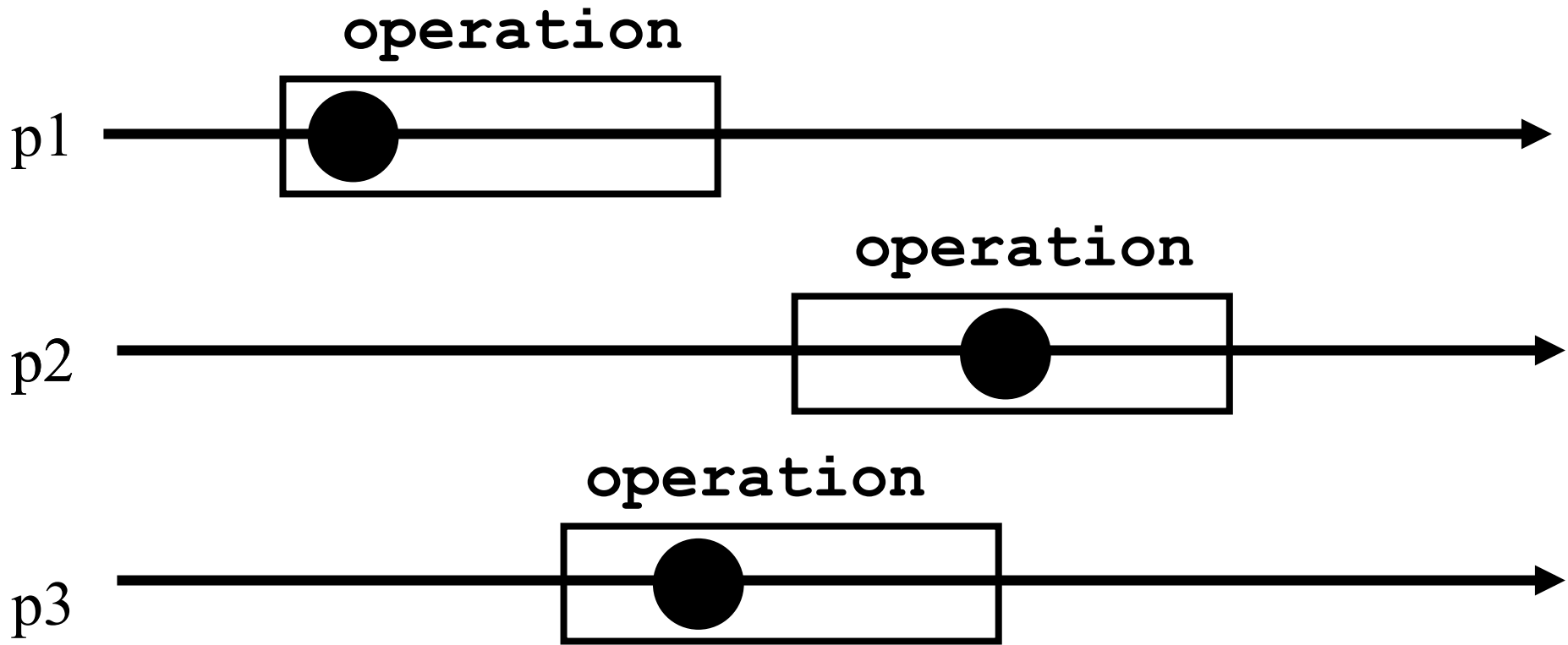
# Atomicity



# Atomicity (the crash case)

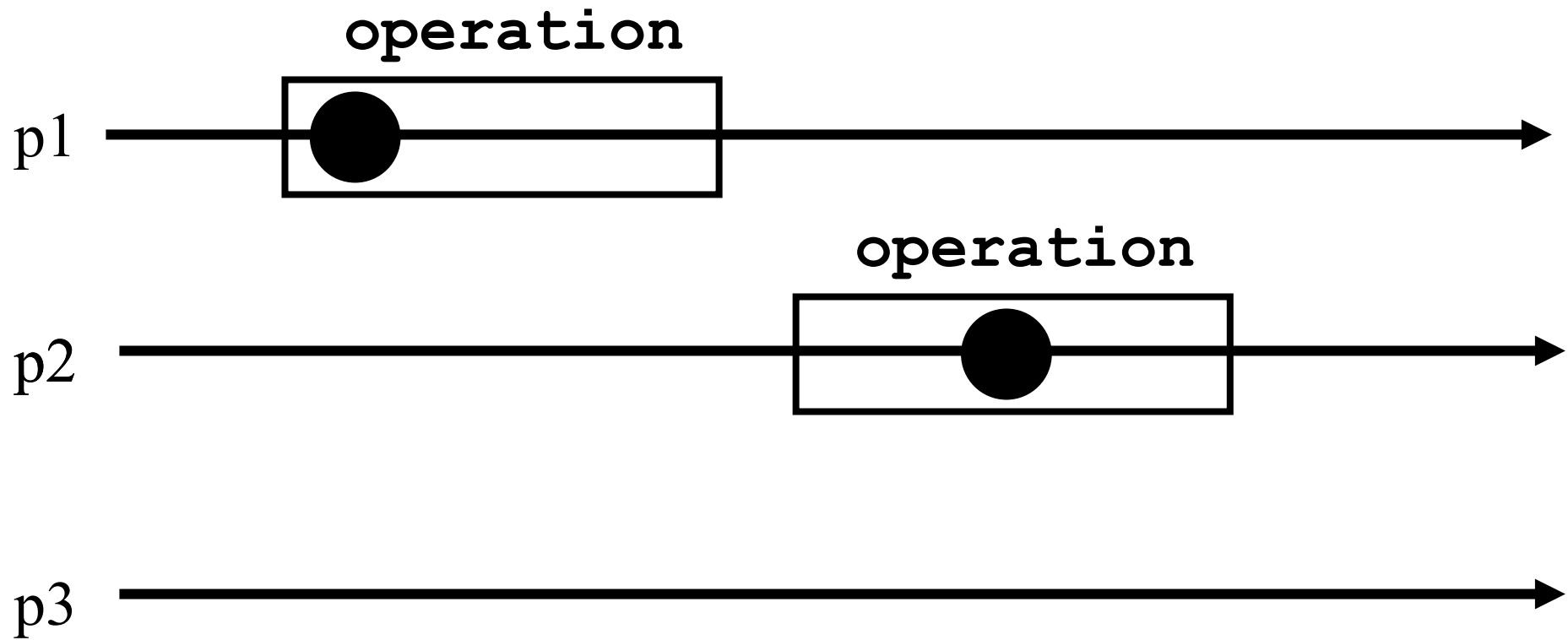


# Atomicity (the crash case)





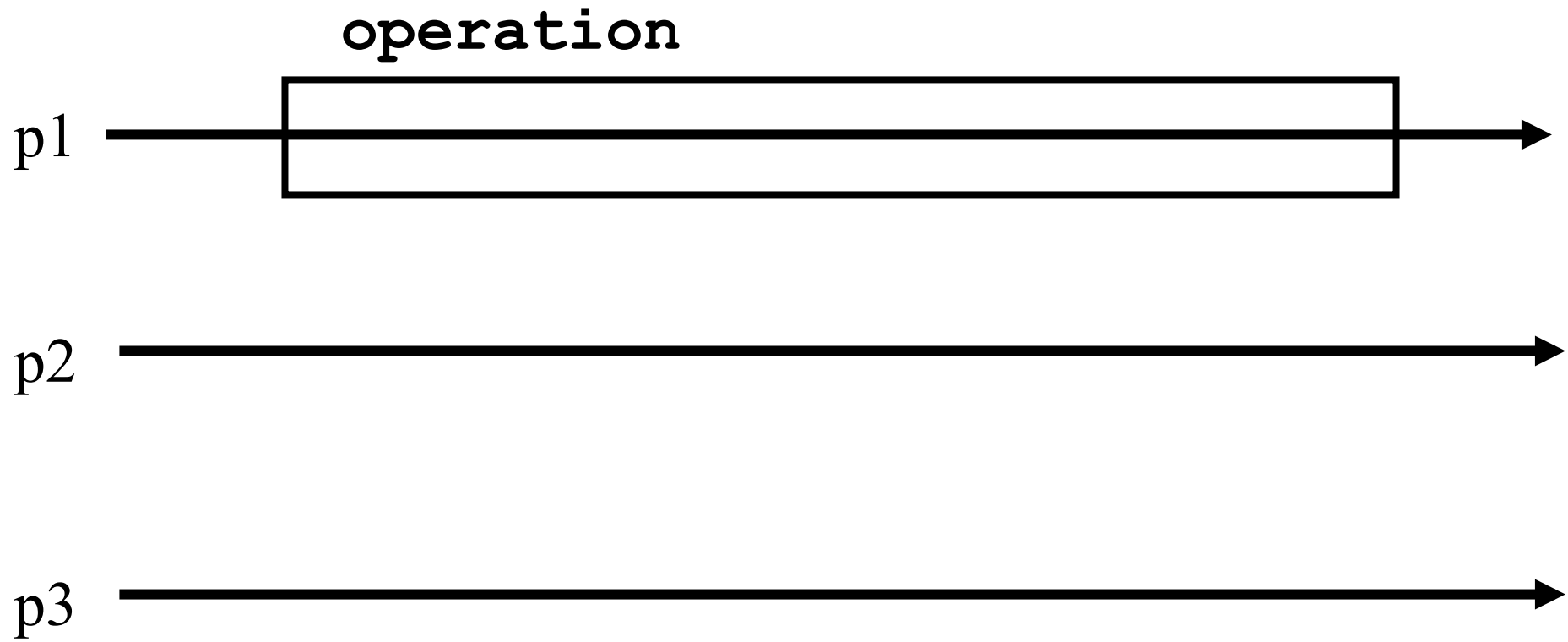
# Atomicity (the crash case)



# Wait-freedom

- Any correct process that invokes an operation eventually gets a reply, no matter what happens to the other processes (crash or very slow)

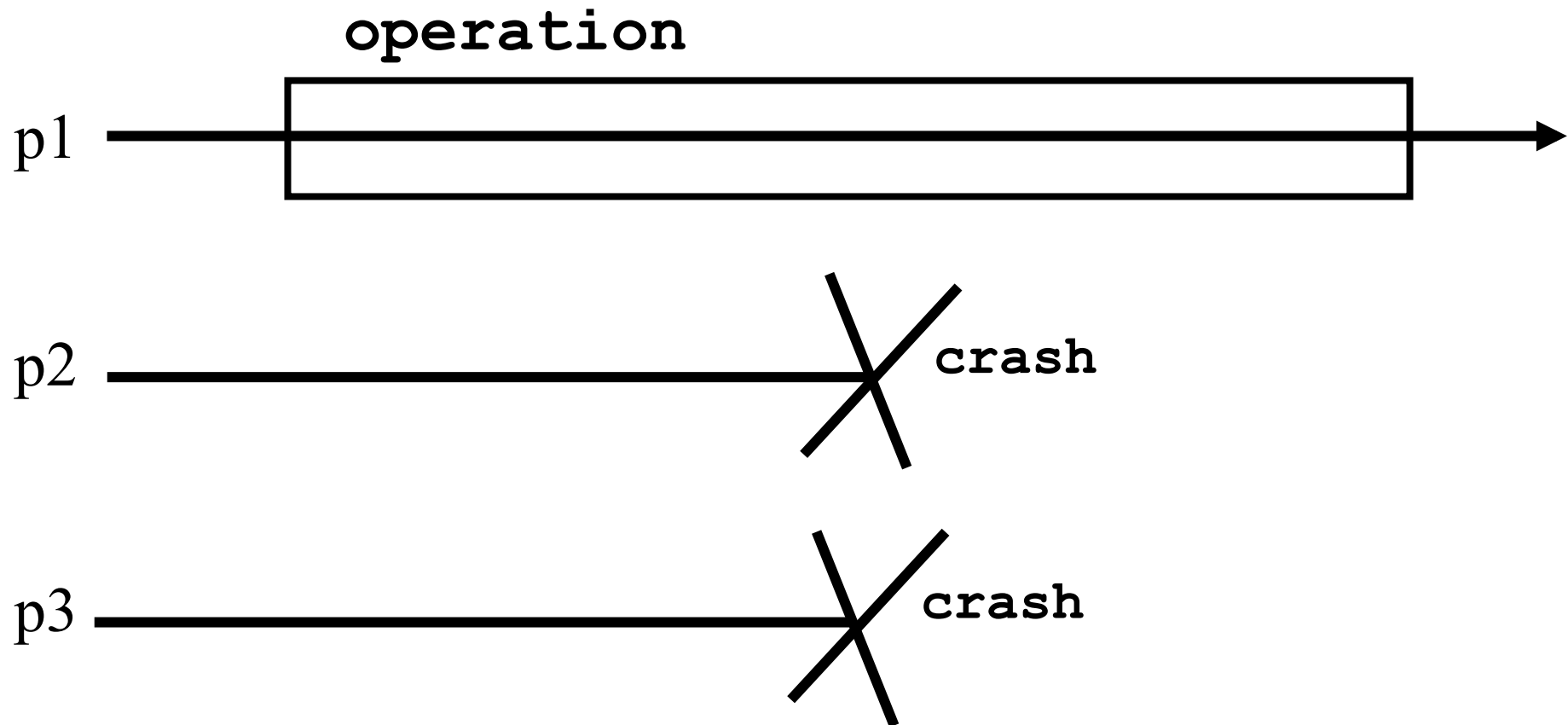
# Wait-freedom



# Wait-freedom

- ☛ Wait-freedom conveys the robustness of the implementation
- ☛ With a wait-free implementation, a process gets replies despite the crash of the  $n-1$  other processes
- ☛ Note that this precludes implementations based on locks (mutual exclusion)

# Wait-freedom



# Roadmap

- *Model*
  - *Processes and objects*
  - *Atomicity and wait-freedom*
- *Examples*
- *Content*

# Motivation

- ☛ Most synchronization primitives (problems) can be precisely expressed as atomic objects (implementations)
- ☛ Studying how to ensure robust synchronization boils down to studying wait-free atomic object implementations

# Example 1

- The reader/writer synchronization problem corresponds to the ***register*** object
- Basically, the processes need to read or write a shared data structure such that the value read by a process at a time  $t$ , is the last value written before  $t$



# ***Register***

- A ***register*** has two operations: ***read()*** and ***write()***
- We assume that a ***register*** contains an integer for presentation simplicity, i.e., the value stored in the ***register*** is an integer, denoted by  $x$  (initially 0)

# *Sequential specification*

- Sequential specification

- read()*

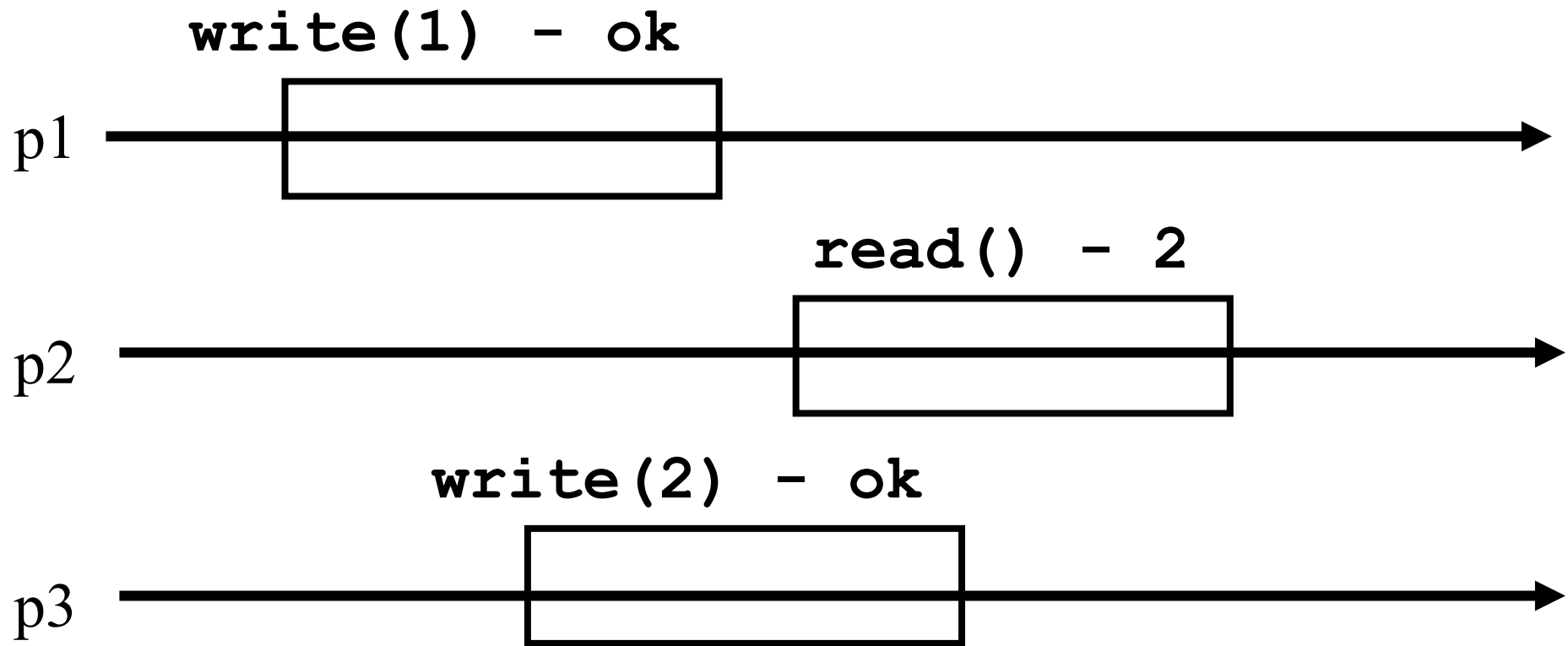
- return(x)

- write(v)*

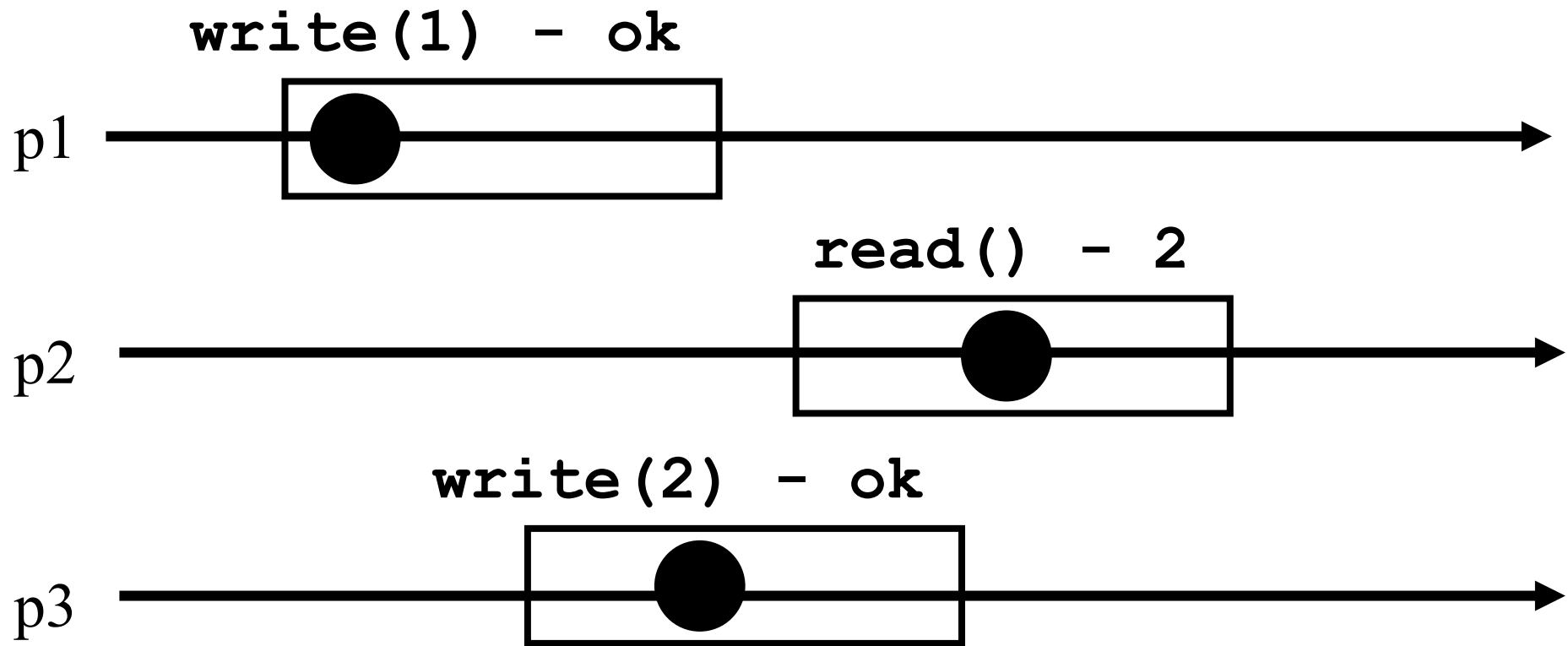
- x ← v;

- return(ok)

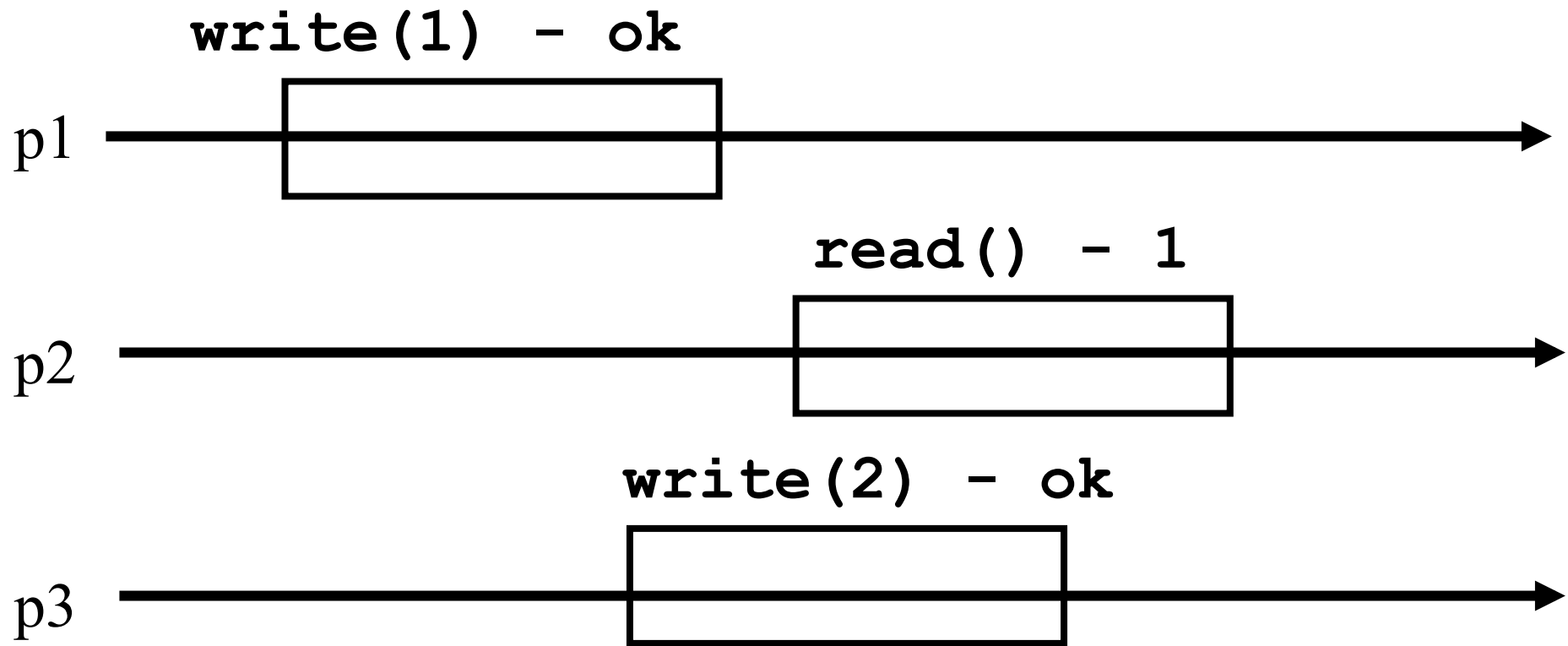
# Atomicity?



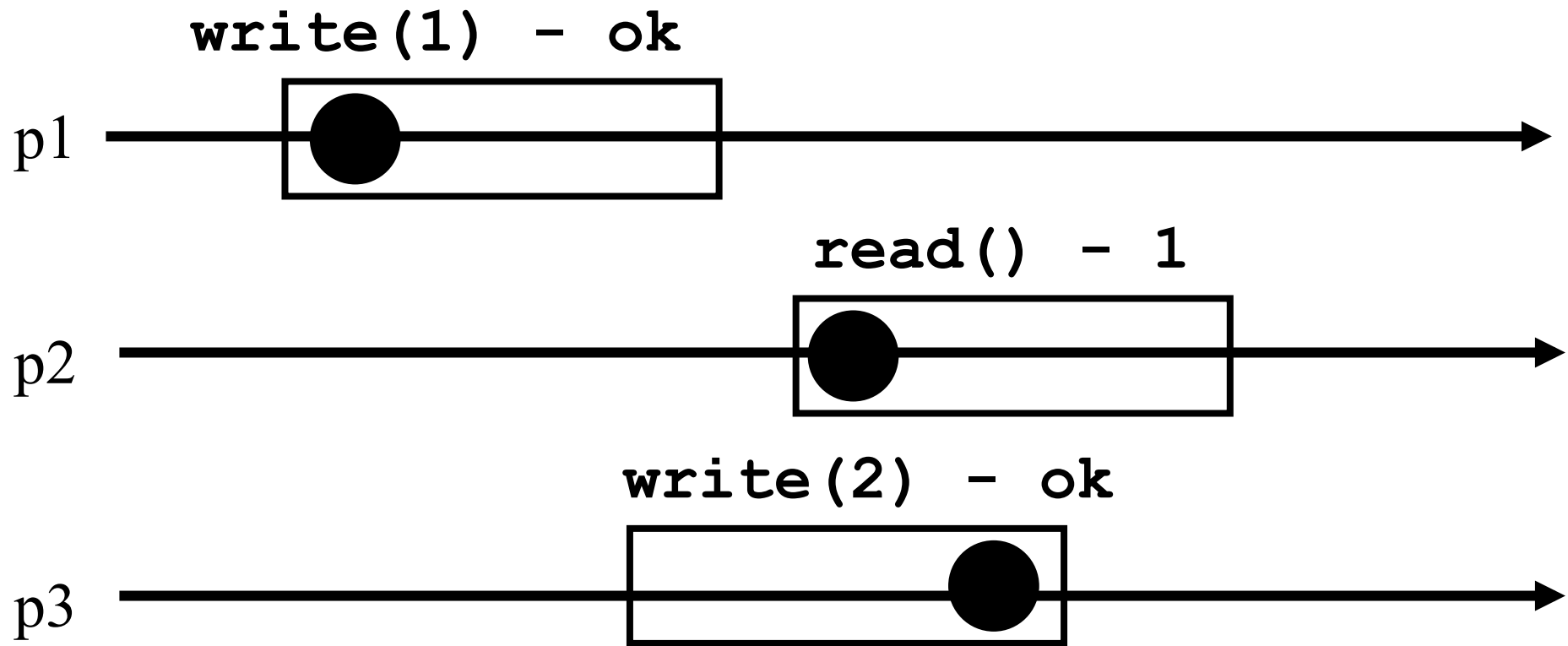
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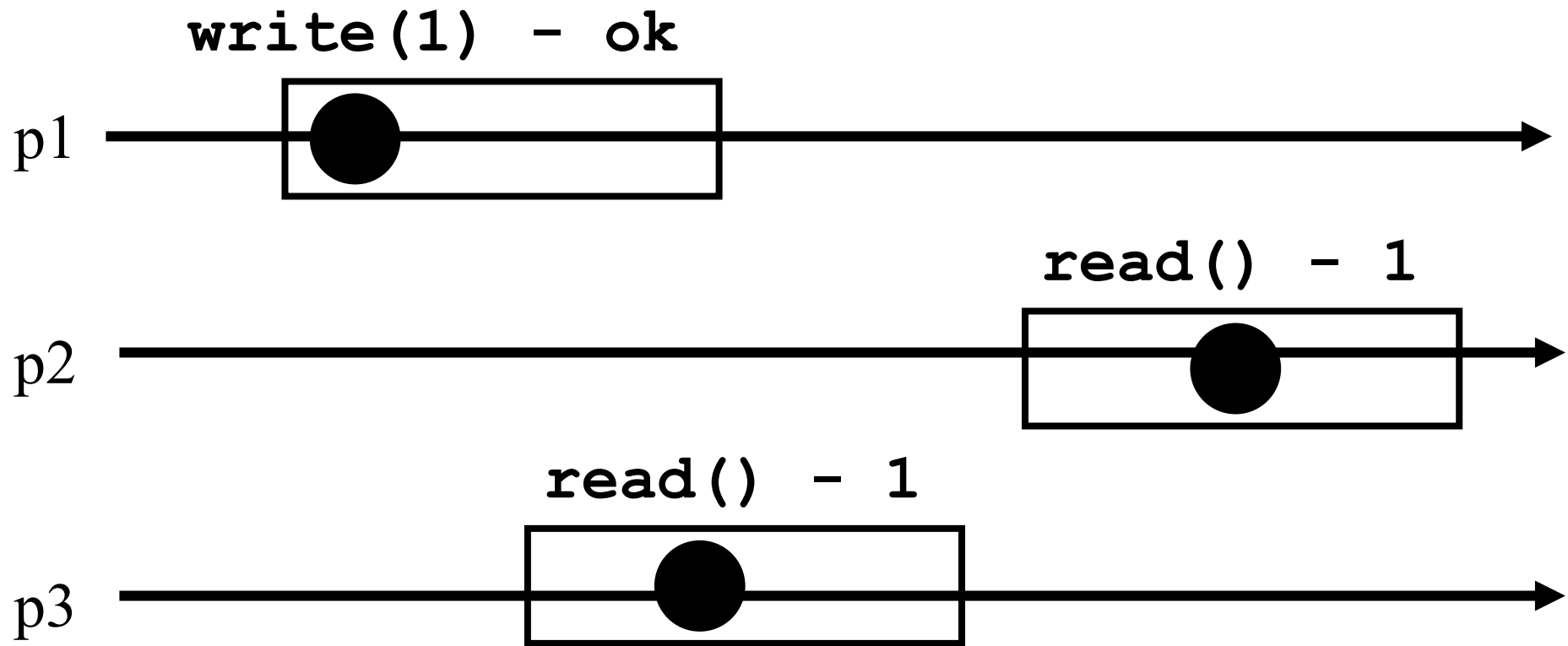
# Atomicity?



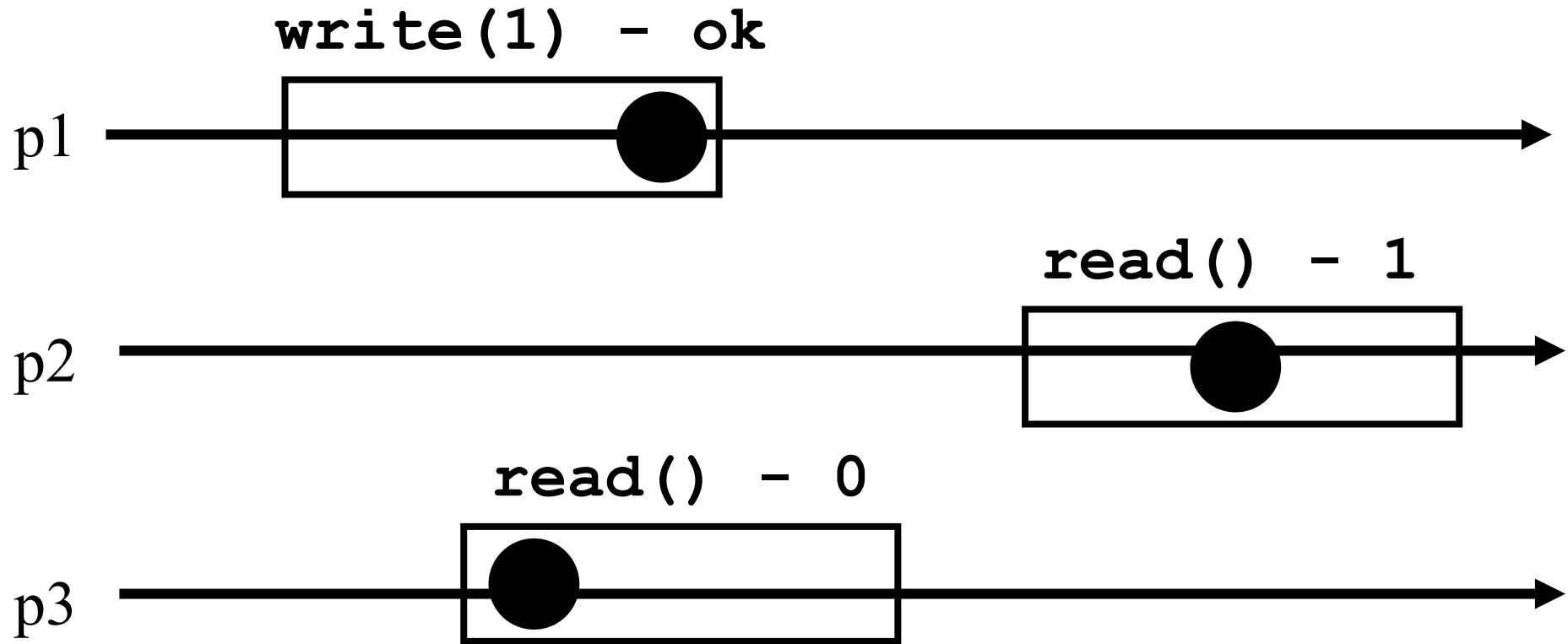
# Atomicity?



# Atomicity?

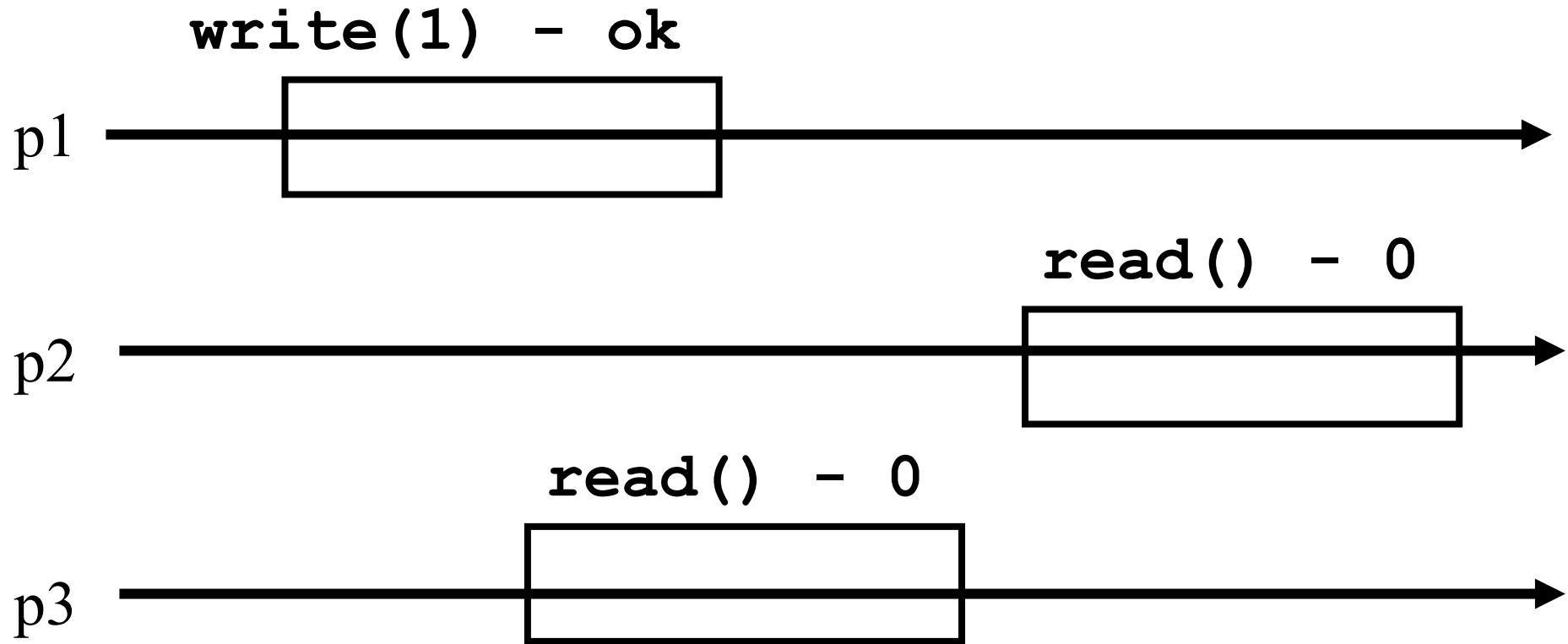


# Atomicity?

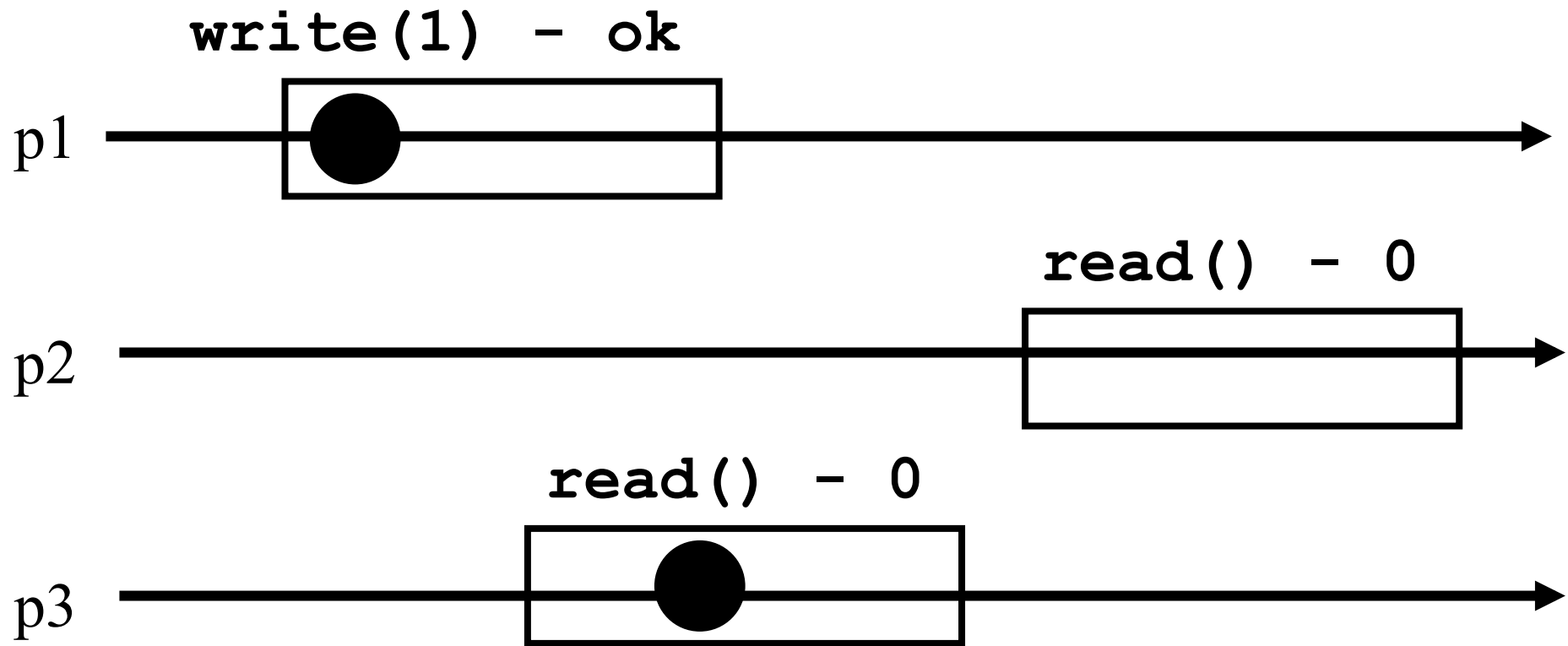




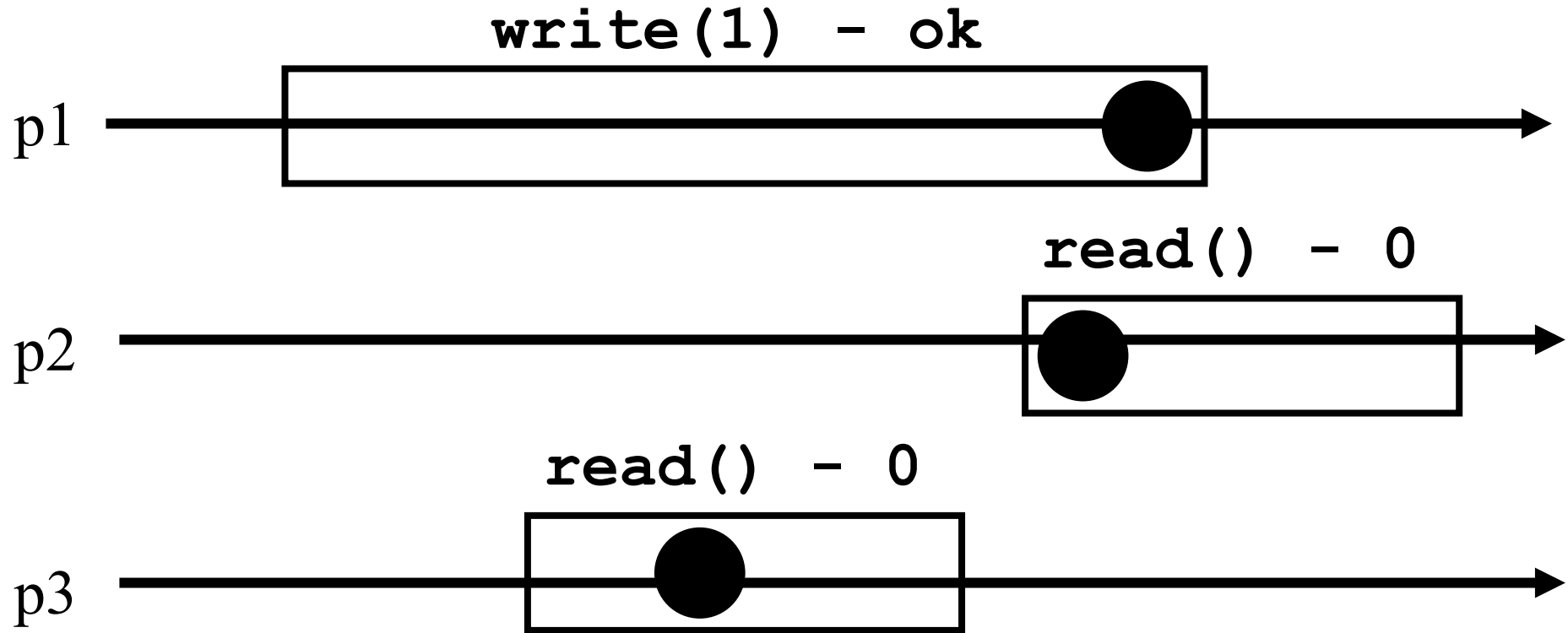
# Atomicity?



# Atomicity?

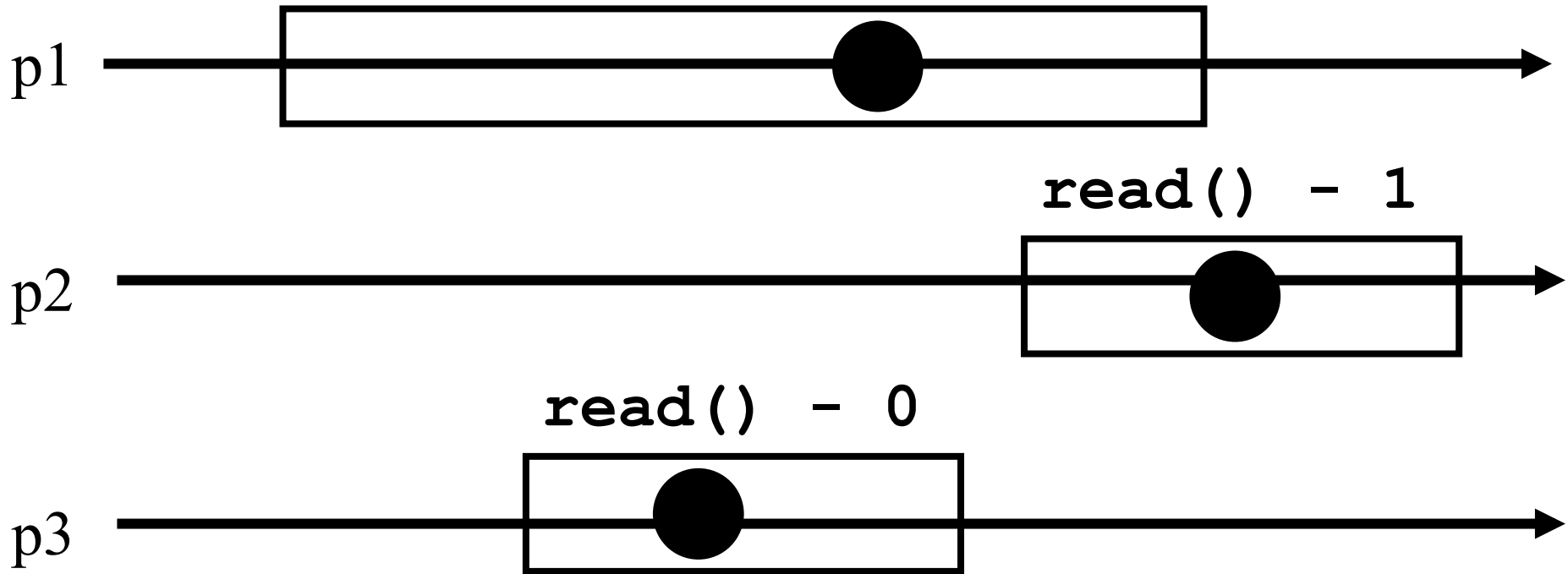


# Atomicity?



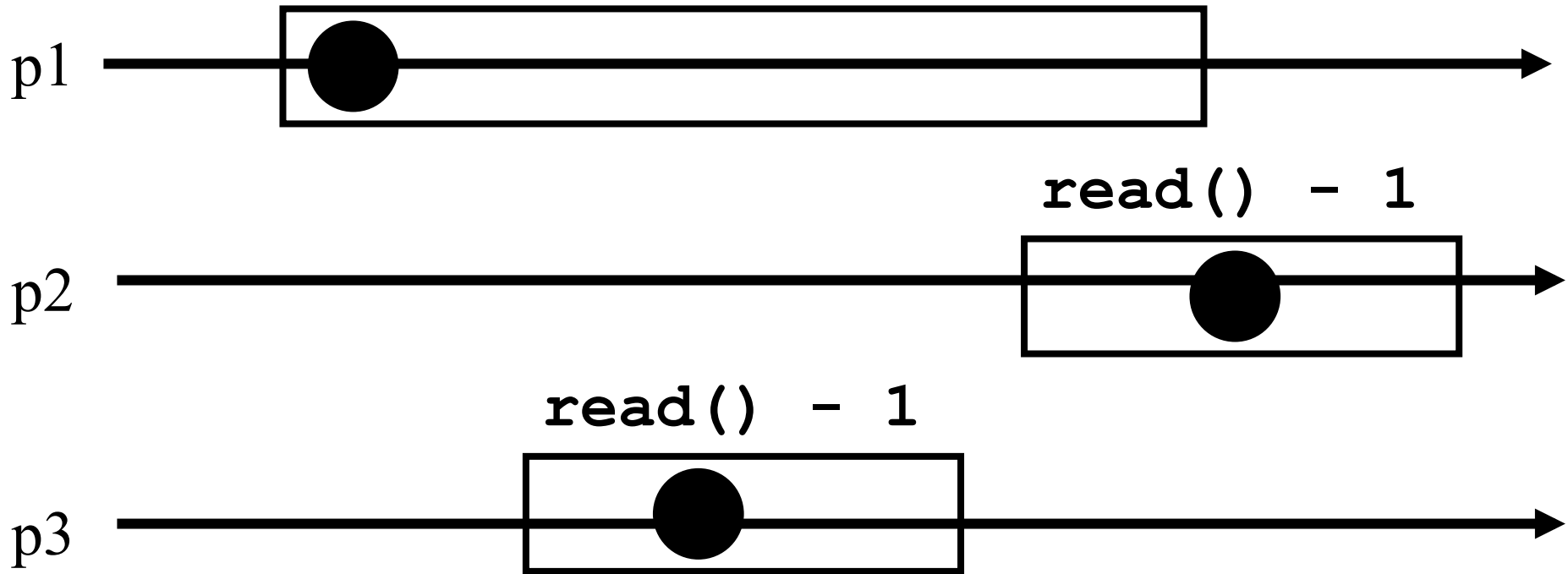
# Atomicity?

`write(1) - ok`



# Atomicity?

`write(1) - ok`



## Example 2

- The producer/consumer synchronization problem corresponds to the **queue** object
- Producer processes create items that need to be used by consumer processes
- An item cannot be consumed by two processes and the first item produced is the first consumed

# Queue

- A **queue** has two operations: ***enqueue()*** and ***dequeue()***
- We assume that a **queue internally** maintains a list  $x$  which exports operation ***appends()*** to put an item at the end of the list and ***remove()*** to remove an element from the head of the list

# ***Sequential specification***

## ***☛ dequeue()***

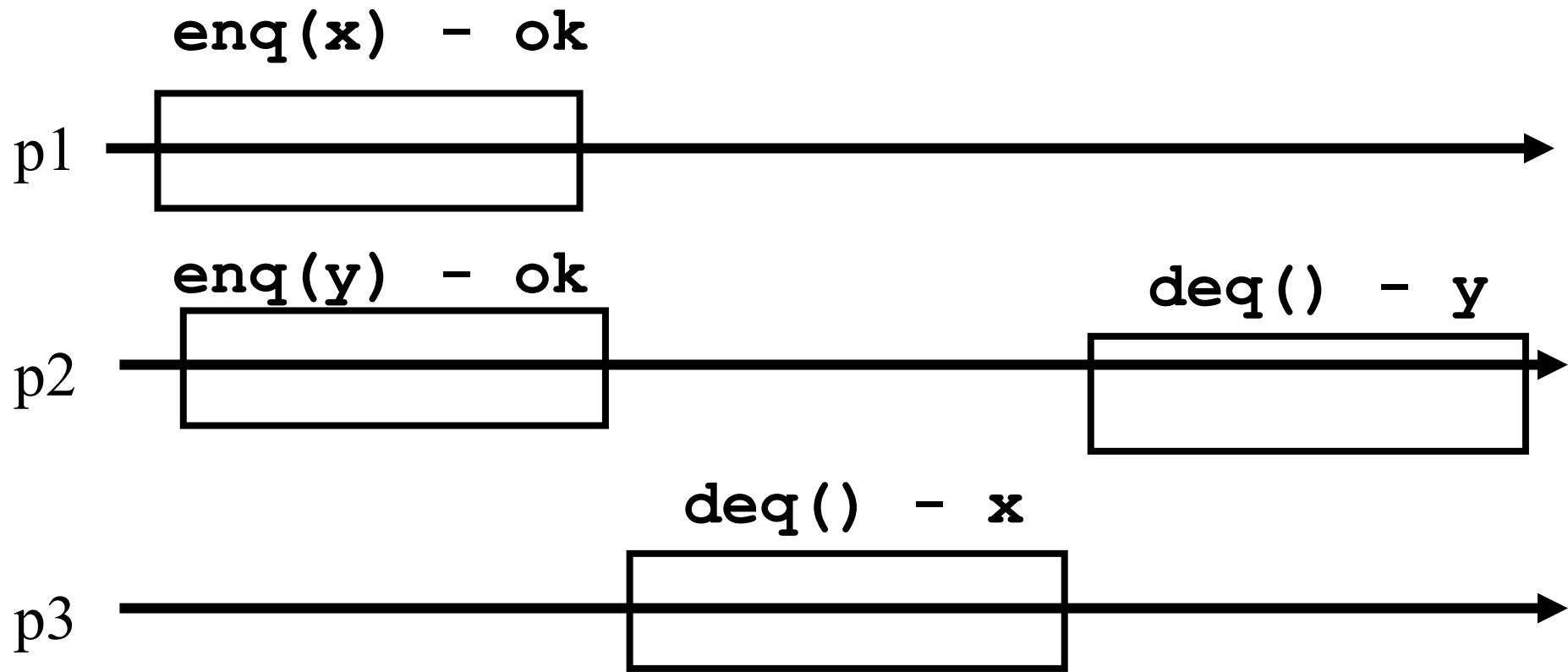
- ☛ if(x=0) then return(nil);***
- ☛ else return(x.remove());***

## ***☛ enqueue(v)***

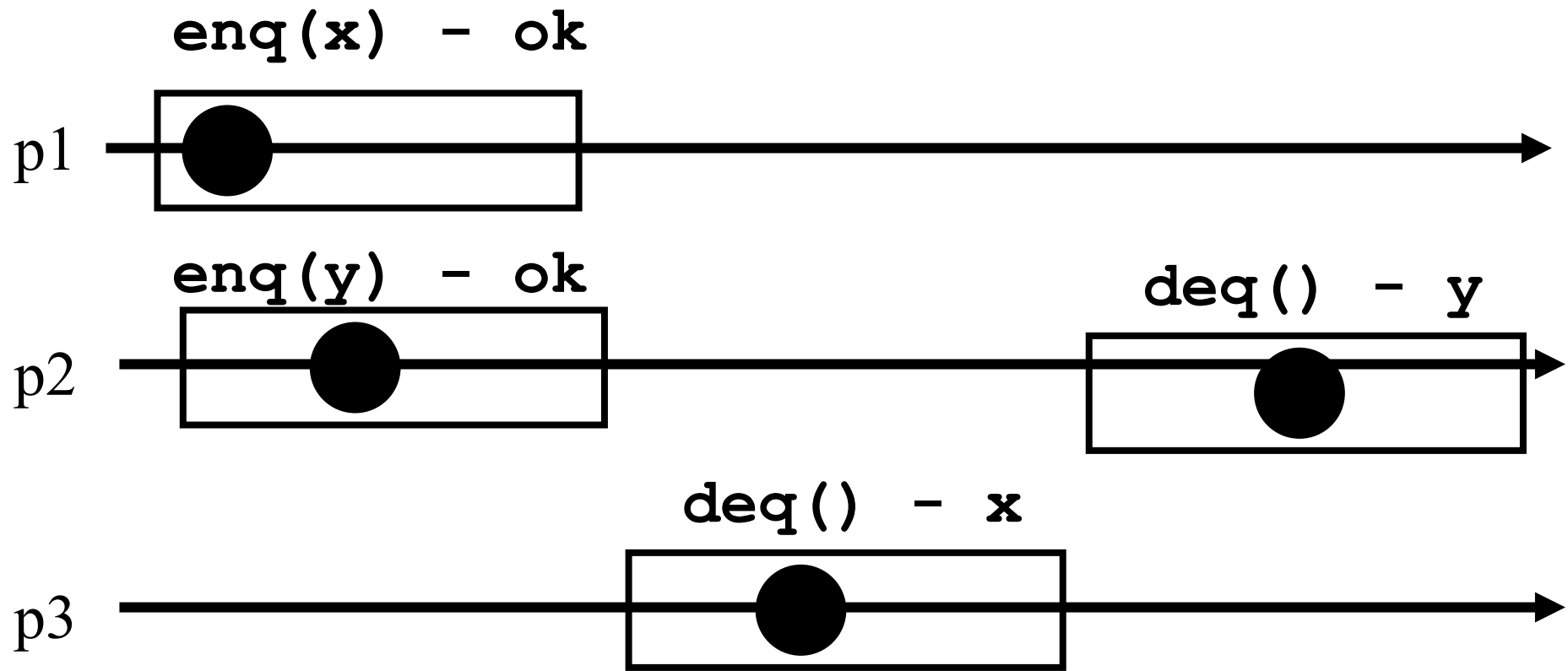
- ☛ x.append(v);***
- ☛ return(ok)***



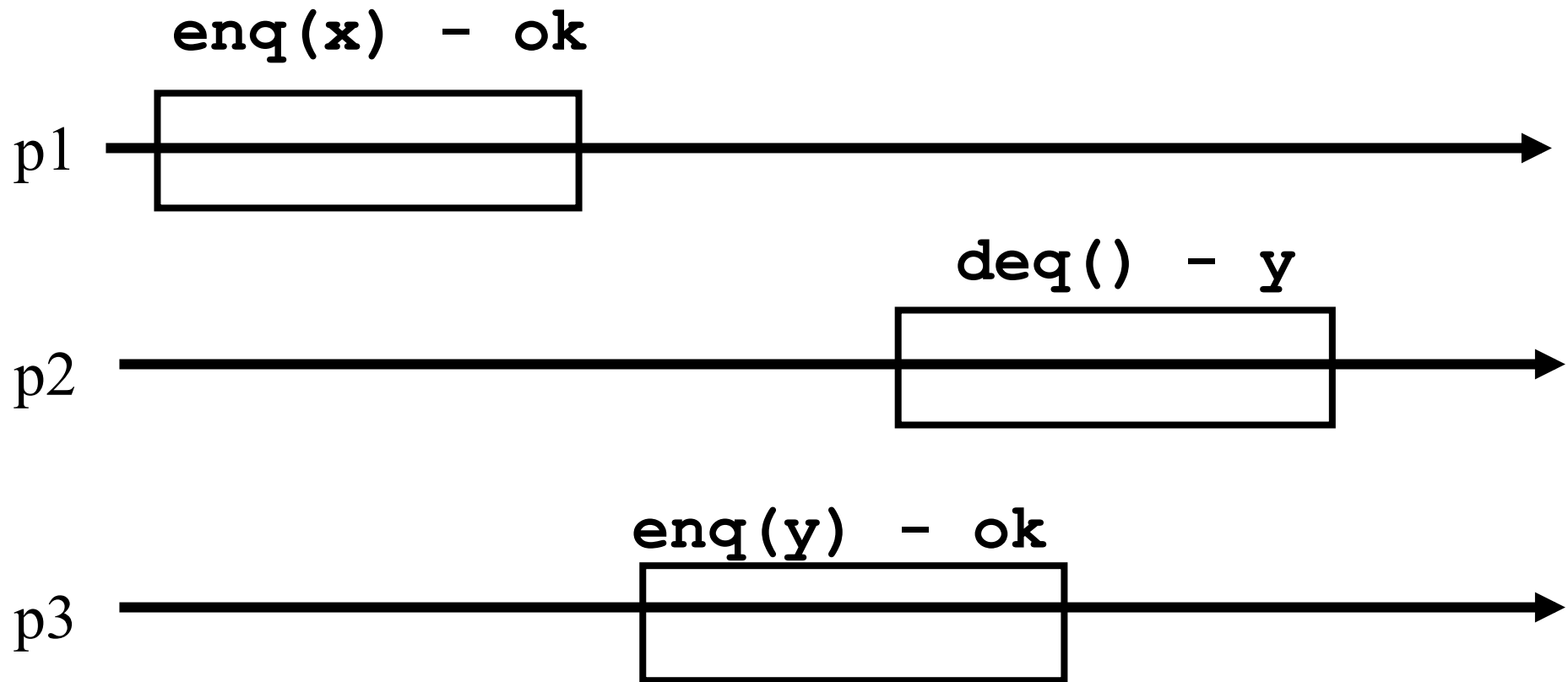
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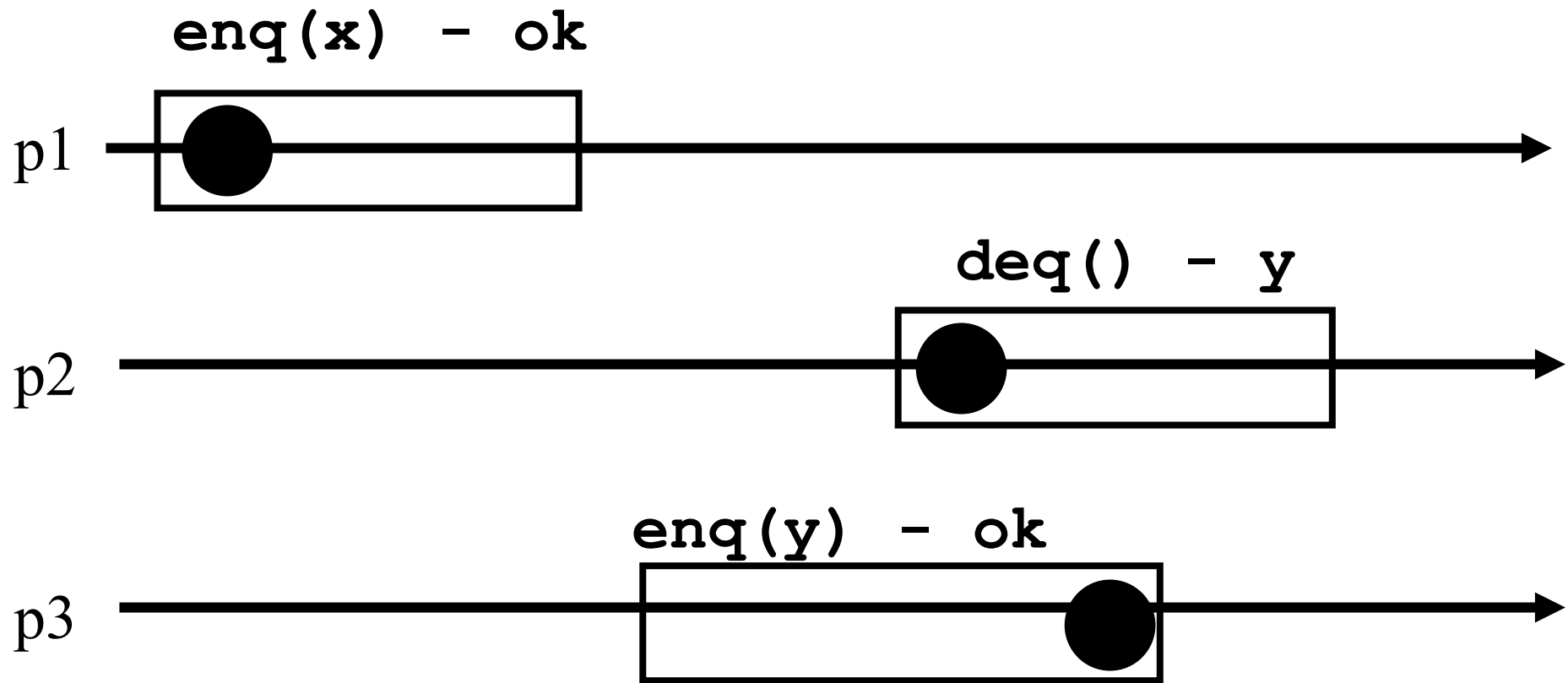
# Atomicity?



# Atomicity?



# Atomicity?



# Roadmap

- *Model*
  - *Processes and objects*
  - *Atomicity and wait-freedom*
- *Examples*
- *Content*

# ***Content***

- ☛ (1) Implementing ***registers***
- ☛ (2) The power & limitation of ***registers***
- ☛ (3) ***Universal*** objects & synchronization number
- ☛ (4) The power of ***time*** & failure detection
- ☛ (5) Tolerating ***failure*** prone objects
- ☛ (6) ***Anonymous*** implementations
- ☛ (7) ***Transaction*** memory

## In short

This course shows how to wait-free  
implement high-level atomic  
objects out of basic objects

Remark. Unless explicitly stated  
otherwise, objects mean atomic objects  
and implementations are wait-free