# Implementing the Consensus Object with Timing Assumptions

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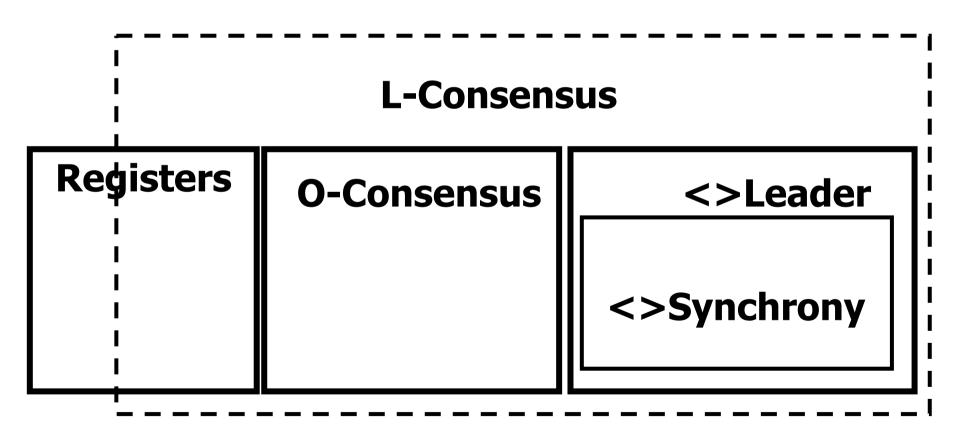


## A modular approach

```
We implement Wait-free Consensus (Consensus)
  through:
  Lock-free Consensus (L-Consensus)
 and
 Registers
We implement L-Consensus through
  Obstruction-free Consensus (O-Consensus)
 and
 <>Leader (encapsulating timing assumptions and
  sometimes denoted by \Omega)
```

## A modular approach

#### **Consensus**



### Consensus

Wait-Free-Termination: If a correct process proposes, then it eventually decides

Agreement: No two processes decide differently

Validity: Any value decided must have been proposed

### L-Consensus

Lock-Free-Termination: If a correct process proposes, then at least one correct process eventually decides

Agreement: No two processes decide differently

Validity: Any value decided must have been proposed

### **O-Consensus**

Obstruction-Free-Termination: If a correct process proposes and eventually executes alone, then the process eventually decides

Agreement: No two processes decide differently

Validity: Any value decided must have been proposed

## Example 1

## Example 2

## O-Consensus algorithm (idea)

- A process that is eventually « left alone » to execute steps, eventually decides
- Several processes might keep trying to concurrently decide until some unknown time: agreement (and validity) should be ensured during this preliminary period

## O-Consensus algorithm (data)

- Each process pi maintains a timestamp ts, initialized to i and incremented by n
- The processes share an array of register pairs **Reg[1,..,n]**; each element of the array contains two registers:
  - Reg[i].T contains a timestamp (init to 0)

## O-Consensus algorithm (functions)

- To simplify the presentation, we assume two functions applied to Reg[1,..,N]
  - r highestTsp() returns the highest timestamp among all elements Reg[1].T, Reg[2].T, .., Reg[N].T
  - \*\* highestTspValue() returns the value with the highest timestamp among all elements Reg[1].V, Reg[2].V, .., Reg[N].V

## O-Consensus algorithm

```
propose(v):
while(true)
  Reg[i].T.write(ts);
  val := Reg[1,..,n].highestTspValue();
  r if val = \bot then val := v;
  Reg[i].V.write(val,ts);
  f if ts = Reg[1,..,n].highestTsp() then
        return(val)
  r ts := ts + n
```

## O-Consensus algorithm

```
propose(v):
while(true)
  (1) Reg[i].T.write(ts);
  (2) val := Reg[1,..,n].highestTspValue();
  r if val = \bot then val := v;
  (3) Reg[i].V.write(val,ts);
   (4) if ts = Reg[1,...,n].highestTsp() then
        return(val)
   r ts := ts + n
```

## O-Consensus algorithm

- (1) pi announces its timestamp
- (2) pi selects the value with the highest timestamp (or its own if there is none)
- (3) pi announces the value with its timestamp
- (4) if pi's timestamp is the highest, then pi decides (i.e., pi knows that any process that executes line 2 will select pi's value)

#### L-Consensus

We implement L-Consensus using <>leader (leader()) and the O-Consensus algorithm

The idea is to use <>leader to make sure that, eventually, one process keeps executing steps alone, until it decides

#### <> Leader

- One operation *leader()* which does not take any input parameter and returns, as an output parameter, a boolean
- A process considers itself leader if the boolean is true
  - ✓ Property: If a correct process invokes leader, then the invocation returns and eventually, some correct process is permanently the only leader

## Example

### L-Consensus

```
propose(v): while(true)
  if leader() then
     Reg[i].T.write(ts);
      val := Reg[1,..,n].highestTspValue();
     r if val = \bot then val := v;
     Reg[i].V.write(val,ts);
     f if ts = Reg[1,...,n].highestTsp()
           then return(val)
      r ts := ts + n
```

## From L-Consensus to Consensus (helping)

 Every process that decides writes its value in a register *Dec* (init to ⊥)

Every process periodically seeks for a value in Dec

#### Consensus

```
propose(v)
while (Dec.read() = \perp)
f if leader() then
   Reg[i].T.write(ts);
   val := Reg[1,..,n].highestTspValue();
   \sigma if val = \bot then val := p;
   r Reg[i].V.write(val,ts);
   \sigma if ts = Reg[1,..,n].highestTsp()
             then Dec.write(val)
   rts := ts + n;
return(Dec.read())
```

#### <> Leader

- One operation *leader()* which does not take any input parameter and returns, as an output parameter, a boolean
- A process considers itself leader if the boolean is true
  - ✓ Property: If a correct process invokes leader, then
    the invocation returns and eventually, some correct
    process is permanently the only leader

### <>Leader: algorithm

- We assume that the system is <>synchronous
  - ✓ There is a time after which there is a lower and an upper bound on the delay for a process to execute a local action, a read or a write in shared memory
  - ✓ The time after which the system becomes synchronous is called the global stabilization time (GST) and is unknown to the processes
- This model captures the practical observation that distributed systems are usually synchronous and sometimes asynchronous

## <>Leader: algorithm (shared variables)

 Every process pi elects (stores in a local variable leader) the process with the lowest identity that pi considers as non-crashed; if pi elects pj, then j < i</li>

 A process pi that considers itself leader keeps incrementing Reg[i]; pi claims that it wants to remain leader

 NB. Eventually, only the leader keeps incrementing the shared register Reg[i]

## <>Leader: algorithm (local variables)

- Every process periodically increments local variables *clock* and *check*, as well as a local variable *delay* whenever its leader changes
- Process pi maintains *lasti[j]* to record the last value of *Reg[j]* pi has read (pi can hence know whether pj has progressed)
- The next leader is the one with the smallest id that makes some progress; if no such process pj such that j<i exists, then pi elects itself (noLeader is true)

## <>Leader: algorithm (variables)

- check, and delay are initialized to 1
- lasti[j] and Reg[j] are initialized to 0
- The next leader is the one with the smallest id that makes some progress; if no such process pj such that j<i exists, then pi elects itself (noLeader is true)

### <>Leader: algorithm

leader(): return(leader)

- check, delay and leader init to 1
- lasti[j] and Reg[j] init to 0;
- Task:

```
while(true) do
```

```
✓ clock := 0;
```

√ If (leader=self) then

```
✓ Reg[i].write(Reg[i].read()+1);
```

```
\checkmark clock := clock + 1;
```

√ if(clock = check) then

✓ elect();

### <>Leader: algorithm (cont'd)

```
elect():
noLeader := true;
for j = 1 to (i-1) do

√ if (Reg[j].read() > last[j]) then

   ✓ last[j] := Reg[j].read();

√ if(leader ≠ pj) then delay:=delay*2;

✓ check := check + delay;

   ✓ leader:= pj;
     noLeader := false; break (for);
if (noLeader) then leader := self;
```

### Consensus = Registers + <> Leader

- <>Leader has one operation *leader()* which does not take any input parameter and returns, as an output parameter, a boolean; a process considers itself leader if the boolean is true
  - ✓ Property: If a correct process invokes leader, then the invocation returns and eventually, some correct process is permanently the only leader
- <>Leader encapsulates the following synchrony assumption: there is a time after which a lower and an upper bound hold on the time it takes for every process to execute a step (eventual synchrony)

### Minimal Assumptions

- Consensus is impossible in an asynchronous system with Registers (FLP83, LA88)
- Consensus is possible in an eventually synchronous system (i.e., <> Leader) with Registers (DLS88, LH95)
- What is the minimal synchrony assumption needed to implement Consensus with Registers?
- Is there any weaker timing abstraction than
   <>Leader that help Registers solve Consensus

### Failure detector

• A *failure detector* is a distributed (wait-free) oracle that provides processes with information about the *crashes* of processes

• Examples: P,  $\Diamond P$ ,  $\Diamond S$ ,  $\Diamond W$ ,  $\Omega$ ,  $\Diamond$  Leader

 NB. A failure detector does only provide information about crashes (CT96)

### Failure detector relations

- We say that a failure detector D implements
   abstraction A (e.g., object O) if there is an algorithm
   that implements A using D
- We say that a failure detector D is weaker than a failure detector D' if D' implements D (D ≤ D')
- If D is weaker than D' and D' is not weaker than D, then D is said to be **strictly weaker** than D' (D < D')
- We say that two failure detectors are equivalent if each is weaker than the other (D ≅ D')

### Failure detector $\Omega$

- Failure detector 
   Ω outputs a process q at every process p (we say that p trusts q) and ensures the following property:
  - Eventually, the same correct process is permanently trusted by every process
  - NB. Note that the process that is trusted might keep changing until some eventual time

### <>Leader $\cong \Omega$

• To implement <>Leader using  $\Omega$ , every process simply returns true if it is leader (the process emulates the output of <>Leader)

To implement <>Leader using Ω, every process writes its name in a shared register L when leader() returns true; all processes periodically read L and elect the process in L (eventually, only one process is elected)

## Failure detector example

- Failure detector 
   Ω outputs a process q at every process p (we say that p trusts q) and ensures the following property:
  - *\phi* unique leader: eventually, the same correct process is permanently trusted by every process
  - NB. Note that the process that is trusted might keep changing until some eventual time

### Questions

- (1) Show that  $\Omega$  is the weakest failure detector to implement consensus with Registers (i.e., give an algorithm that implements  $\Omega$  with any failure detector that implements Consensus with Registers)
- (2) What is the weakest failure detector to implement Consensus with objects of consensus number k and Registers?
- (3) What is the weakest failure to implement an object with consensus number k using Registers?