

# Registers

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# ***Register***

- A ***register*** has two operations: ***read()*** and ***write()***
- Sequential specification
- • ***read()***
  - return(x)
- • ***write(v)***
  - $x \leftarrow v$ ; return(ok)

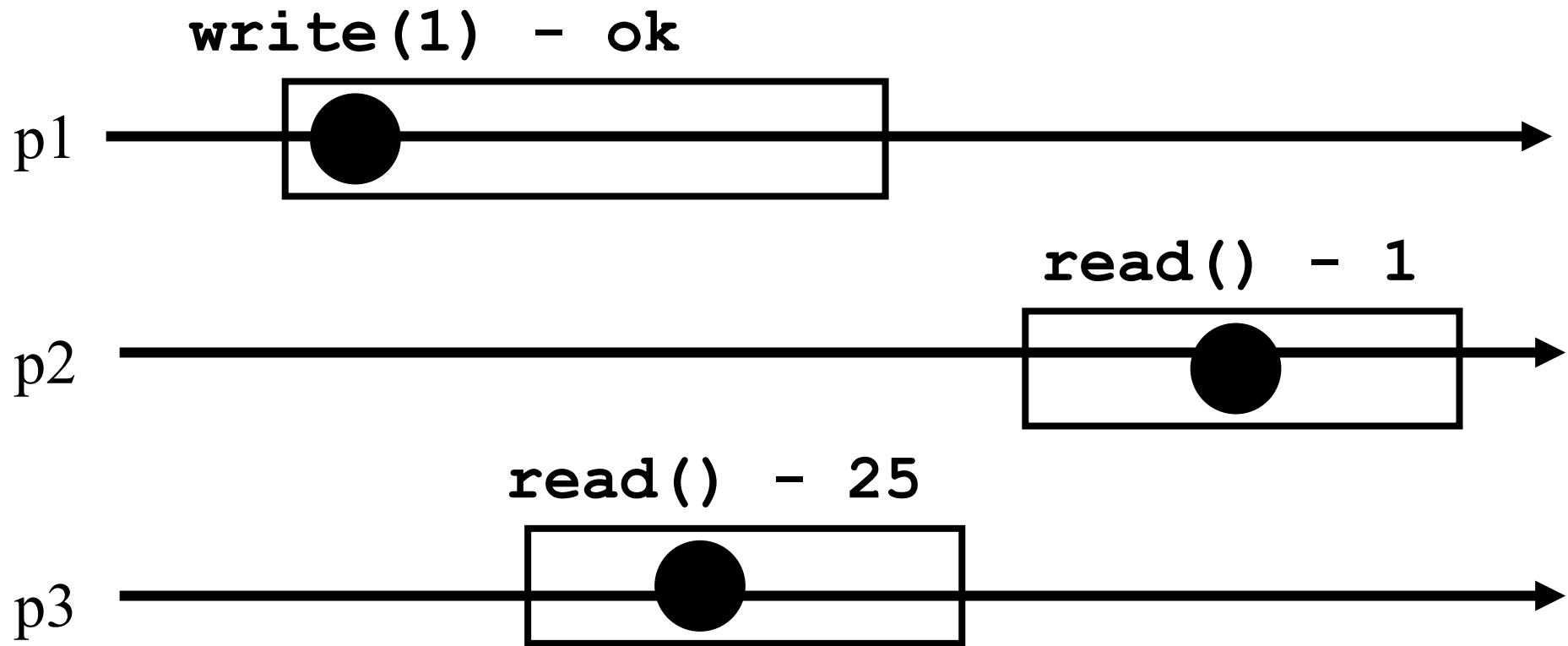
# Simplifications

- We assume that **registers** contain only integers
- Unless explicitly stated otherwise, **registers** are initially supposed to contain 0

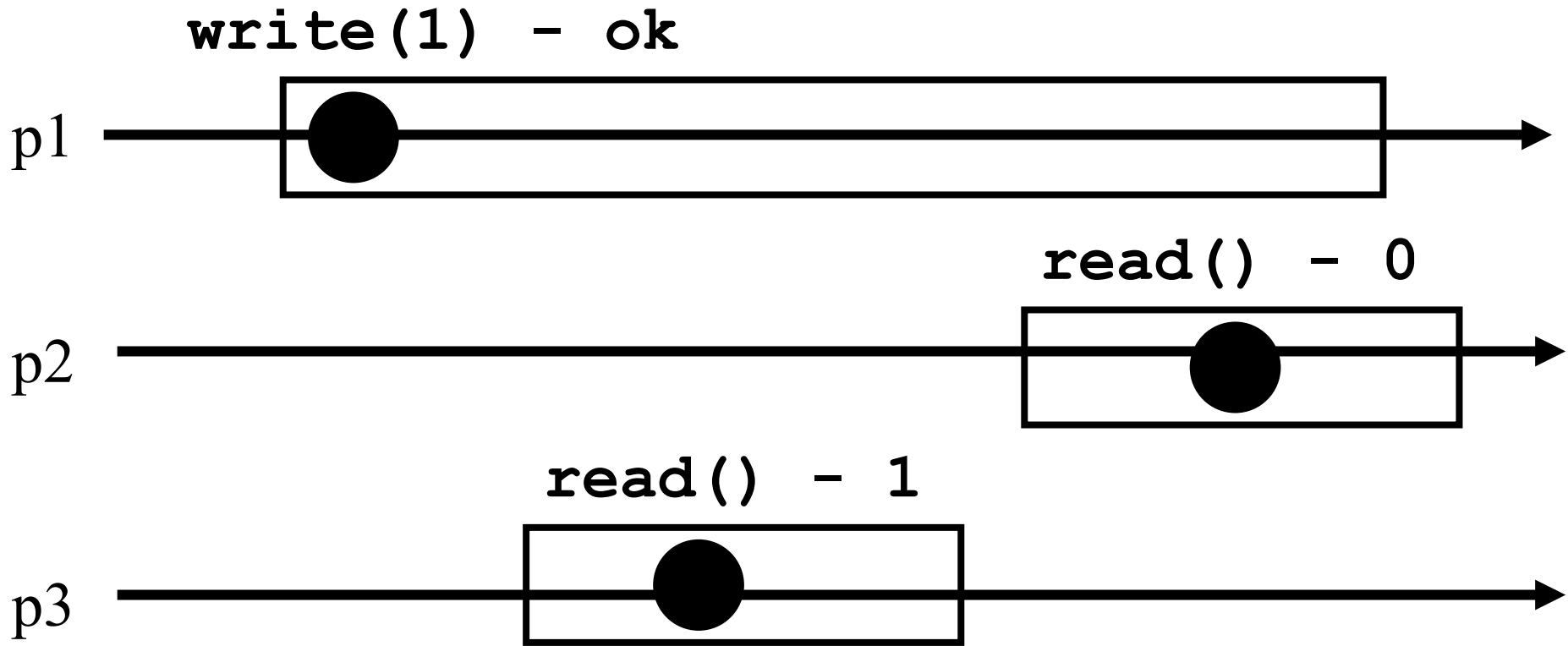
# Space of registers

- Dimension 1: binary (boolean) – multivalued
- Dimension 2:
  - SRSW (single reader, single writer)
  - MRSW (multiple reader, single writer)
  - MRMW (multiple reader, multiple writer)
- Dimension 3: safe – regular – atomic

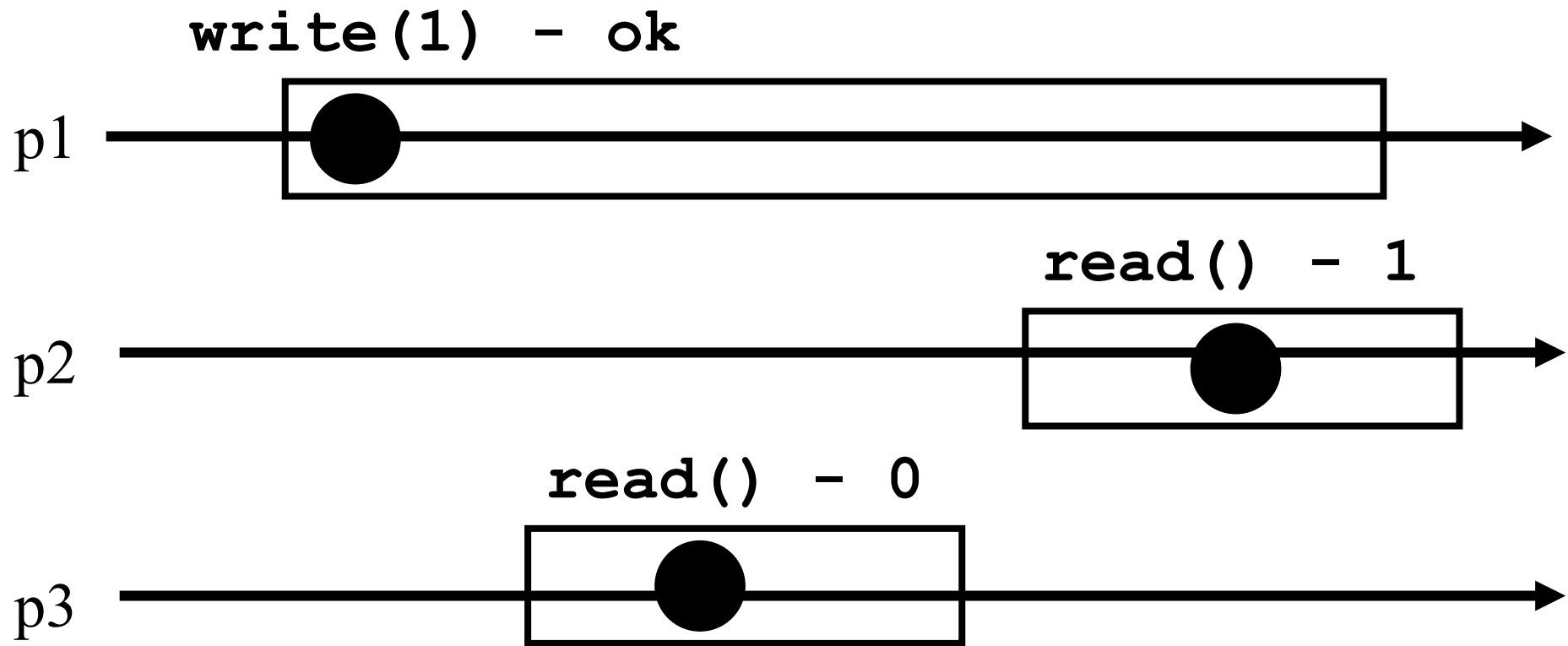
# Safe execution



# Regular execution



# Atomic execution



# 2 decades of hard work

- Theorem: A multivalued MRMW atomic ***register*** can be implemented with binary SRSW safe ***register***



# Algorithms

- The process executing the code is implicitly assumed to be  $p_i$
- We assume a system of  $N$  processes
- NB. We distinguish base and high-level registers

# Conventions

- The operations to be implemented are denoted ***Read()*** and ***Write()***
- Those of the base registers are denoted ***read()*** and ***write()***
- We omit the ***return(ok)*** instruction at the end of ***Write()*** implementations

# (1) From (binary) SRSW safe to (binary) MRSW safe

- We use an array of SRSW *registers*

Reg[1,..,N]

- **Read()**

- return (Reg[i].read());

- **Write(v)**

- for j = 1 to N

- Reg[j].write(v);

# From (binary) SRSW safe to (binary) MRSW safe

- The transformation works also for multi-valued registers and regular ones
- It does not however work for atomic registers

## (2) From binary MRSW safe to binary MRSW regular

- We use one MRSW safe register

- **Read()**

- `return(Reg.read());`

- **Write(v)**

- if `old  $\neq$  v` then

- `Reg.write(v);`

- `old := v;`

# From binary MRSW safe to binary MRSW regular

- The transformation works for single reader ***registers***
- It does not work for multi-valued ***registers***
- It does not work for atomic ***registers***

# (3) From *binary* to *M-Valued* MRSW regular

- We use an array of MRSW registers  
Reg[0,1,...,M] init to [1,0,...,0]
- **Read()**
  - for j = 0 to M
    - if Reg[j].read() = 1 then return(j)
- **Write(v)**
  - Reg[v].write(1);
  - for j=v-1 downto 0
    - Reg[j].write(0);

# From *binary* to *M-Valued* MRSW regular

- The transformation would not work if the Write() would first write 0s and then 1
- The transformation works for regular but NOT for atomic registers



## (4) From *SRSW regular* to *SRSW atomic*

- We use one SRSW register `Reg` and two local variables `t` and `x`
- **Read()**
  - `(t',x') = Reg.read();`
  - `if t' > t then t:=t'; x:=x';`
  - `return(x)`
- **Write(v)**
  - `t := t+1;`
  - `Reg.write(v,t);`

# From SRSW regular to SRSW atomic

- The transformation would not work for multiple readers
- The transformation would not work without timestamps  
(variable  $t$  represents logical time)

## (5) From SRSW atomic to MRSW atomic

- We use  $N \times N$  SRSW atomic registers  $RReg[(1,1),(1,2),\dots,(k,j),\dots,(N,N)]$  to communicate among the readers
  - In  $RReg[(k,j)]$  the reader is  $p_k$  and the writer is  $p_j$
- We also use  $n$  SRSW atomic **registers**  $WReg[1,\dots,N]$  to store new values
  - the writer in all these is  $p_1$
  - the reader in  $WReg[k]$  is  $p_k$

# (5) From SRSW atomic to MRSW atomic (cont'd)

## • **Write(v)**

- `t1 := t1+1;`
- for `j = 1 to N`
  - `WReg.write(v,t1);`

# (5) From SRSW atomic to MRSW atomic (cont'd)

## Read()

- for  $j = 1$  to  $N$  do
  - $(t[j], x[j]) = \text{RReg}[i, j].\text{read}();$
- $(t[0], x[0]) = \text{WReg}[i].\text{read}();$
- $(t, x) := \text{highest}(t[..], x[..]);$
- for  $j = 1$  to  $N$  do
  - $\text{RReg}[j, i].\text{write}(t, x);$
- return( $x$ )

**Value with highest timestamp**

# From SRSW atomic to MRSW atomic

- The transformation would not work for multiple writers
- The transformation would not work if the readers do not communicate (i.e., if a reader does not write)

## (6) From *MRSW* atomic to *MRMW* atomic

- We use  $N$  *MRSW* atomic registers  $\text{Reg}[1,\dots,N]$ ; the writer of  $\text{Reg}[j]$  is  $p_j$
- **Write( $v$ )**
  - for  $j = 1$  to  $N$  do
    - $(t[j],x[j]) = \text{Reg}[j].\text{read}()$ ;
  - $(t,x) := \text{highest}(t[..],x[..])$ ;
  - $t := t+1$ ;
  - $\text{Reg}[i].\text{write}(t,v)$ ;

# (6) From MRSW atomic to MRMW atomic (cont'd)

## • **Read()**

- for  $j = 1$  to  $N$  do
  - $(t[j], x[j]) = \text{Reg}[j].\text{read}();$
- $(t, x) := \text{highest}(t[..], x[..]);$
- return( $x$ )