Registers

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Register

- A register has two operations: read() and write()
- Sequential specification
- read()
 - return(x)
 - write(v)
 - r x <- v; return(ok)</pre>

Simplifications

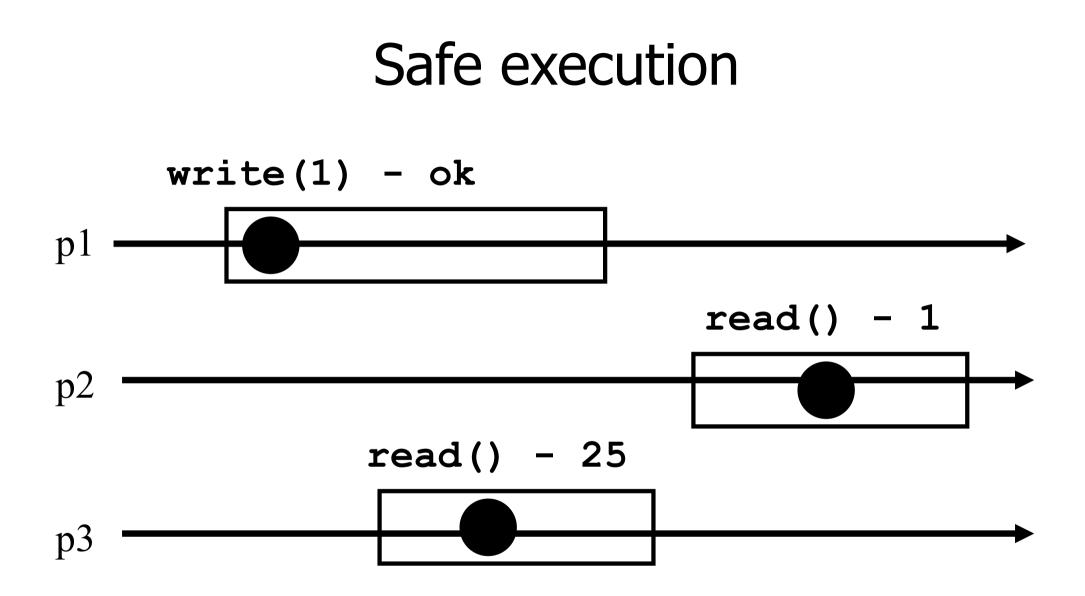
- We assume that *registers* contain only integers
- Unless explicitly stated otherwise, registers are initially supposed to contain 0

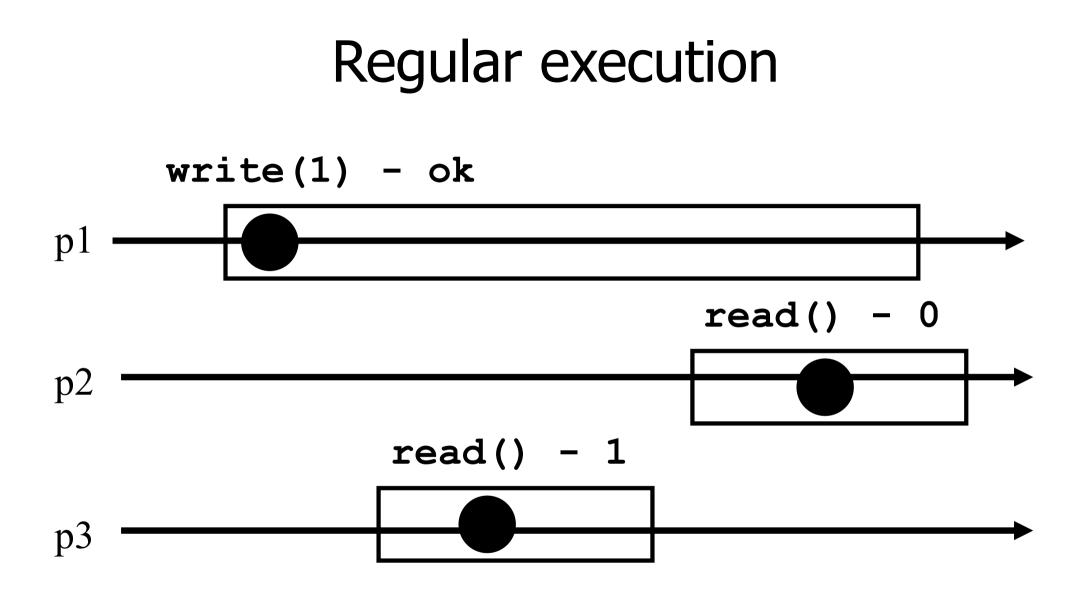
Space of registers

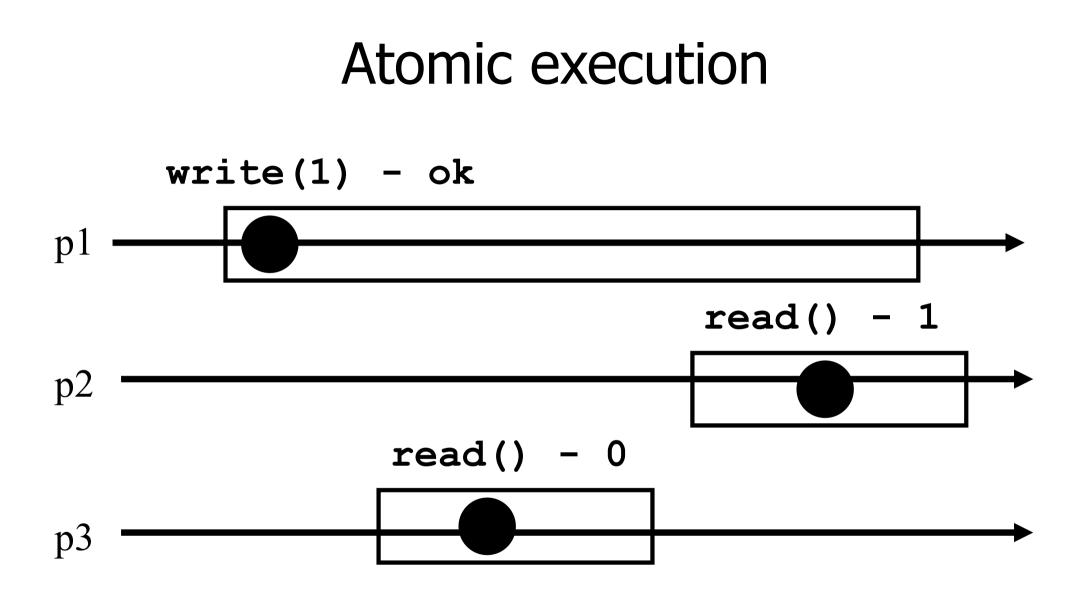
Dimension 1: binary (boolean) – multivalued

Dimension 2:

- SRSW (single reader, single writer)
- MRSW (multiple reader, single writer)
- MRMW (multiple reader, multiple writer)
- ✓ Dimension 3: safe regular atomic







2 decades of hard work

Theorem: A multivalued MRMW atomic register can be implemented with binary SRSW safe register

Algorithms

- The process executing the code is implicitly assumed to be pi
- We assume a system of N processes
- NB. We distinguish base and high-level registers

Conventions

- The operations to be implemented are denoted *Read()* and *Write()*
- Those of the base registers are denoted read() and write()
- We omit the *return(ok)* instruction at the end of *Write()* implementations

(1) From (binary) SRSW safe to (binary) MRSW safe

- We use an array of SRSW registers
 Reg[1,..,N]
- Read()
 - return (Reg[i].read());
- Write(v)
 - r for j = 1 to N
 - Reg[j].write(v);

From (binary) SRSW safe to (binary) MRSW safe

The transformation works also for multivalued registers and regular ones

It does not however work for atomic registers

(2) From binary MRSW safe to binary MRSW regular

- We use one MRSW safe register
- Read()
 - return(Reg.read());

- Write(v)
 - ✓ if old \neq v then
 - Reg.write(v);
 - old := v;

From binary MRSW safe to binary MRSW regular

The transformation works for single reader registers

It does not work for multi-valued registers

It does not work for atomic registers

(3) From *binary* to *M-Valued* MRSW regular

- We use an array of MRSW registers Reg[0,1,...,M] init to [1,0,...,0]
- Read()
 - \checkmark for j = 0 to M
 - r if Reg[j].read() = 1 then return(j)
- Write(v)
 - Reg[v].write(1);
 - for j=v-1 downto 0
 - Reg[j].write(0);

From *binary* to *M-Valued* MRSW regular

- The transformation would not work if the Write() would first write 0s and then 1
- The transformation works for regular but NOT for atomic registers

(4) From SRSW *regular* to SRSW *atomic*

We use one SRSW register Reg and two local variables t and x

Read()

- (t',x') = Reg.read();
- if t' > t then t:=t'; x:=x';

return(x)

- Write(v)
 - r t := t+1;

Reg.write(v,t);

From SRSW regular to SRSW atomic

 The transformation would not work for multiple readers

- The transformation would not work without timestamps
- (variable t represents logical time, i.e., timestamp)

(5) From SRSW atomic to MRSW atomic

- We use N*N SRSW atomic registers RReg[(1,1),(1,2),..,(k,j),..(N,N)] to communicate among the readers
 - In RReg[(k,j)] the reader is pk and the writer is pj
- We also use n SRSW atomic *registers* WReg[1,..,N] to store new values
 - the writer in all these is p1
 - the reader in WReg[k] is pk

(5) From SRSW atomic to MRSW atomic (cont'd)

Write(v)

- r t1 := t1+1;
- \checkmark for j = 1 to N
 - WReg.write(v,t1);

(5) From SRSW atomic to MRSW atomic (cont'd)

Read()

- \checkmark for j = 1 to N do
 - (t[j],x[j]) = RReg[i,j].read();
- (t[0],x[0]) = WReg[i].read();
- (t,x) := highest(t[..],x[..]);
- \checkmark for j = 1 to N do
 - // RReg[j,i].write(t,x);
- return(x)

Value with highest timestamp

From SRSW atomic to MRSW atomic

The transformation would not work for multiple writers

The transformation would not work if the readers do not communicate (i.e., if a reader does not write)

(6) From *MRSW* atomic to *MRMW* atomic

We use N MRSW atomic registers Reg[1,..,N]; the writer of Reg[j] is pj

Write(v) for j = 1 to N do (t[j],x[j]) = Reg[j].read(); (t,x) := highest(t[..],x[..]); t := t+1; Reg[i].write(t,v); }

(6) From MRSW atomic to MRMW atomic (cont'd)

Read() for j = 1 to N do (t[j],x[j]) = Reg[j].read(); (t,x) := highest(t[..],x[..]); return(x)