Concurrent Algorithms

October 27, 2020

Exercise 5

Problem 1.

Let *A* be an *obstruction-free* algorithm implementing some shared object *O* with operations op_1, \ldots, op_k . The goal of the exercise is to transform algorithm *A* into a *wait-free* algorithm *B* that also implements shared object *O* (i.e., the operations op_1, \ldots, op_k). We will do it by implementing an abstraction called a *contention manager*, using an *eventually perfect* failure detector $\diamond \mathcal{P}$ and atomic registers.



A contention manager implements two operations: try_i and $resign_i$ (invoked by process p_i). These operations do not take any arguments and always return ok. A contention manager resolves contention, and thus guarantees wait-freedom, by delaying some processes that have invoked try_i . In other words, when a process p_i invokes try_i , a contention manager can decide when to return from the operation—it can delay the response of try_i for an arbitrarily long time.

We assume that algorithm A uses the interface of the contention manager, i.e., that it invokes try_i and $resign_i$. More precisely, every time an operation op_m , implemented by A, is executed by a process p_i , the following conditions are satisfied:

- 1. *try_i* is called always before the first step of the implementation of *op_m* is executed (i.e., just after *op_m* is invoked), and possibly many times while *op_m* is being executed,
- *resign_i* is called *only* immediately after the last step of the implementation of *op_m* is executed (i.e., just before the result of *op_m* is returned),
- 3. If process *p_i* is correct but never returns from operation *op_m* (i.e., the implementation of the operation is executed infinitely long), then *p_i* calls *try_i* infinitely many times.

Moreover, every time process p_i invokes try_i or $resign_i$, p_i waits until $try_i/resign_i$ returns before executing any further steps of algorithm A.

An eventually perfect failure detector $\diamond P$ maintains, at every process p_i , a set *suspected*_i of suspected processes. $\diamond P$ guarantees that eventually, after some unknown time, the following conditions are satisfied:

- 1. Every correct process permanently suspects every crashed process,
- 2. No correct process is ever suspected by any correct process.

This means that $suspected_i$ can be arbitrary and different at every process for any *finite* period of time. However, eventually, at every correct process p_i , set $suspected_i$ will be permanently equal to the set of processes that have crashed.

Your task is to implement a contention manager *C* (i.e., the operations try_i and $resign_i$, for every process p_i) that converts obstruction-free algorithm *A* into wait-free algorithm *B*, and that uses only atomic registers and failure detector $\diamond P$.