Concurrent programming: From theory to practice

Concurrent Algorithms 2020

Vasileios Trigonakis
Principal Member of Technical Staff
Oracle Labs, Zurich

Theoretical (design)

Practical (design)

Practical (implementation)

Theoretical (design)

Practical (design)

Practical (implementation)

- Impossibilities
- Upper/Lower bounds
- Techniques
- System models
- Correctness proofs



Design (pseudo-code)

Theoretical (design)

Practical (design)

Practical (implementation)

- Impossibilities
- Upper/Lower bounds
- Techniques
- System models
- Correctness proofs

- System models
 - shared memory
 - message passing
- Finite memory
- Practicality issues
 - re-usable objects
- Performance



Design (pseudo-code)



Design (pseudo-code, prototype)

Theoretical (design)

- Impossibilities
- Upper/Lower bounds
- Techniques
- System models
- Correctness proofs



Design (pseudo-code)

Practical (design)

- System models
 - shared memory
 - message passing
- Finite memory
- Practicality issues
 - re-usable objects
- Performance



Design (pseudo-code, prototype)

Practical (implementation)

- Hardware
- Which atomic ops
- Memory consistency
- Cache coherence
- Locality
- Performance
- Scalability



Implementation (code)

Outline

- CPU caches
- Cache coherence
- Placement of data
- Graph processing: Concurrent data structures

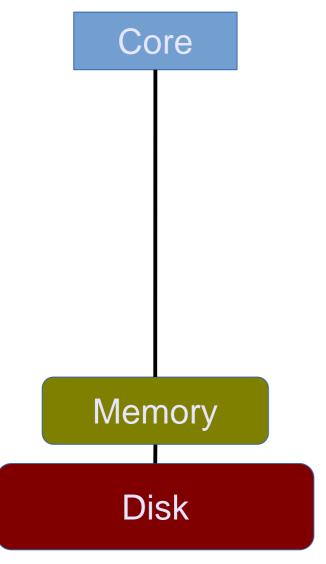
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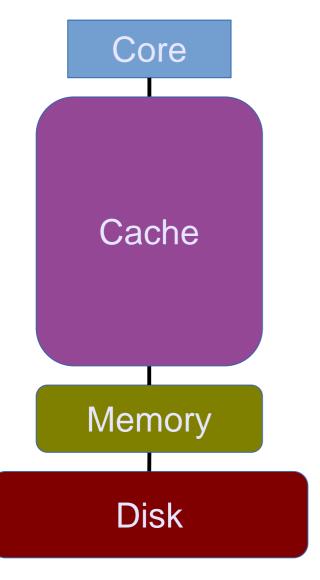
Core

- Core freq: 2GHz = 0.5 ns / instr
- Core → Disk = ~ms

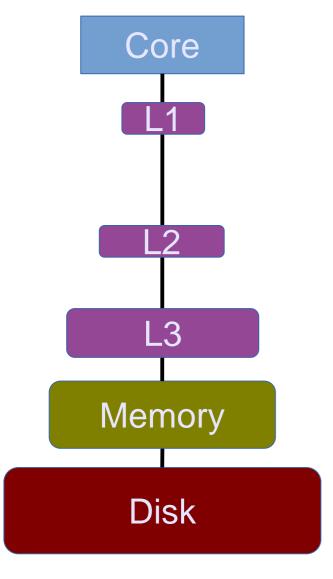
Disk



- Core freq: 2GHz = 0.5 ns / instr
- Core → Disk = ~ms
- Core → Memory = ~100ns



- Core freq: 2GHz = 0.5 ns / instr
- Core → Disk = ~ms
- Core → Memory = ~100ns
- Cache
 - Large = slow
 - Medium = medium
 - Small = fast



- Core freq: 2GHz = 0.5 ns / instr
- Core → Disk = ~ms
- Core → Memory = ~100ns
- Cache

- Core →
$$L3 = \sim 20$$
ns

- Core
$$\rightarrow$$
 L2 = ~7ns

- Core
$$\rightarrow$$
 L1 = ~1ns

Typical server configurations

Intel Xeon

14 cores @ 2.4GHz

L1: 32KB

L2: 256KB

L3: 40MB

Memory: 256GB



AMD Opteron

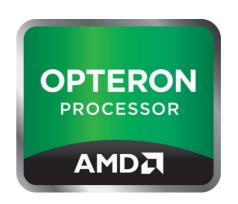
18 cores @ 2.4GHz

L1: 64KB

L2: 512KB

- L3: 20MB

Memory: 256GB



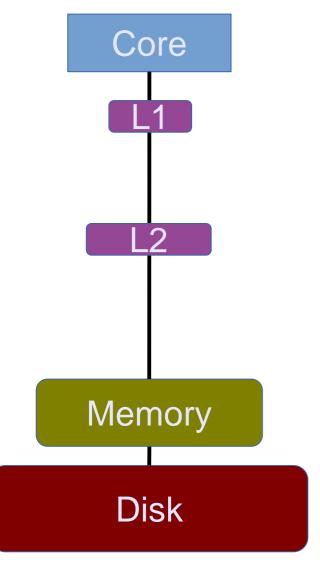
Experiment

Throughput of accessing some memory, depending on the memory size

Outline

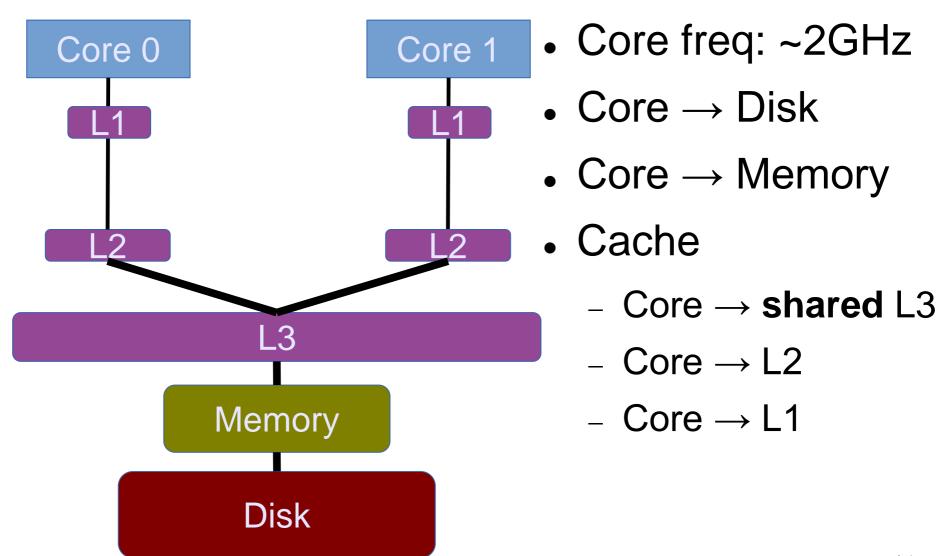
- CPU caches
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Until ~2004: single-cores

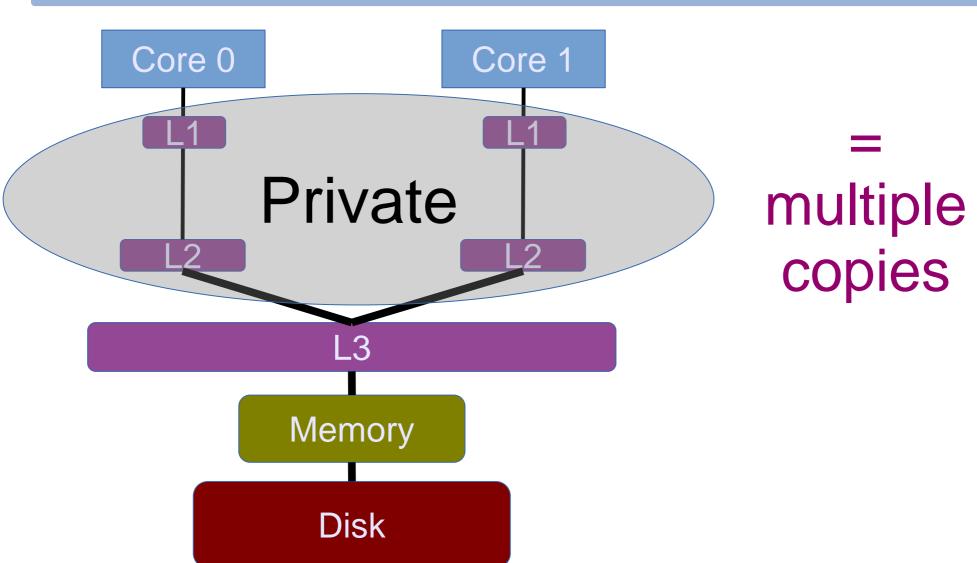


- Core freq: 3+GHz
- Core → Disk
- Core → Memory
- Cache
 - Core → L3
 - Core \rightarrow L2
 - Core \rightarrow L1

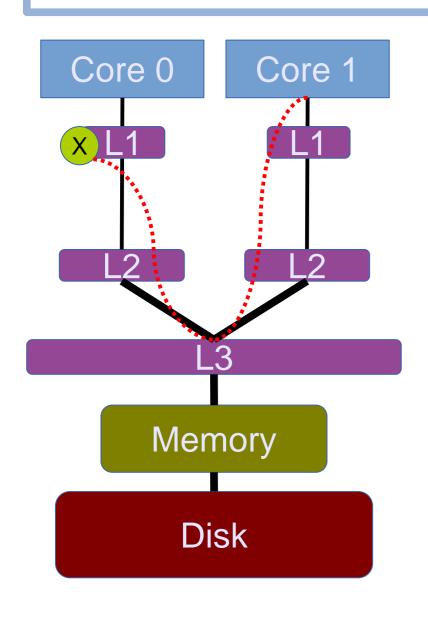
After ~2004: multi-cores



Multi-cores with private caches



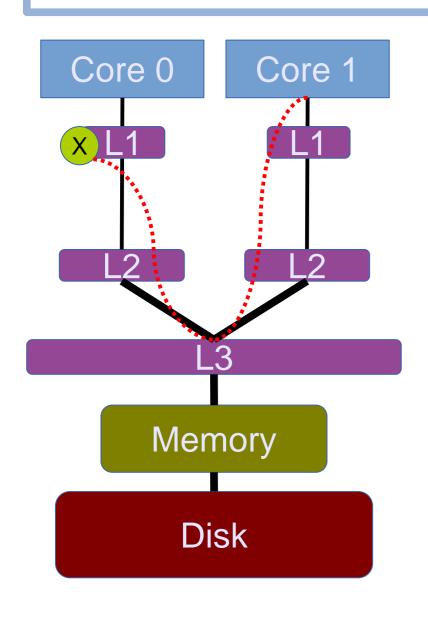
Cache coherence for consistency



Core 0 has X and Core 1

- wants to write on X
- wants to read X
- did Core 0 write or read X?

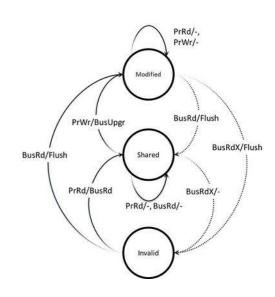
Cache coherence principles



- To perform a write
 - invalidate all readers, or
 - previous writer
- To perform a read
 - find the latest copy

Cache coherence with MESI

- A state diagram
- State (per cache line)
 - Modified: the only dirty copy
 - Exclusive: the only clean copy
 - Shared: a clean copy
 - Invalid: useless data



The ultimate goal for scalability

- Possible states
 - Modified: the only dirty copy
 - Exclusive: the only clean copy
 - Shared: a clean copy
 - Invalid: useless data

Which state is our "favorite"?

The ultimate goal for scalability

- Possible states
 - Modified: the only dirty copy
 - Exclusive: the only clean copy

-Shared: a clean copy

Invalid: useless data

- = threads can keep the data close (L1 cache)
- = faster

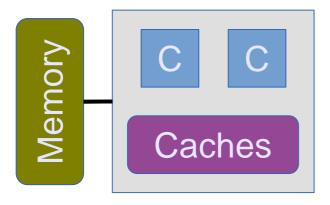
Experiment The effects of false sharing

Outline

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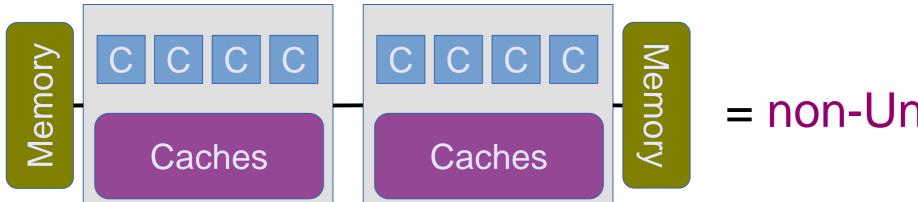
Uniformity vs. non-uniformity

Typical desktop machine

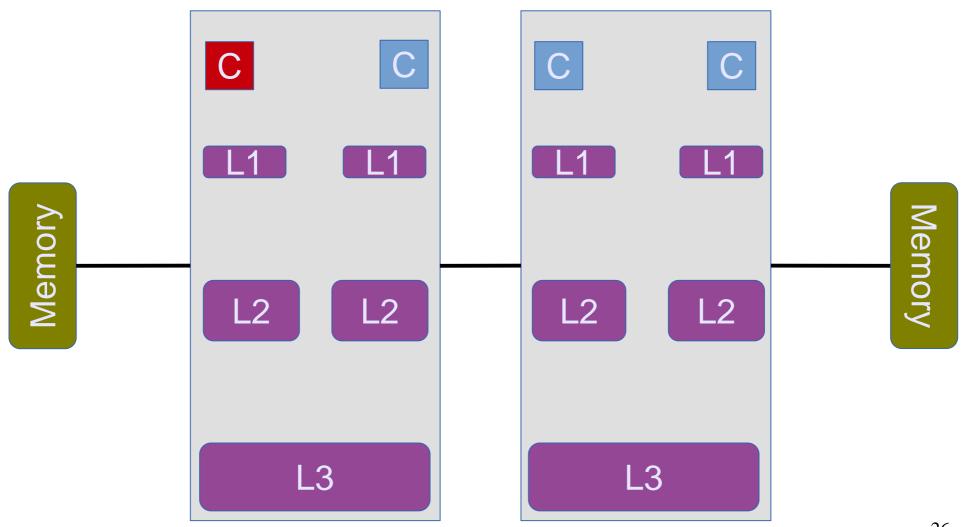


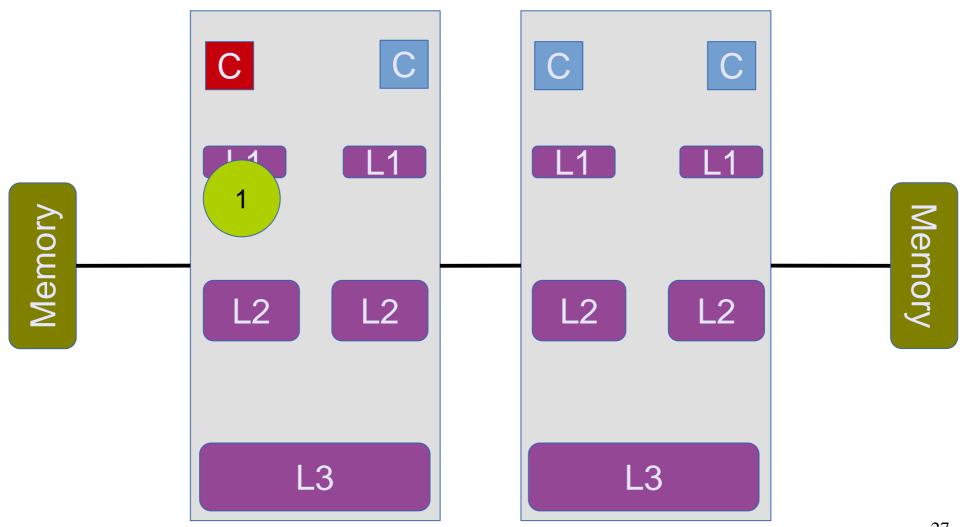
= Uniform

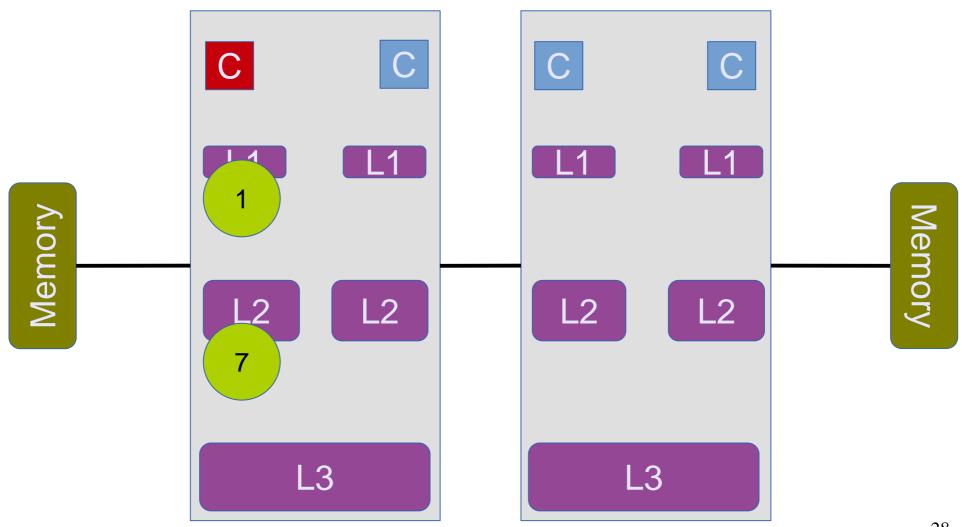
Typical server machine

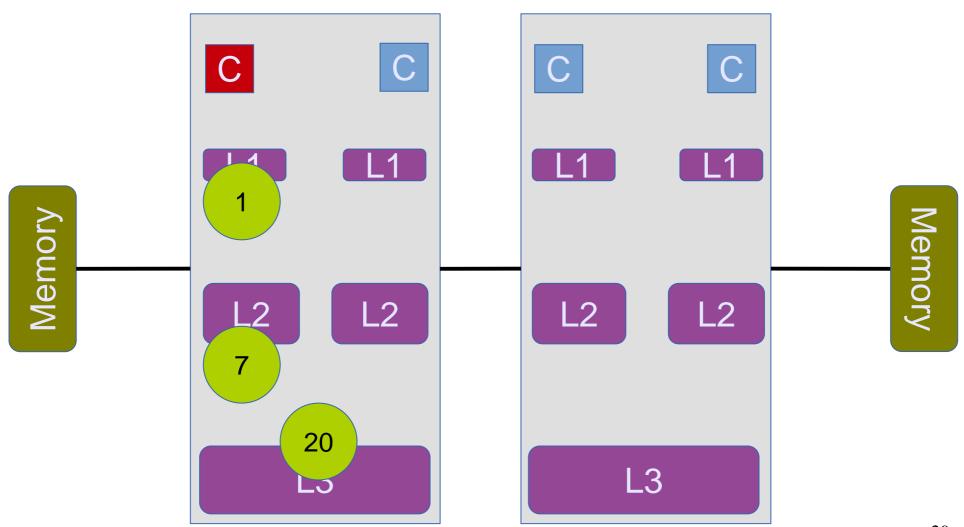


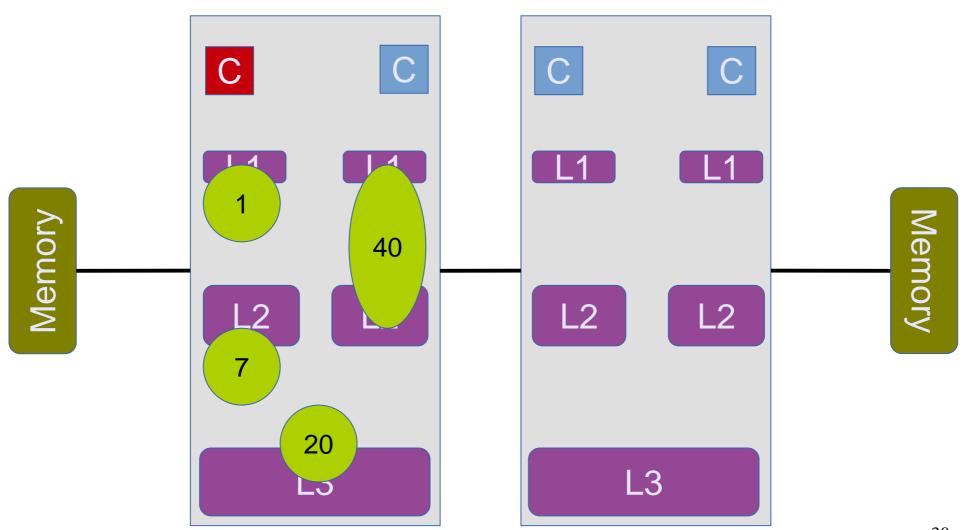
= non-Uniform

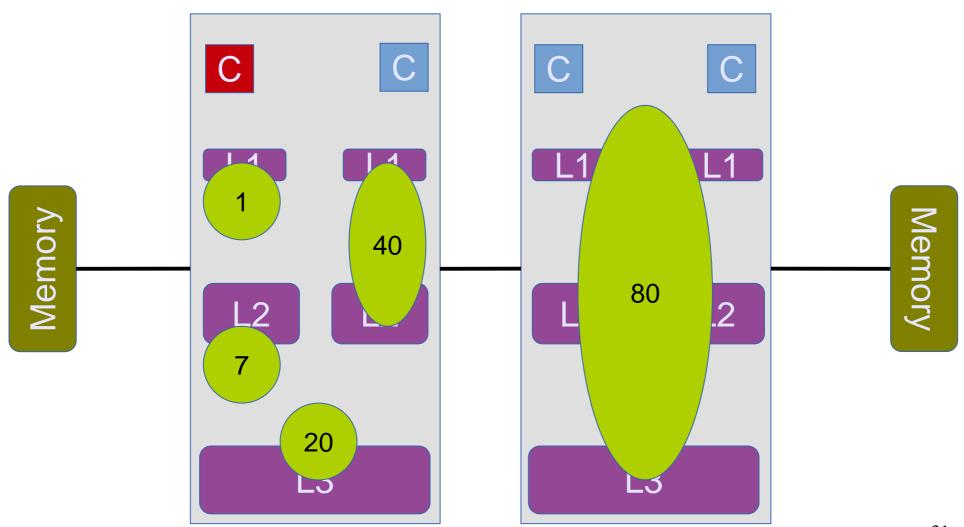


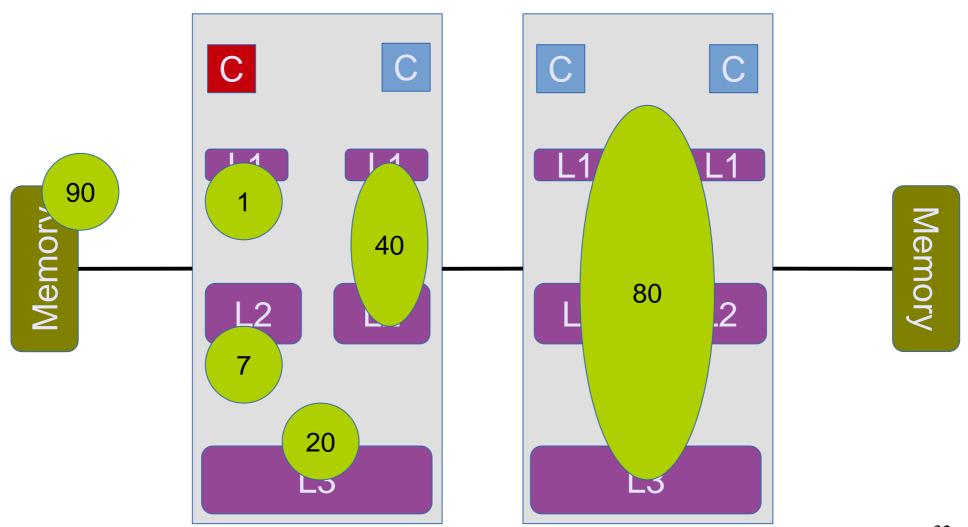


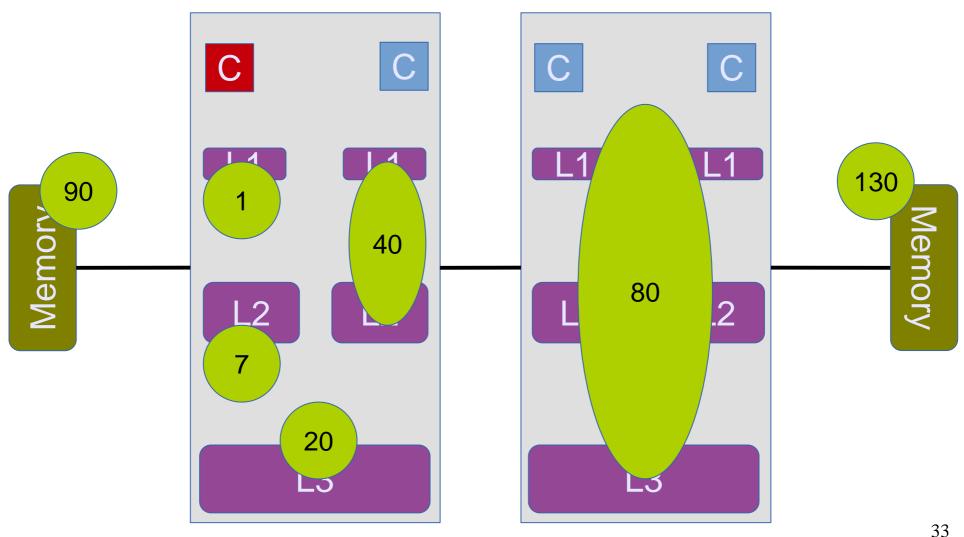


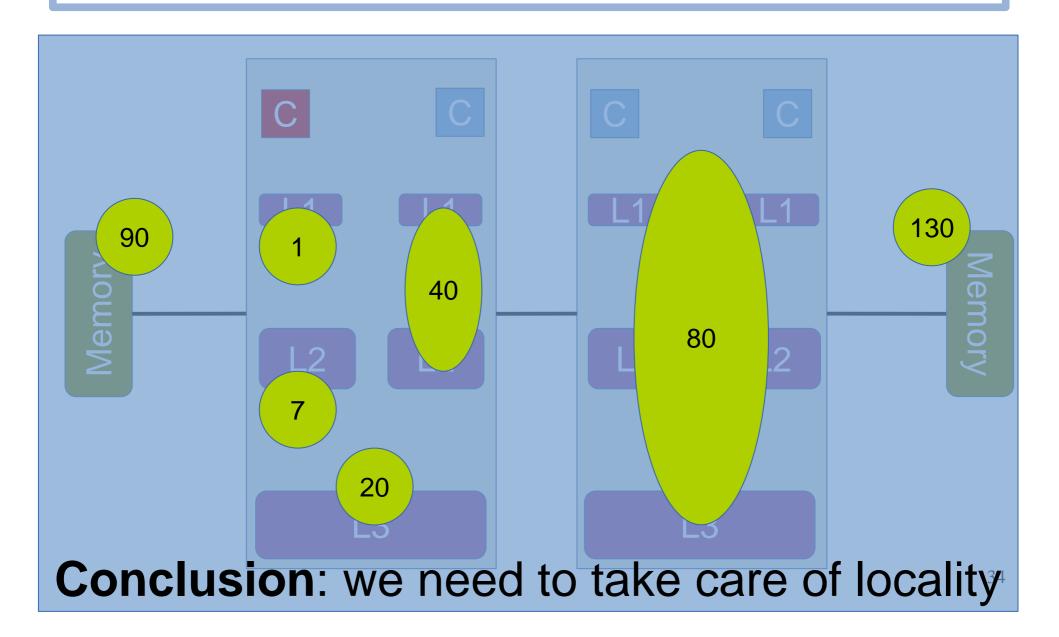












Experiment The effects of locality

Experiment The effects of locality

Outline

- CPU caches
- Cache coherence
- Placement of data
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Graph processing

Relational view

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Pec	Ta

Name	Likes
Vasilis	Breaking bad
Rachid	Dexter
Vasilis	Dexter

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Name	Similar
Breaking bad	Dexter
Dexter	Breaking bad

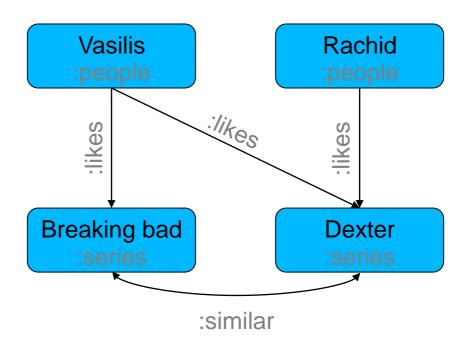
Graph processing

Relational view

People Table		Name	Likes
	Vasilis	Breaking bad	
	Rachid	Dexter	
	•	Vasilis	Dexter

(0		Name	Similar
rie	ple	Breaking bad	Dexter
Se	Ha Ta	Dexter	Breaking bad

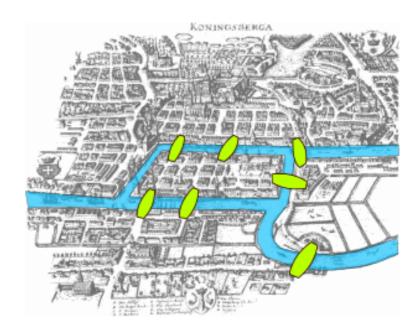
Graph view



Graphs keep the connections among entities materialized

Graph analytics

- Graphs have been studied in Math for centuries
 - Since Euler's "Seven Bridges of Königsberg", 1736
- Repeatedly traverse your graph and calculate math properties
- Classic graph problems
 - Graph isomorphism
 - Travelling salesman's problem
 - Max flow, min cut
 - ...
- More recent developments
 - Pagerank
 - Infomap

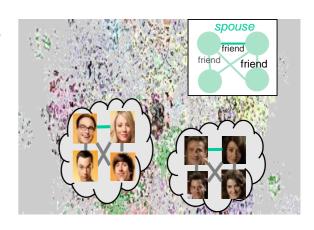


Graph queries

- Graph pattern matching
 - Query graphs to find sub-graphs that match a pattern e.g., triangle counting
- Essentially: SQL for graphs

Graph queries

- Graph pattern matching
 - Query graphs to find sub-graphs that match a pattern e.g., triangle counting
- Essentially: SQL for graphs
- Example: Friends of my friends



Graph processing frequently involves both analytics and queries

Dissecting a graph processing system

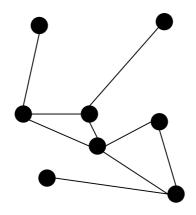
with a focus on (concurrent) data structures

Dissecting a graph processing system Preparing for a job interview

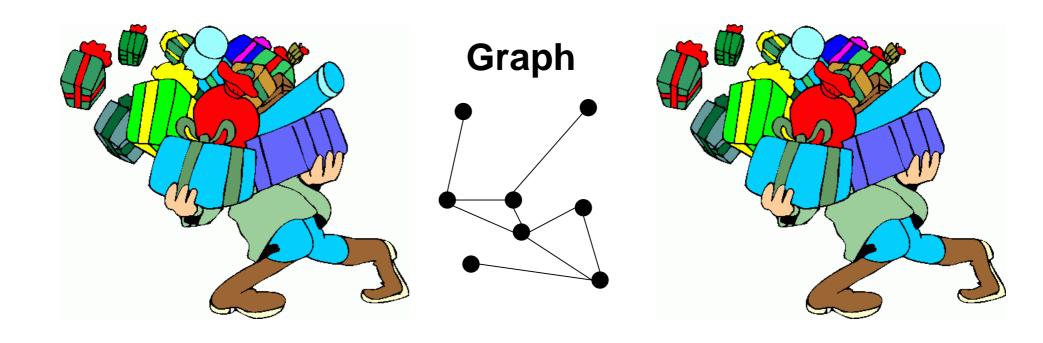
with a focus on (concurrent) data structures

Architecture of a graph processing system

Graph



Architecture of a graph processing system



Tons of other data and metadata to store

tmp graph structure



"Vasilis", "Breaking bad", :likes

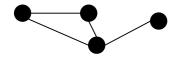
"Rachid", "Dexter", :likes

"Vasilis", "Dexter", :likes

"Dexter", "Breaking bad", :similar

"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ Rachid $\rightarrow 1$ $0 \rightarrow \text{Vasilis}$ $1 \rightarrow \text{Rachid}$

Breaking bad $\rightarrow 2$

 $2 \rightarrow$ Breaking bad

Dexter \rightarrow 3

 $3 \rightarrow Dexter$

labels

:likes, :people, :similar, ...

properties

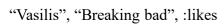
"Vasilis", {people, male}, 33, Zurich

"Rachid", {people, male}, ??, Lausanne

lifetime management

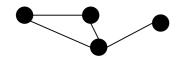
Runtime

tmp graph structure

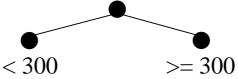


- "Rachid", "Dexter", :likes
- "Vasilis", "Dexter", :likes
- "Dexter", "Breaking bad", :similar
- "Breaking bad", "Dexter", :similar

graph structure



indices / / metadata



buffer management

1MB

1MB

1MB

1MB

user-ids - internal ids

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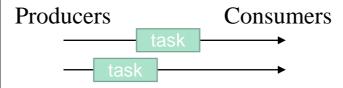
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lifetime management

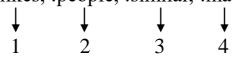
number of references: X

task / job scheduling



labels

:likes, :people, :similar, :male ...



 $\{\text{people, male}\} \rightarrow \{2,4\}$

renaming

used

used

used

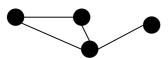
Runtime

Operations

tmp graph structure

- "Vasilis", "Breaking bad", :likes "Rachid", "Dexter", :likes
- "Vasilis", "Dexter", :likes
- "Dexter", "Breaking bad", :similar
- "Breaking bad", "Dexter", :similar

graph structure



1MB

metadata

>= 300

group by oin

Vasilis, Breaking bad Vasilis, 2 Rachid, Dexter Rachid, 1 Vasilis, Dexter

buffer management

< 300

indices /

1MB

distinct

Vasilis Rachid **Vasilis**



Vasilis Rachid

user-ids - internal ids

Vasilis $\rightarrow 0$ Rachid → 1

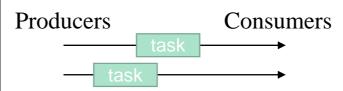
 $0 \rightarrow Vasilis$ 1 → Rachid Breaking bad $\rightarrow 2$

Dexter \rightarrow 3

 $2 \rightarrow$ Breaking bad

 $3 \rightarrow Dexter$

task / job scheduling



11 12 0 9 8 13 32 8 9 11 23 32 9 23 12357320 13

labels

:likes, :people, :similar, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

number of references: X

labels

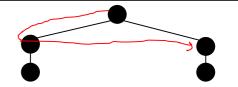
:likes, :people, :similar, :male ...

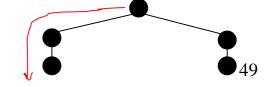
 $\{\text{people, male}\} \rightarrow \{2,4\}$

renaming

used used used

BFS





tmp graph structure

"Vasilis", "Breaking bad", :likes

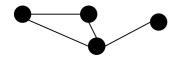
"Rachid", "Dexter", :likes

"Vasilis", "Dexter", :likes

"Dexter", "Breaking bad", :similar

"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis Rachid $\rightarrow 1$ 1 \rightarrow Rachid

Breaking bad \rightarrow 2 \rightarrow Breaking bad

Dexter $\rightarrow 3$ 3 \rightarrow Dexter

labels

:likes, :people, :similar, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

- tmp graph structure
 - append only
 - dynamic schema

tmp graph structure

"Vasilis", "Breaking bad", :likes

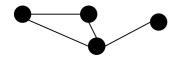
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lifetime management

- tmp graph structure
 - append only
 - dynamic schema
 - → segmented table

tmp graph structure

"Vasilis", "Breaking bad", :likes

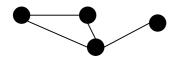
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graph structure



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lifetime management

- tmp graph structure
 - append only
 - dynamic schema
 - → segmented table
- Classic graph structures

tmp graph structure

"Vasilis", "Breaking bad", :likes

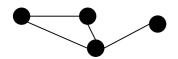
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"Vasilis", "Dexter", :likes

"Dexter", "Breaking bad", :similar

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graph structure



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"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

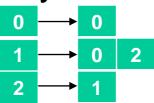
lifetime management

number_of_references: X

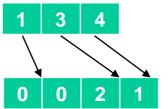
- tmp graph structure
 - append only
 - dynamic schema
 - → segmented table
- Classic graph structures
 - 1. connectivity matrix

	0	1	2
0	X		
1	X		X
2		Χ	

2. adjacency list



3. compressed source row (CSR)



tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Dexter", "Breaking bad", :similar

graph structure

"Breaking bad", "Dexter", :similar



user-ids - internal ids

Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis Rachid $\rightarrow 1$ 1 \rightarrow Rachid

Breaking bad \rightarrow 2 2 \rightarrow Breaking bad

Dexter $\rightarrow 3$ 3 \rightarrow Dexter

labels

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"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

- Mapping user ids to internal ids
 - create once
 - read-only after

tmp graph structure

"Vasilis", "Breaking bad", :likes

"Rachid", "Dexter", :likes

SOUTTER

"Dexter", "Breaking bad", :similar

"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis Rachid $\rightarrow 1$ 1 \rightarrow Rachid Breaking bad $\rightarrow 2$ 2 \rightarrow Breaking bad

Dexter $\rightarrow 3$ 3 \rightarrow Dexter

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"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

- Mapping user ids to internal ids
 - create once
 - read-only after
 - → hash map, lock-free reads

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
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graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis Rachid $\rightarrow 1$ 1 \rightarrow Rachid Breaking bad $\rightarrow 2$ 2 \rightarrow Breaking bad Dexter $\rightarrow 3$ 3 \rightarrow Dexter

labels

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properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

- Mapping user ids to internal ids
 - create once
 - read-only after
 - → hash map, lock-free reads
- Mapping internal ids to user ids
 - create once
 - read-only after
 - fixed key range: [0, N]

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Dexter", "Breaking bad", :similar
"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis Rachid $\rightarrow 1$ 1 \rightarrow Rachid Breaking bad $\rightarrow 2$ 2 \rightarrow Breaking bad Dexter $\rightarrow 3$ 3 \rightarrow Dexter

labels

:likes, :people, :similar, ...

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"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

- Mapping user ids to internal ids
 - create once
 - read-only after
 - → hash map, lock-free reads
- Mapping internal ids to user ids
 - create once
 - read-only after
 - fixed key range: [0, N]
 - → (sequential) array

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Dexter", "Breaking bad", :similar
"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis \rightarrow 0 0 \rightarrow Vasilis
Rachid
Breaking 1 \rightarrow Rachid
Dexter \rightarrow 3 \rightarrow Dexter

labels

:likes, :people, :similar, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

number_of_references: X

Storing labels

- usually a small enumeration e.g., person, female, male
- storing strings is expensive "person" → ~ 7 bytes
- comparing strings is expensive

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Dexter", "Breaking bad", :similar
"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis \rightarrow 0 0 \rightarrow Vasilis Rachid \rightarrow 1 \rightarrow Rachid Break 1 2 \rightarrow 2 \rightarrow Baking 3 \rightarrow Dexter

labels

:likes, :people, :similar, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

number of references: X

Storing labels

- usually a small enumeration e.g., person, female, male
- storing strings is expensive "person" → ~ 7 bytes
- comparing strings is expensive
- → dictionary encoding, e.g.,
 - person \rightarrow 0
 - female → 1
 - male \rightarrow 2

Ofc, hash map to

- store those
- translate during runtime

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Dexter", "Breaking bad", :similar
"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis
Rachid $\rightarrow 1$ \rightarrow Rachid
Breaking $\rightarrow 1$ \rightarrow Rachid
Dexter $\rightarrow 3$ 0 \rightarrow Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis $\rightarrow 0$ \rightarrow Vasilis $\rightarrow 0$ \rightarrow Dexter

labels

:likedictionariyr, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

number_of_references: X

Property

- one type per property, e.g., int
- 1:1 mapping with vertices/edges

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Dexter", "Breaking bad", :similar
"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis
Rachid $\rightarrow 1$ \rightarrow Rachid
Breaking $\rightarrow 1$ \rightarrow Rachid
Dexter $\rightarrow 3$ 0 \rightarrow Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis $\rightarrow 0$ \rightarrow Vasilis $\rightarrow 0$ \rightarrow Dexter

labels

:likedictionanyr, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

number_of_references: X

Property

- one type per property, e.g., int
- 1:1 mapping with vertices/edges
- → (sequential) arrays

tmp graph structure

"Vasilis", "Breaking bad", :likes

"Rachid", "Dexter", :likes

"Ouffer
"Dexter", "Breaking bad", :similar
"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ $0 \rightarrow \text{Vasilis}$ Rachidash and $2 \rightarrow \text{Rachidash}$ Breaking $1 \rightarrow \text{Rachidash}$ Dexter $\rightarrow 3$ $3 \rightarrow \text{Dexter}$

labels

:likedictionariyr, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

number_of_references: X

Property

- one type per property, e.g., int
- 1:1 mapping with vertices/edges
- → (sequential) arrays
- Lifetime management (and other counters)
 - cache coherence: atomic counters can be expensive

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Breaking bad", :similar
"Breaking bad", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ $0 \rightarrow \text{Vasilis}$ Rachidash 2 map $\stackrel{1}{\rightarrow}$ Rachidash
Breaking Sh 2 map $\stackrel{1}{\rightarrow}$ Rachidash
Dexter $\rightarrow 3$ $3 \rightarrow \text{Dexter}$

labels

:likedictionariyr, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

number_of_references: X

Property

- one type per property, e.g., int
- 1:1 mapping with vertices/edges
- → (sequential) arrays
- Lifetime management (and other counters)
 - cache coherence: atomic counters can be expensive
 - Two potential solutions
 - 1. approximate counters
 - 2. stripped counters

Thread local: counter[0] counter[1] counter[2]

```
increment(int by) { counter[my_thread_id] += by; }
int value() {
  int sum = 0;
  for (int i = 0; i < num_threads; i++) { sum += counter[i]; }
  return sum;</pre>
```

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Breaking bad", :similar
"Breaking bad", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ $0 \rightarrow \text{Vasilis}$ Rachihash 2 map^2 Breaking $3 \rightarrow \text{Dexter}$ Dexter $\rightarrow 3$ $3 \rightarrow \text{Dexter}$

labels

dictionary (= map)

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

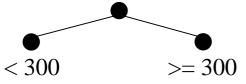
lifetime management

number_of_references: X
stripped counter

Score

Structure	# Usages
array / buffer	5
map	2

indices / metadata



buffer management

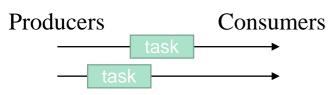
1MB

1MB

1MB

1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...



{people, male} \rightarrow {2,4}

renaming (ids)

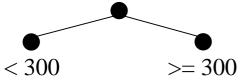
used

used

used

- Used for speeding up "queries"
 - Which vertices have label :person?
 - Which edges have value > 1000?

indices / metadata



buffer management

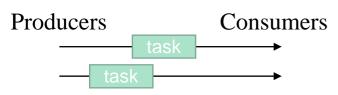
1MB

1MB

1MB

1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...



 $\{\text{people, male}\} \rightarrow \{2,4\}$

renaming (ids)

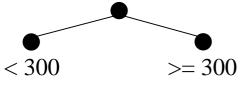
used

used

used

- Used for speeding up "queries"
 - Which vertices have label :person?
 - Which edges have value > 1000?
- →maps, trees

indices / metadata

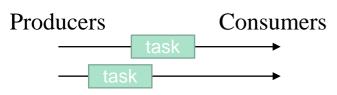


buffer management

1MB

1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...

 $\{\text{people, male}\} \rightarrow \{2,4\}$

renaming (ids)

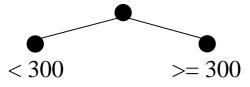
used

used

used

- Used for speeding up "queries"
 - Which vertices have label :person?
 - Which edges have value > 1000?
- →maps, trees
- Buffer management
 - In "real" systems, resource management is very important
 - buffer pools
 - no order
 - insertions and deletions
 - no keys

indices / metadata



buffer management

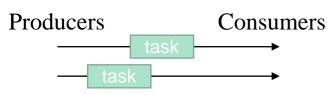
1MB

1MB

1MB

1MB

task / job scheduling



labels

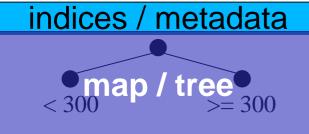
 $\{\text{people, male}\} \rightarrow \{2,4\}$

renaming (ids)

used used

sed used

- Used for speeding up "queries"
 - Which vertices have label :person?
 - Which edges have value > 1000?
- →maps, trees
- Buffer management
 - In "real" systems, resource management is very important
 - buffer pools
 - no order
 - insertions and deletions
 - no keys
 - → Fixed num object pool: array
 - → Otherwise: **list**
 - → Variable-sized elements: heap

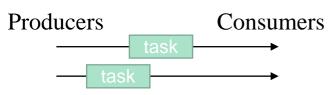


buffer management

1MB 1Marray

1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...



 $\{\text{people, male}\} \rightarrow \{2,4\}$

renaming (ids)

used

used

used

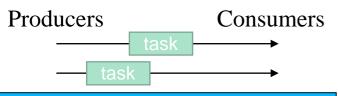
- Task and job scheduling
 - producers create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements

indices / metadata map / tree 300 >= 300

buffer management



task / job scheduling



labels

 $\{\text{people, male}\} \rightarrow \{2,4\}$

renaming (ids)

used used

d used

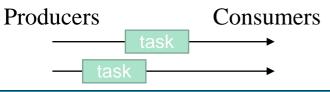
- Task and job scheduling
 - producers create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements
 - → queues
- Storing / querying sets of labels
 - set equality expensive
 - usually common groups
 e.g., {person, female}, {person, male}

indices / metadata map / tree 300 300

buffer management

1MB 1Marray/1B 1MB

task / job scheduling



labels

:likes, :people, :similar, :male ...

1 2 3 4

{people, male} \rightarrow {2,4}

renaming (ids)

used used

used

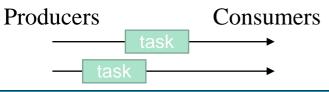
- Task and job scheduling
 - producers create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements
 - → queues
- Storing / querying sets of labels
 - set equality expensive
 - usually common groupse.g., {person, female}, {person, male}
 - → 2-level **dictionary** encoding
 - {person, female} → 0
 - {person, male} → 1

indices / metadata map / tree 300 300

buffer management



task / job scheduling



labels

 $\{\text{people, male}\} \rightarrow \{2,4\}$

renaming (ids)

used

used used

- Task and job scheduling
 - producers create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements
 - → queues
- Storing / querying sets of labels
 - set equality expensive
 - usually common groups
 e.g., {person, female}, {person, male}
 - → 2-level **dictionary** encoding
 - {person, female} → 0
 - {person, male} → 1
- Giving unique ids (renaming)

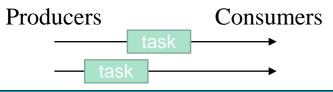
Runtime

indices / metadata map / tree 300 >= 300

buffer management

1MB 1Marray/B 1MB

task / job scheduling



labels

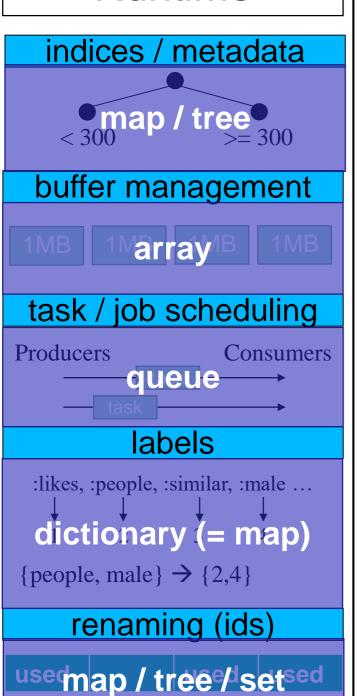
{people, male} \rightarrow {2,4}

renaming (ids)

used used used

- Task and job scheduling
 - produces create and share tasks
 - consumers get and handle tasks
 - insertions and deletions
 - usually FIFO requirements
 - → queues
- Storing / querying sets of labels
 - set equality expensive
 - usually common groups
 e.g., {person, female}, {person, male}
 - → 2-level **dictionary** encoding
 - {person, female} → 0
 - {person, male} → 1
- Giving unique ids (renaming)
 - → tree, map, set, counter, other?

Runtime



Score

Structure	# Usages
array / buffer	6
map	5
tree / heap	2
set	1
queue	1

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter
Rachid, 1

distinct

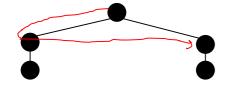
Vasilis Rachid Vasilis



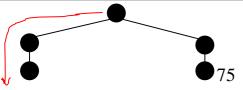
limit (top k)

11 12 0 9 8 13 8 9 11 23 32 9 1 2 3 5 7 3 2 0 13

BFS



DFS



Group by

- Mapping from keys to values
- 2. Atomic value aggregations e.g., COUNT, SUM, MAX
- insertion only

group by / join

Vasilis, Breaking bad
Rachid, Dexter
Vasilis, Dexter
Rachid, 1

distinct

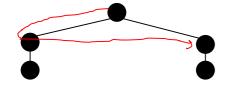
Vasilis Rachid Vasilis



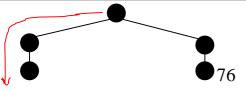
limit (top k)

11 12 0 9 8 13 8 9 11 23 32 9 1 2 3 5 7 3 2 0 13

BFS



DFS



Group by

- Mapping from keys to values
- 2. Atomic value aggregations e.g., COUNT, SUM, MAX
- insertion only
- → hash map
- → atomic inc / sum / max, etc.

group by / join

Vasilis, Breaking bad Rachid, Dexter Vasilis, Dexter

Vasilis, 2
Rachid, 1

distinct

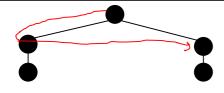
Vasilis Rachid Vasilis



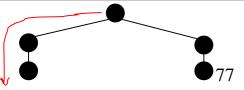
limit (top k)

11 12 0 9 8 13 8 9 11 23 32 9 1 2 3 5 7 3 2 0 13

BFS



DFS



Group by

- 1. Mapping from keys to values
- 2. Atomic value aggregations e.g., COUNT, SUM, MAX
- insertion only
- → hash map
- → atomic inc / sum / max, etc.

Join

- create a map of the small table
- insertion phase, followed by
- probing phase

group by / join

Vasilis, Breaking bad Rachid, Dexter Vasilis, Dexter

Vasilis, 2
Rachid, 1

distinct

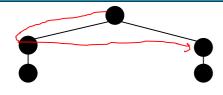
Vasilis Rachid Vasilis



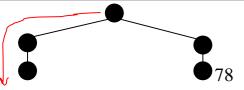
limit (top k)

11 12 0 9 8 13 8 9 11 23 32 9 1 2 3 5 7 3 2 0 13

BFS



DFS



Group by

- 1. Mapping from keys to values
- 2. Atomic value aggregations e.g., COUNT, SUM, MAX
- insertion only
- → hash map
- → atomic inc / sum / max, etc.

Join

- create a map of the small table
- insertion phase, followed by
- probing phase
- → hash map, lock-free probing

group by / join

Vasilis, Breaking bad
Rachid Dexter
Vasilis, 2
Vasilis, 2
Tatomics1

distinct

Vasilis Rachid Vasilis



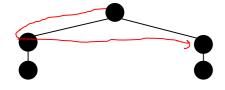
Vasilis Rachid

limit (top k)

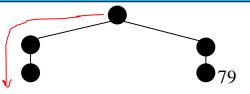
11 12 0 9 8 13 8 9 11 23 32 9 1 2 3 5 7 3 2 0



BFS



DFS



Distinct

can be solved with sorting, or

group by / join

Vasilis, Breaking bad
Rachid Dexter
Vasilis, 2
Vasilis, 2

Vasilis, 2

Tatomics 1

distinct

Vasilis Rachid Vasilis



Vasilis Rachid

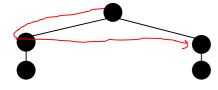
23

13

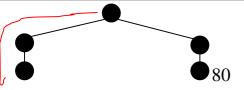
limit (top k)

11 12 0 9 8 13 8 9 11 23 32 9 1 2 3 5 7 3 2 0

BFS



DFS



Distinct

- can be solved with sorting, or
- → hash set

group by / join

Vasilis, Breaking bad
Rachid Dexter Vasilis, 2
Vasilis, Dexter Vasilis, 2

distinct

Vasilis Rachid Vasilis

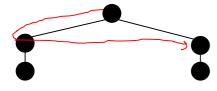


Vasilis Rachid

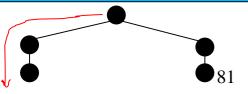
limit (top k)

11 12 0 9 8 13 8 9 11 23 32 9 1 2 3 5 7 3 2 0 13

BFS



DFS



Distinct

- can be solved with sorting, or
- → hash set
- Limit (top k)
 - can be solved with sorting, or
 - different specialized structures

group by / join

Vasilis, Breaking bad
Rachid Dexter
Vasilis, 2

Vasilis, 2

Tatomics

distinct

Vasilis Rachid Vasilis

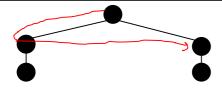


Vasilis Rachid

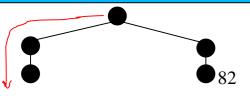
limit (top k)

11 12 0 9 8 13 8 9 11 23 32 9 1 2 3 5 7 3 2 0 13

BFS



DFS



Distinct

- can be solved with sorting, or
- → hash set
- Limit (top k)
 - can be solved with sorting, or
 - different specialized structures
 - → tree
 - → heap
 - → ~ list
 - → array (e.g., 2 elements only)
 - → register (1 element only)

group by / join

Vasilis, Breaking bad
Rachid Dexter
Vasilis, 2
Vasilis, 2

Vasilis, 2

Tatomics

Tatomics

Tatomics

distinct

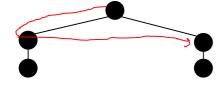
Vasilis Rachid Vasilis

hash set achid

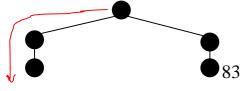
limit (top k)

11 12 0 9 8 13 8 9 1 tree 9/ heap /3 ist

BFS



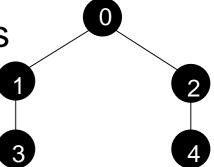
DFS



Breadth-first search (BFS)



track visited vertices



group by / join

Vasilis, Breaking bad
Rachid Dexter
Vasilis, 2
Vasilis, 2

Vasilis, 2

Tatomics

Tatomics

Tatomics

distinct

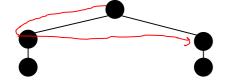
Vasilis Rachid Vasilis

hash set achid

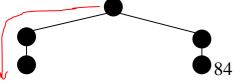
limit (top k)

11 12 0 9 8 13 8 9 1 tree 9/ heap /3 ist

BFS



DFS

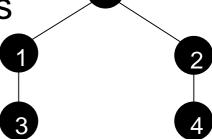


Breadth-first search (BFS)



track visited vertices

- → queue
- \rightarrow set



group by / join

Vasilis, Breaking bad
Rachid Dexter
Vasilis, 2
Vasilis, 2
Tatomics1

distinct

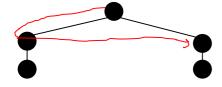
Vasilis Rachid Vasilis

hash setachid

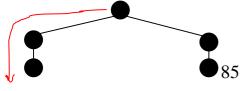
limit (top k)

11 12 0 9 8 13 8 9 1 **tree**9/ heap /3 ist

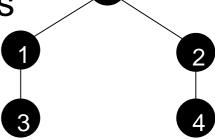
BFS



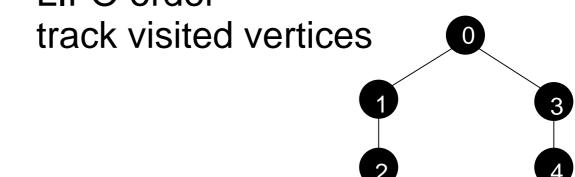
DFS



- Breadth-first search (BFS)
 - FIFO order
 - track visited vertices
 - → queue
 - \rightarrow set



- Depth-first search (DFS)
 - LIFO order



group by / join

Vasilis, Breaking bad
Rachid Dexter
Vasilis, 2
Vasilis, 2
Tatomics1

distinct

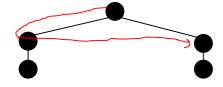
Vasilis Rachid Vasilis

hash set achid

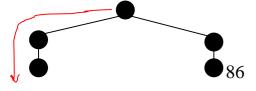
limit (top k)

11 12 0 9 8 13 8 9 1 **tree**9/ heap /²³list

BFS



DFS



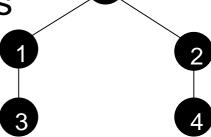
Breadth-first search (BFS)



track visited vertices



 \rightarrow set



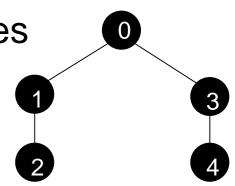
Depth-first search (DFS)

LIFO order

track visited vertices

→ stack

 \rightarrow set



group by / join

Vasilis, Breaking bad
Rachid Dexter Vasilis, 2
Vasilis, Dexter Vasilis, 2

distinct

Vasilis Rachid Vasilis

hash set achid

limit (top k)

11 12 0 9 8 13 8 9 1 **tree**9/ heap /3 ist

BFS



DFS



Score

Structure	# Usages
array / buffer	7
map	6
set	4
tree / heap	3
queue	2
stack	1
list	1

Graph

Runtime

Operations

tmp graph structure

"Vasilis", "Breaking bad", :likes
"Rachid", "Dexter", :likes
"Dexter", "Breaking bad", :similar
"Breaking bad", "Dexter", :similar

graph structure



user-ids - internal ids

Vasilis $\rightarrow 0$ 0 \rightarrow Vasilis

Rachid $\rightarrow 1$ Rachid

Breaking $\rightarrow 1$ Rachid

Dexter $\rightarrow 3$ 3 \rightarrow Dexter

labels

:likedictionanyr, ...

properties

"Vasilis", {people, male}, 33, Zurich "Rachid", {people, male}, ??, Lausanne

lifetime management

number_of_references: X
stripped counter

indices / metadata



buffer management

1MB 1Marray 18 11

task / job scheduling



labels

:likes, :people, :similar, :male ...

1 dictionary 4

{people, male} \rightarrow {2,4}

renaming (ids)

usemap / tree / setsed

group by / join

Vasilis, Breaking bad
Rachid Dexter / atomics

distinct

Vasilis
Rachid hash set
Vasilis

limit (top k)

11 12 0 9 8 13 8 9 1 **tree** 9 / heap / list

BFS



DFS



Conclusions

- Both theory and practice are necessary for
 - Designing, and
 - Implementing fast / scalable data structures
- Hardware plays a huge role on implementations
 - How and which memory access patterns to use
- (Concurrent) Data structures
 - The backbone of every system
 - An "open" and challenging area or research

vasileios.trigonakis@oracle.com - internships++