# Distributed Algorithms, Final Exam Solution

January 2016

## Part I Broadcast (12 points)

Answer the following questions in the provided spaces.

### Question 1 (5x1 = 5 points)

Which of the following properties are safety properties and which are liveness? Mark an "S" or "L" next to each property **clearly** with a *one line* explanation.

- 1. For any message  $m_1$  delivered by a process  $p_1$ , if there exists another process  $p_2$  that delivered  $m_1$  and then delivered a message  $m_2$ , then  $p_1$  also delivers  $m_2$ .  $\underline{L}$
- 2. For every pair of processes  $p_1$  and  $p_2$  that deliver a message  $m_1$ , if  $p_1$  delivers a message  $m_2$  before delivering  $m_1$ , then  $p_2$  also delivers  $m_2$  before delivering  $m_1$ . S
- 3. Every process that crashes is eventually detected.  $\underline{\mathbf{L}}$
- 4. No process is detected before it crashes.  $\underline{S}$
- 5. No two processes deliver the same message.  $\underline{S}$

## Question 2 (3x1 = 3 points)

Mention the properties for the following:

 Causal broadcast (C) Answer: CO1. Validity: If p<sub>i</sub> and p<sub>j</sub> are correct, then every message broadcast by p<sub>i</sub> is eventually delivered by p<sub>j</sub>.
 CO2. No duplication: No message is delivered more than once.
 CO3. No creation: No message is delivered unless it was broadcast CO4. Agreement: For any message m, if a correct process delivers m, then every correct process delivers m.

CO5: Causal order: If any process  $p_i$  delivers a message  $m_2$ , then  $p_i$  must have delivered every message  $m_1$  such that  $m_1 - > m_2$ .

2. Total order broadcast (T)

Answer:

TOB1. Validity: If  $p_i$  and  $p_j$  are correct, then every message broadcast by  $p_i$  is eventually delivered by  $p_j$ .

TOB2. No duplication: No message is delivered more than once.

TOB3. No creation: No message is delivered unless it was broadcast

TOB4. Agreement: For any message m, if a correct process delivers m, then every correct process delivers m.

TOB5. Total order: The processes must deliver all messages according to the same order (i.e., the order is now total).

3. Uniform reliable broadcast (U)  $\,$ 

Answer:

URB1. Validity: If  $p_i$  and  $p_j$  are correct, then every message broadcast by  $p_i$  is eventually delivered by  $p_j$ .

URB2. No duplication: No message is delivered more than once.

URB3. No creation: No message is delivered unless it was broadcast

URB4. Uniform Agreement: For any message m, if a process delivers m, then every correct process delivers m.

## Question 3 (2 points)

Consider the broadcast executions shown below. Which of the following statements are true about this execution? Use the notations from question 2.



## Question 4 (2 points)

Consider the broadcast executions shown below. Which of the following statements are true about this execution? Use the notations from question 2.



- 1. C
- 2. T
- 3. U
- 4. C & T
- 5. T & U
- 6. C & U
- 7. C & T & U
- 8. None of the above.

Answer: C & T & U (7)

# Part II Consensus, NBAC, TRB, GM (15 points)

## Question 1 (5x2 points)

Indicate which sentence is true and which is false with a T and F about three different consensus algorithms, respectively. Explain your answer.

Algorithm I (nonuniform consensus with P): The processes exchange and update proposals in rounds and decide on the value of the non-suspected process with the smallest id.

Algorithm II (uniform consensus with P): The processes exchange and update proposal in rounds, and decide after n rounds.

Algorithm III (uniform consensus with majority): The processes alternate in the role of a coordinator until one of them succeeds in imposing a decision.

- Algorithm I can satisfy uniform consensus if we use Uniform Reliable Broadcast instead of Best Effort Broadcast. Answer: F.
- In algorithm II, the decided value is proposed by the correct process with lowest ID. Answer: F.
- Using a ◊P in algorithm II does not violate Agreement property but Termination. Answer: F.
- 4. In algorithm III, if  $p_i$  is leader and decides, the decided value is actually proposed by  $p_i$ . Answer: F.
- 5. Algorithm III finishes in at least N rounds because a process processes its value in a round only if it is the leader in that round. *Answer:* F. If all the processes are correct and none of them is suspected in the first round, the leader can impose a decision in the first round.

## Question 2 (4x0.5 point)

Explain the difference between each of the following pairs of abstractions in terms of their respective properties.

- 1. Consensus and Non Blocking Atomic Commit (NBAC).
- 2. Reliable Broadcast and Terminating Reliable Broadcast.
- 3. Group Membership and perfect failure detector (P).
- 4. View Synchrony and uniform view Synchrony.

## Question 3 (3x1 point)

Each of the below executions represents a NBAC abstraction implemented using Uniform Consensus. All the processes propose 1 in the beginning. Write all the possible values (0, 1, or 0/1) for **a**, **b**, **c** and **d** in each execution. ( $\otimes$  shows the sender is detected to have crashed and the message is lost.)



# Part III Process Failures and Shared Memory (13 points)

## Question 1

Consider the fail-silent system model, i.e., where processes may fail by crashing, and the failure detection *cannot* be detected, so no failure detector can be used.

- 1. Does any implementation of a regular register require a majority of correct processes in this case? Explain your answer.
- 2. Now suppose an eventually perfect failure detector is available is a correct majority still required? Explain your answer.

#### Answer

See solution 4.8 in the course book, pg. 197-198.

### Question 2

Mark each of the following statements with either:

- T, if the statement is true, or
- F, if that statement is false.
- 1. Consider any algorithm running in system of n total processes. The algorithm does not make use of any failure detector, thus this system must comprise at least  $n = 2 \cdot f + 1$  processes in order to tolerate a predefined subset of f processes crashing. [F]
- 2. The Uniform Reliable Broadcast abstraction ensures that, despite a process crashing while it broadcasts a message m, the correct processes still eventually deliver m. [F]
- 3. A regular register execution where no crashes occur is equivalent with an atomic register execution. [F]
- 4. Consider a Reliable Broadcast algorithm. If all sending processes are assumed to be correct, then this algorithm actually satisfies the Uniform variant of Agreement. [T]

5. If sending processes in a Causal Broadcast algorithm are assumed to be correct, then this algorithm actually satisfies the Uniform Causal Broadcast specification. [T]

### Question 3. A regular register array.

#### (4.5 points)

Traditional registers, as defined in the class, are meant to store one single object (e.g., a value). A *register array*, in contrast, is able to store multiple objects.

We consider a regular register array algorithm  $\mathcal{A}$  which relies on m underlying regular registers,  $[R_0, ..., R_{m-1}]$ . Each underlying register stores an object. We assume that all objects have the form of  $\langle key_i/value_i \rangle$  tuples, with  $i \in \{0, ..., m-1\}$ . Thus, each object is uniquely associated with one of the underlying registers, such that object with key  $key_i$  is associated register  $R_i$ .

Additionally, we require that  $\mathcal{A}$  runs on N processes,  $p_0, ..., p_{N-1}$ , where  $N = M \cdot 2$ . To ensure reliability, this algorithm guarantees that every underlying register is replicated at two processes, as follows. Processes are first grouped in pairs,  $\{p_0, p_1\}, \{p_2, p_3\}, ..., \{p_{N-2}, p_{N-1}\}$ . And then each process pair replicates one of the registers, such that the first pair of processes handles (i.e., replicates) register  $R_0$ , the second pair handles register  $R_1$ , and so on.

For handling any read or write operation on a key  $key_i$ , a process either triggers that operation on its underlying register (if  $key_i$  is associated to its underlying register), or it forwards the operation to one of the two processes handling the register associated with  $key_i$ .

The specification of a regular register array is as follows:

Name: Regular register array.

**Properties:** Same as properties *Termination* and *Validity* of regular registers. **Requests:** 

read( $k_i$ )  $\rightarrow v_i$ ,

write $(k_i, v_i)$ , where  $k_i$  is they key of the object, and  $v_i$  is the value.

Give an implementation of  $\mathcal{A}$ , assuming that the *m* underlying regular registers are already provided.

Algorithm 1 A regular register array.

```
1: Implements:
 2:
         Regular register array (\mathcal{A})
 3: Uses:
 4:
         RegularRegister (rr_i)
 5: upon event \langle read \mid k_x \rangle at process p_i do
         if (i = 2 \cdot x) || (i = 2 \cdot x + 1) then
 6:
 7:
              trigger \langle rr_i, read \mid k_x \rangle
 8:
         else
              p = x * 2 \# p is one of the processes handling k_i
 9:
10:
              forward \langle \mathcal{A}, read | k_x \rangle to process p
11:
          end if
12: upon event \langle write \mid k_x, v \rangle at process p_i do
          if (i = 2 \cdot x) || (i = 2 \cdot x + 1) then
13:
14:
              trigger \langle rr_i, write \mid k_x, v \rangle
15:
          \mathbf{else}
              p = x * 2 \# p is one of the processes handling k_i
16:
              forward \langle \mathcal{A}, write \mid k_i, v \rangle to process p
17:
          end if
18:
```