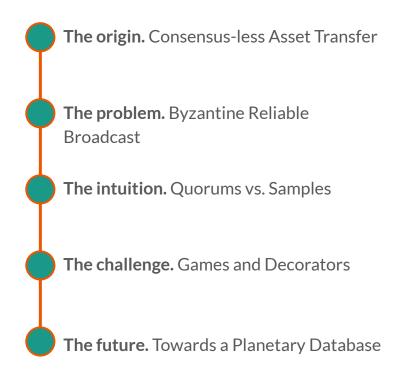
Planetary Scale Systems

Matteo Monti Distributed Computing Laboratory Ecole Polytechnique Fédérale de Lausanne

Distributed Algorithms Course - 30/11/2020

Summary

Randomized algorithms hold a promise for planetary scale systems.

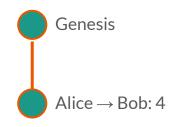


Consensus-less Asset Transfer

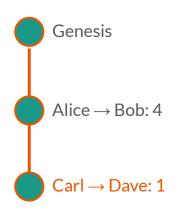


Alice	5
Bob	6
Carl	0
Dave	3

Alice	1
Bob	10
Carl	0
Dave	3



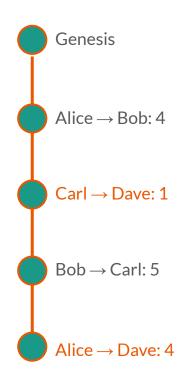
Alice	1
Bob	10
Carl	0
Dave	3



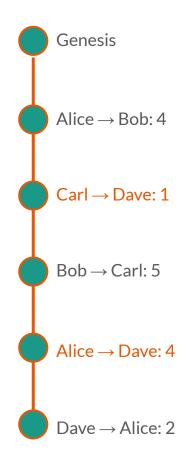
Alice	1
Bob	5
Carl	5
Dave	3



Alice	1
Bob	5
Carl	5
Dave	3



Alice	3
Bob	5
Carl	5
Dave	1





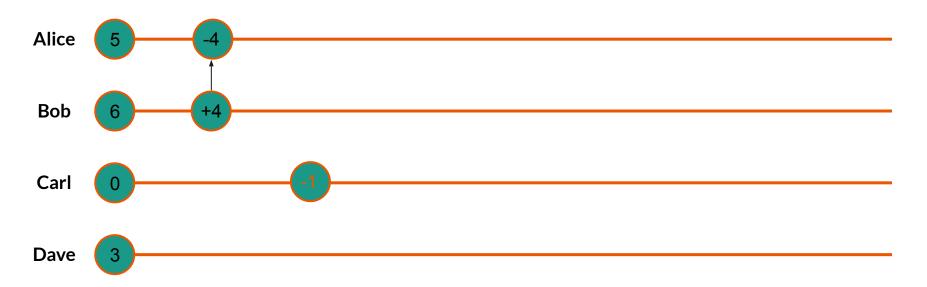
Alice	5	Carl	0
Bob	6	Dave	3



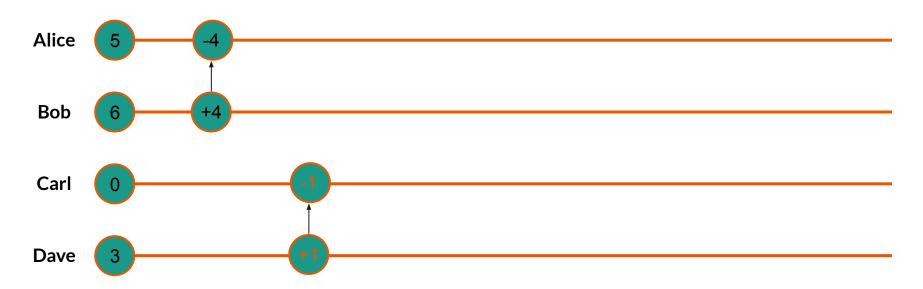
Alice	1	Carl	0
Bob	6	Dave	3



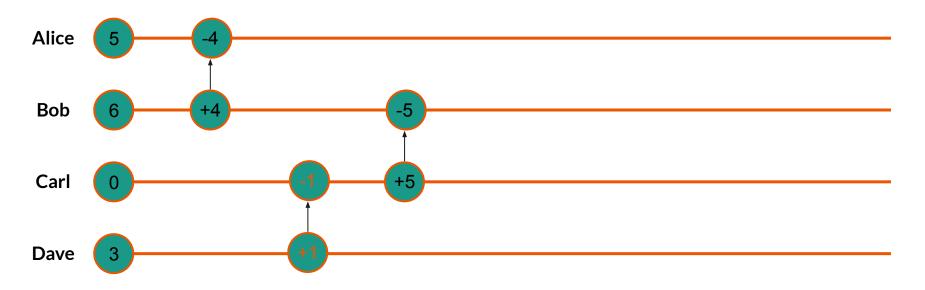
Alice	1	Carl	0
Bob	10	Dave	3



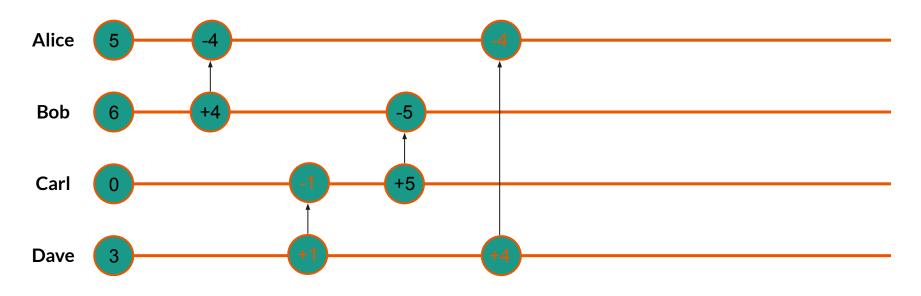
Alice	1	Carl	0
Bob	10	Dave	3



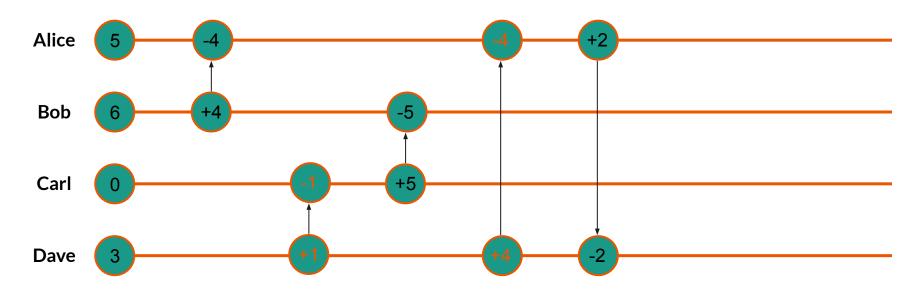
Alice	1	Carl	0
Bob	10	Dave	3



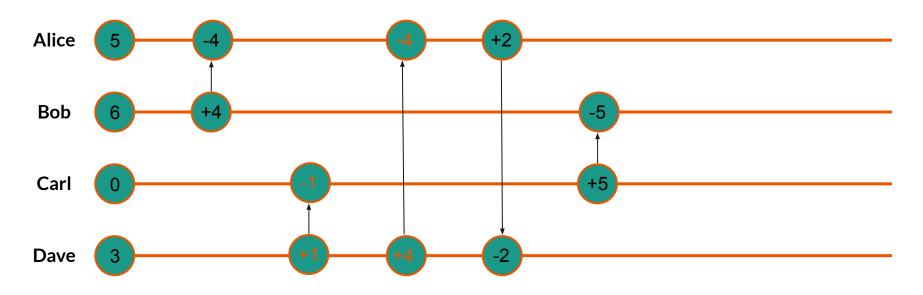
Alice	1	Carl	5
Bob	5	Dave	3



Alice	1	Carl	5
Bob	5	Dave	3



Alice	3	Carl	5
Bob	5	Dave	1



Alice	3	Carl	5
Bob	5	Dave	1

Solving Source-Order Broadcast

Solving Asset Transfer*

[★] Guerraoui, Rachid, et al. "The Consensus Number of a Cryptocurrency"

Proceedings of the 2019 ACM Symposium on Principles of Distributed Computing, 2019.

Per-source FIFO

$\pi_{_1}$	1	2	3 	4	5 	6 	7 	8	9	10 	•••
π_2	1	2	3	4	5 	6 	7 	8	9	10 	•••
π_3	1	2	3	4	5 	6 	7	8	9	10 	
$\pi_{_4}$	1	2	3	4	5 	6	7	8	9	10	•••

1	2	3	4	5	6	7	8	9	10	•••
									•••	

1	2	m_{\circ}	4	5	6	7	8	9	10	• • •
		,,,3								

m.	2	m _o	4	5	6	7	8	9	10	•••
111		3								

m_1	2	m_3	m ₄	5 	6 	7 	8	9	10 	•••
-------	---	-------	----------------	-------	-------	-------	---	---	--------	-----

m_1 m_2 m_3	m ₄ 5	6	7 	8	9	10 	•••
-------------------	------------------	---	-------	---	---	--------	-----

m_{1}	m_2 m_3	m ₄	5 	6 	m ₇	8 	9	10 	•••
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Solving Reliable Broadcast = Solving Asset Transfer

Byzantine Reliable Broadcast

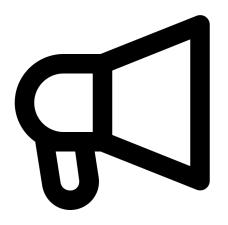
Interface

Broadcast

Request

Deliver

Indication





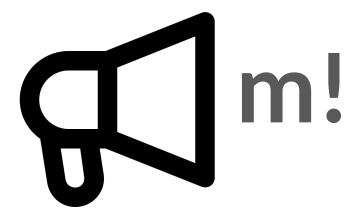
Interface

Broadcast

Request

Deliver

Indication





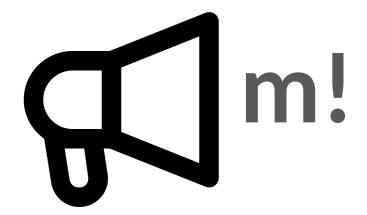
Interface

Broadcast

Request

Deliver

Indication





Properties

Deterministic case

Validity + Consistency + Totality

Validity Consistency **Totality**

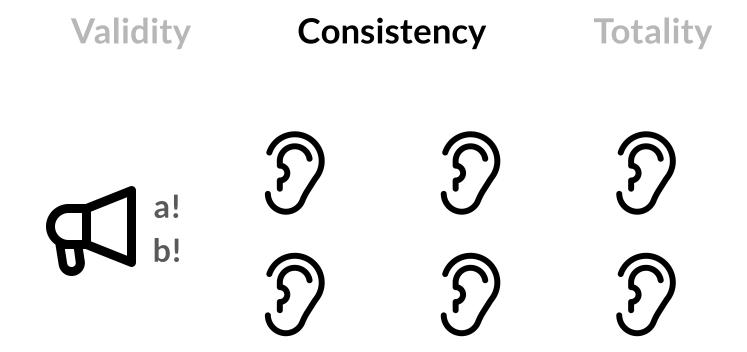
If the sender is correct, every correct process delivers its message.

Validity Consistency Totality

(S) m! (S) m!

(S) m! (S) m!

If the sender is correct, every correct process delivers its message.



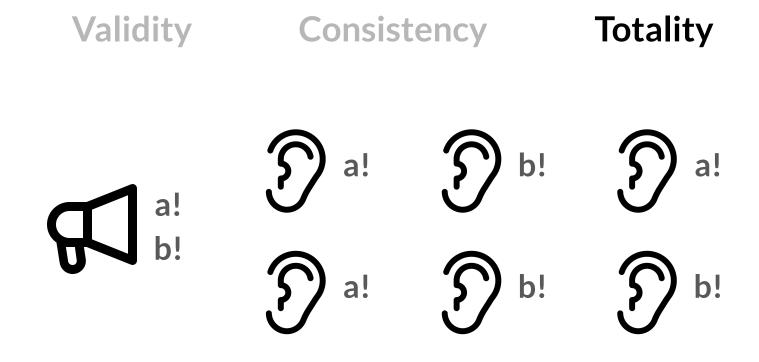
If two correct processes deliver a message, they deliver the same message.

Validity Consistency Totality

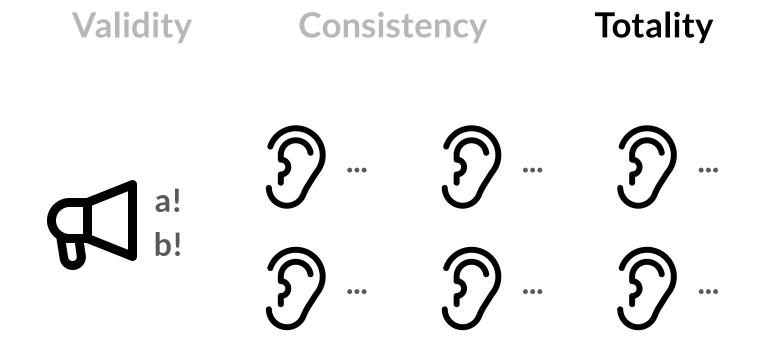
If two correct processes deliver a message, they deliver the same message.



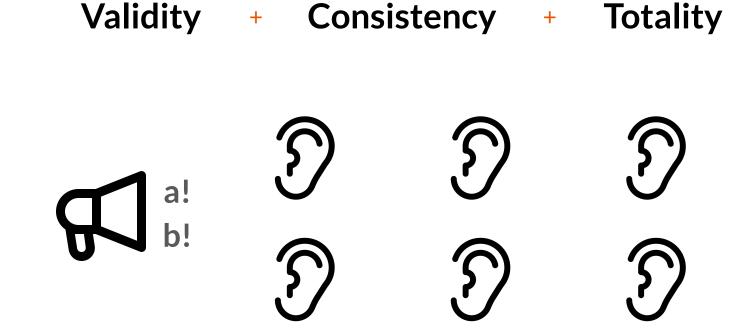
Either every correct process delivers a message, or no correct process delivers a message.



Either every correct process delivers a message, or no correct process delivers a message.



Either every correct process delivers a message, or no correct process delivers a message.



If the sender is correct, every correct process delivers its message. Either every correct process delivers the same message, or no correct process delivers any message.

Validity + Consistency + Totality (5) a! (5) a! (5) a! (5) a!

If the sender is correct, every correct process delivers its message. Either every correct process delivers the same message, or no correct process delivers any message.

Validity + Consistency + Totality

If the sender is correct, every correct process delivers its message. Either every correct process delivers the same message, or no correct process delivers any message.

Deterministic case

Validity + Consistency + Totality

Termination

Deterministic case



Deterministic case

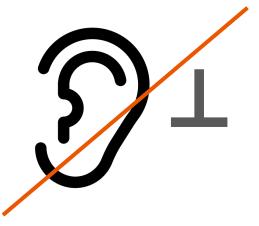




Deterministic case







Deterministic case

Validity + Consistency + Totality

Probabilistic case

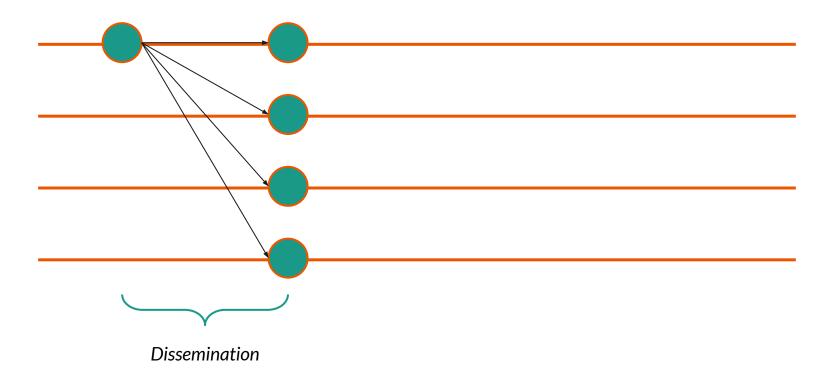
Validity + Consistency + Totality

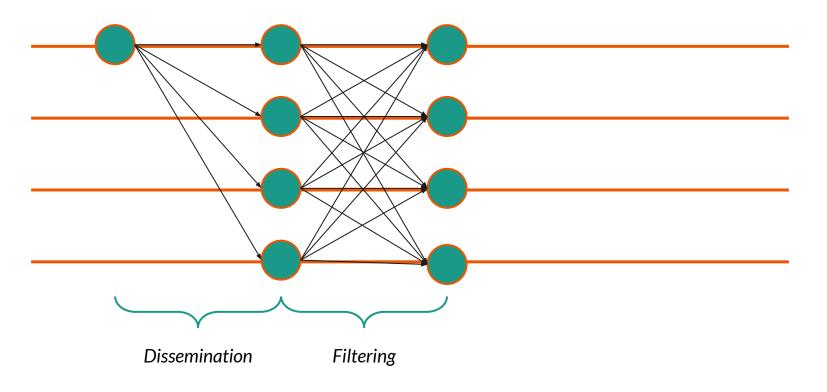
with probability $\geq (1 - \varepsilon)$

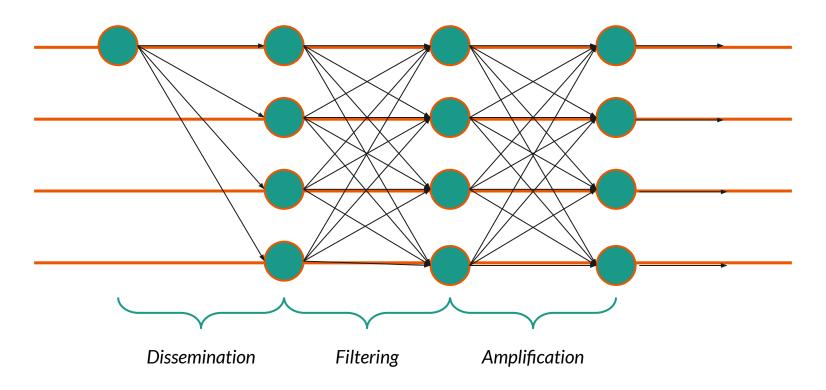
Quorums vs. Samples



[★] Bracha, Gabriel "Asynchronous Byzantine Agreement Protocols" Information and Computation, 1987.

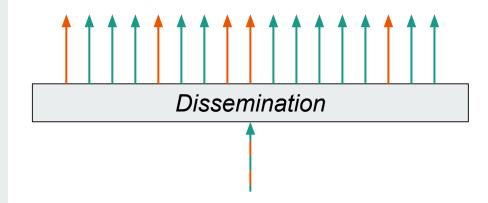






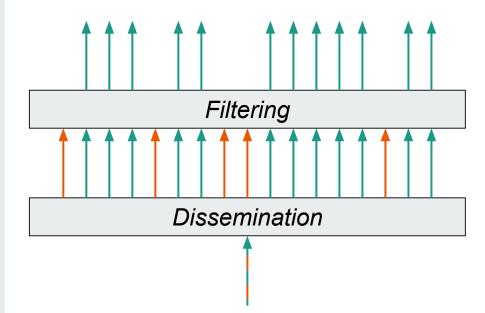
Dissemination

Validity + Totality



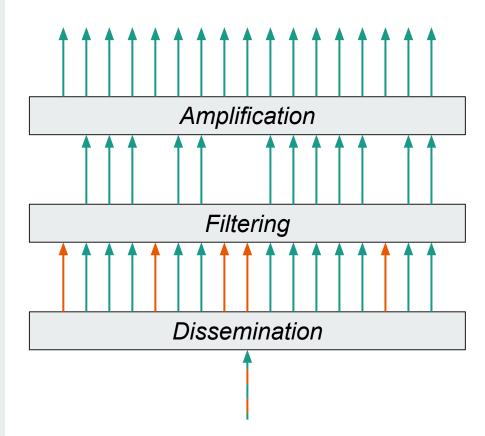
Filtering

Validity + Consistency



Amplification

Validity + Consistency + Totality



What fraction q of the processes satisfy a property P?

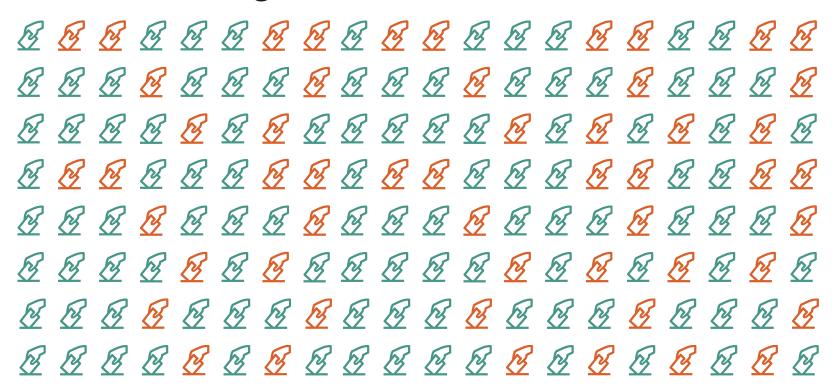
Quorum Voting



Quorum Voting

$$q = 17/24$$

Quorum Voting



Gathering a quorum costs O(N) messages

Sample Voting

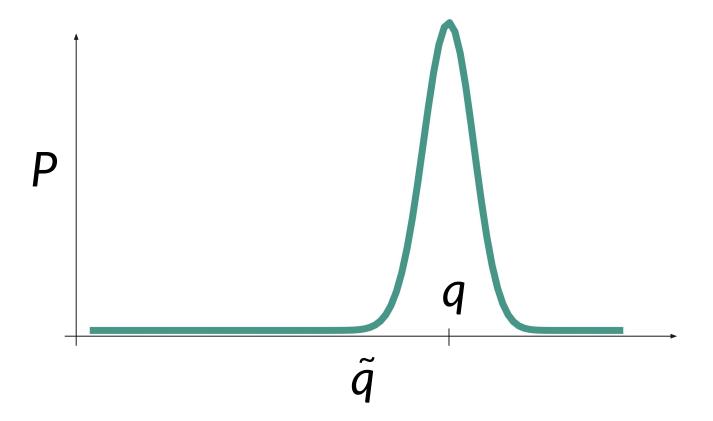


Sample Voting

$$\tilde{q} = 6/8$$

$$\approx 17/24 = q$$

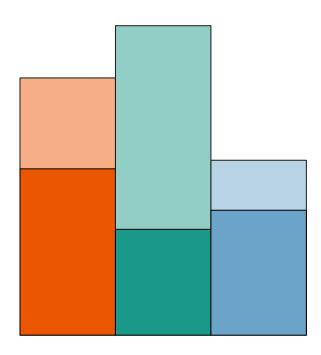
Outcome Distribution

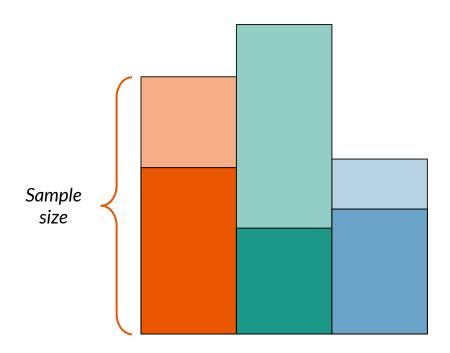


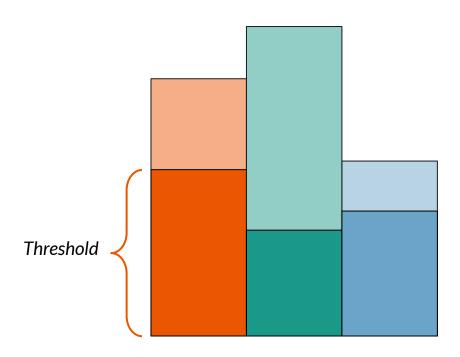
Chernoff Bound

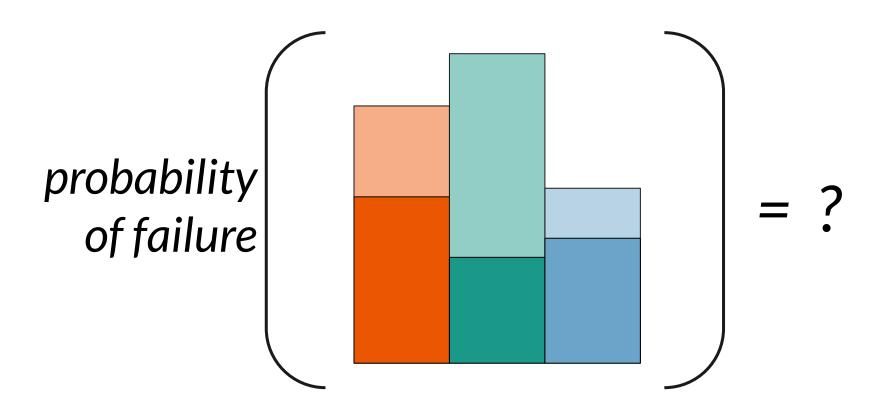
$$P[|\tilde{q} - q| > d] = h(d)^{S}$$

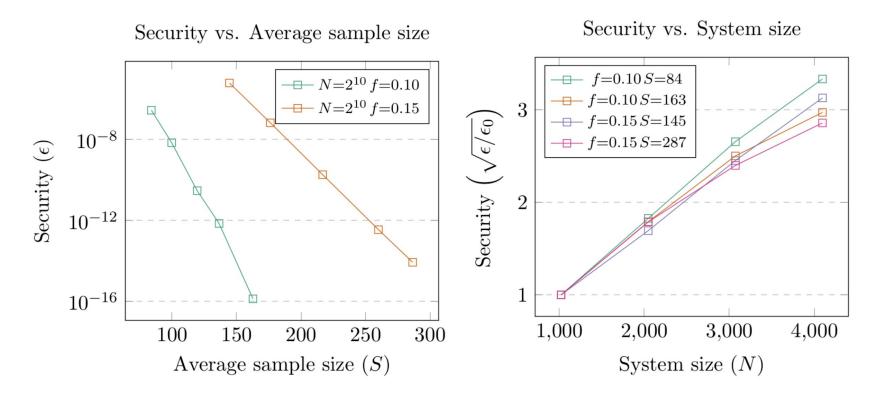
The challenge is to include Byzantine behavior into the equation.











Gathering a sample costs O(log N) messages*

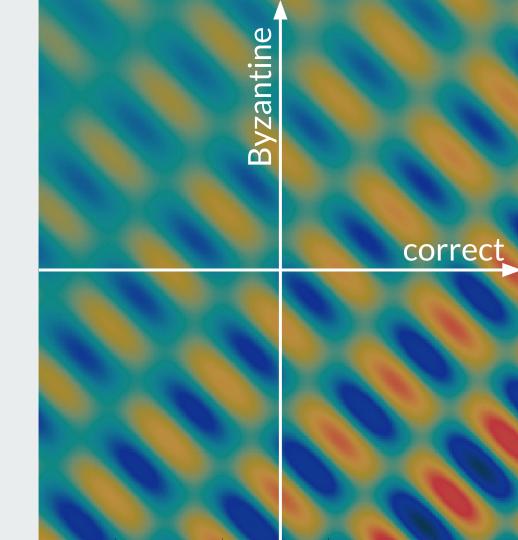
[★] Guerraoui, Rachid, et al. "Scalable Byzantine Reliable Broadcast"

Proceedings of the 33rd International Symposium on Distributed Computing, 2019

Games and Decorators

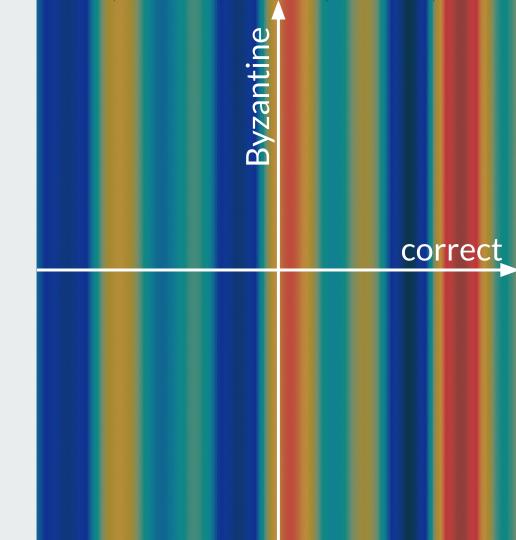
Distribution of outcomes

How does Byzantine behavior correlate to correct behavior?

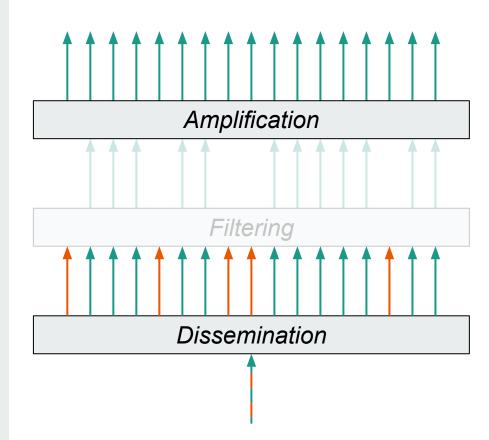


"Arbitrary" is not the same as "Random"!

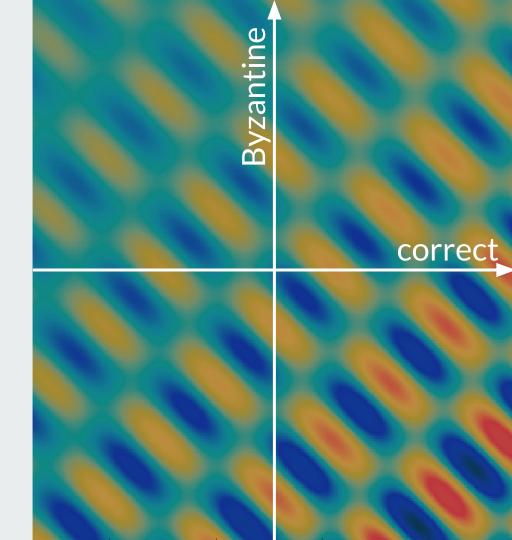
Design an algorithm whose outcome does not depend on adversarial behavior.



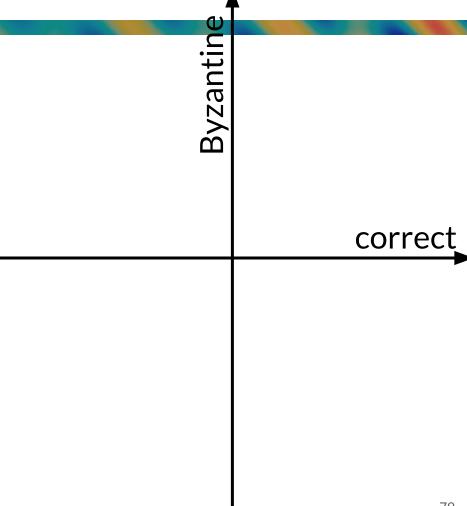
Design an algorithm whose outcome does not depend on adversarial behavior.



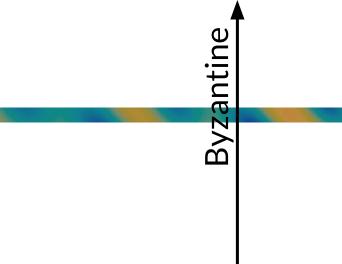
Provably find the worst possible adversary.



Provably find the worst possible adversary.



Provably find the worst possible adversary.



correct

Provably find the worst possible adversary.



correc

Provably find the worst possible adversary.

Byzantine,

correct

Provably find the worst possible adversary.

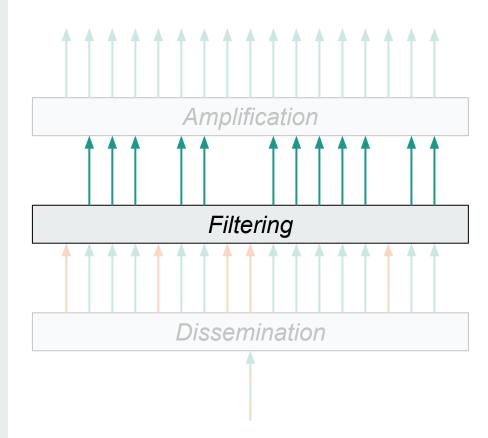








Provably find the worst possible adversary.



Set of Adversaries

adversaries >

aaaaaaaaa

aaaaaaaaa

aaaaaaaaa

aaaaaaaaaa

aaaaaaaaa

aaaaaaaaaa

Set of Adversaries

adversaries >

aaaaaaaaa

aaaaaaaaaa

aaaaaaaaa

aaaaaaaaa

aaaaaaaaa

aaaaaaaab

Set of Adversaries

adversaries \ =

aaaaaaaaa

aaaaaaaaa

aaaaaaaaa

aaaaaaaaa aaaaaaaac

aaaaaaaaa

```
Set of Adversaries
adversaries | =
```

if sneak { loop { noise();

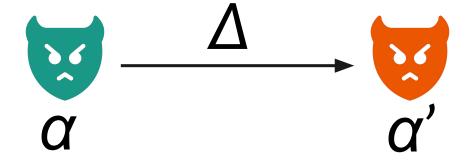
```
Set of Adversaries
adversaries >
```

loop { adversary.

settings. evil += 1;

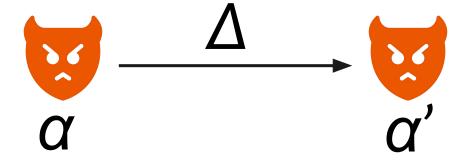
5 } 6 // Mhuahua!

Decorator



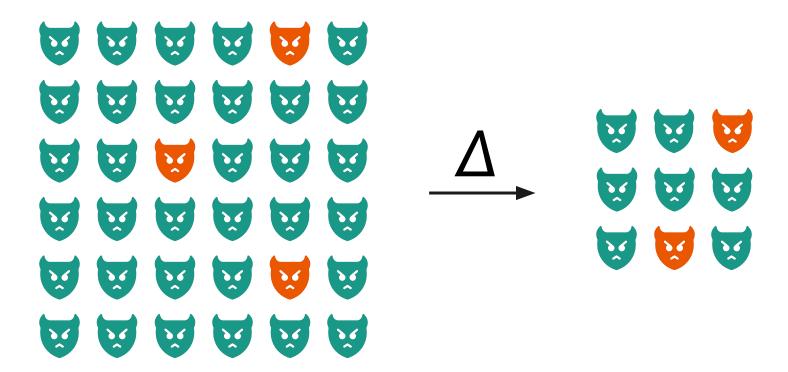
 $P[\alpha' \text{ wins}] \ge P[\alpha \text{ wins}]$

Decorator

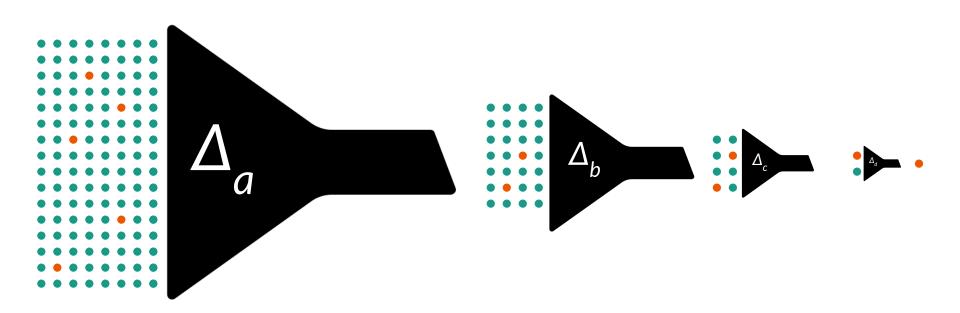


If α is optimal, α' is optimal.

Codomain of a decorator

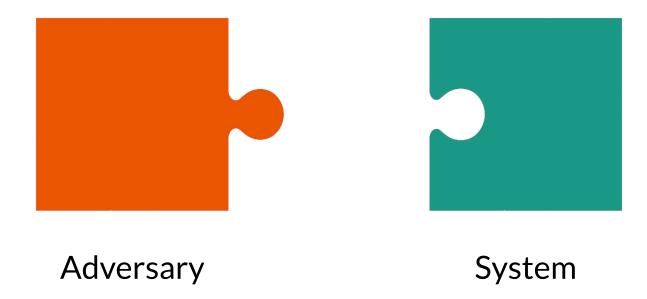


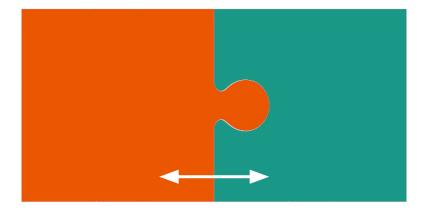
Composing decorators



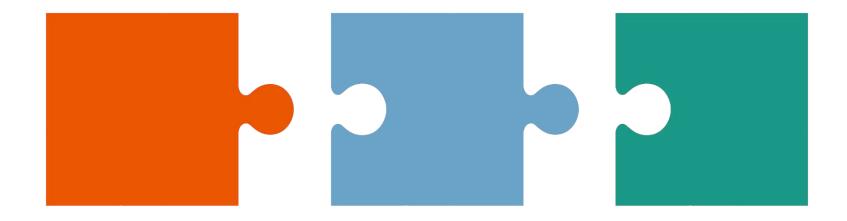


System

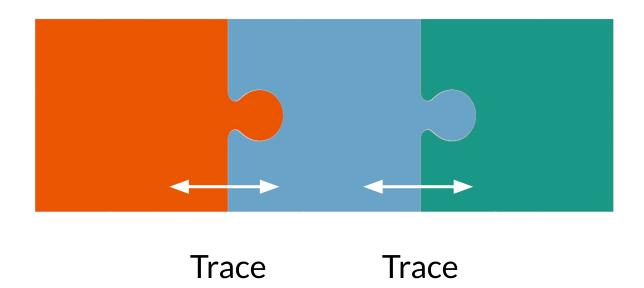


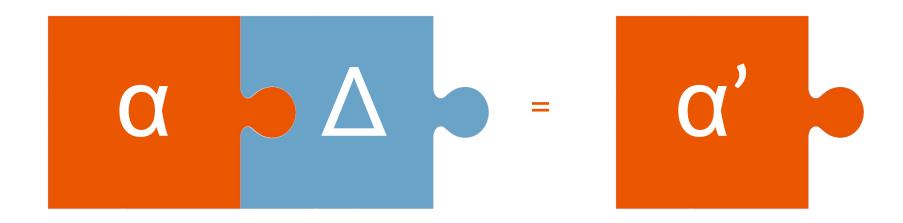


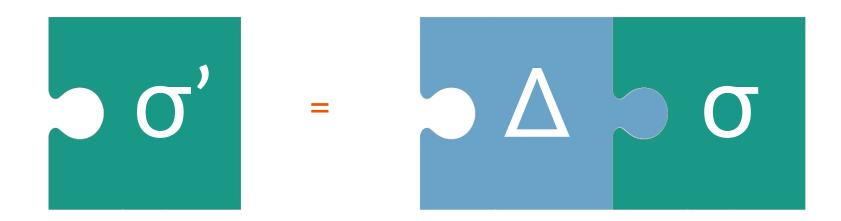
Trace



Decorator







We can convince α to be playing against a "luckier" system σ ', while translating its calls to the original system σ !

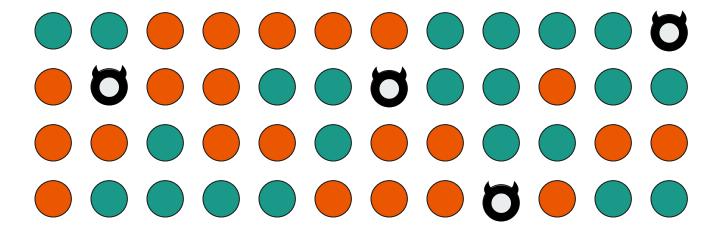
Towards a Planetary Database

Solving Total Order Broadcast = Solving Database

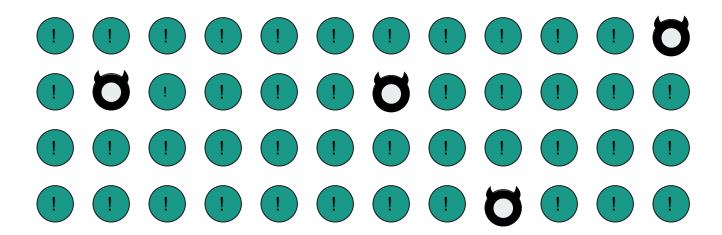
Solving Consensus =

Solving Total Order Broadcast

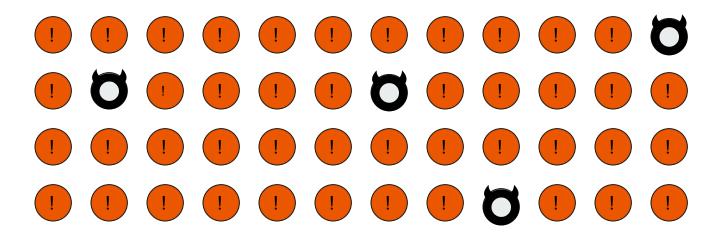
Proposals..



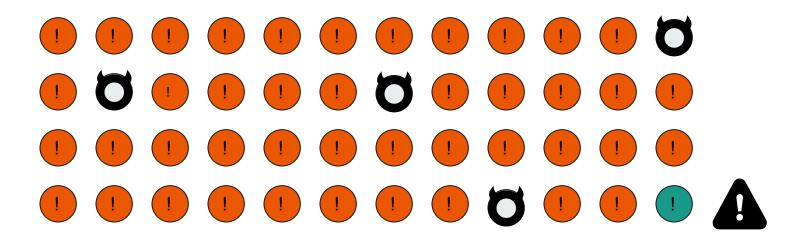
.. and decisions



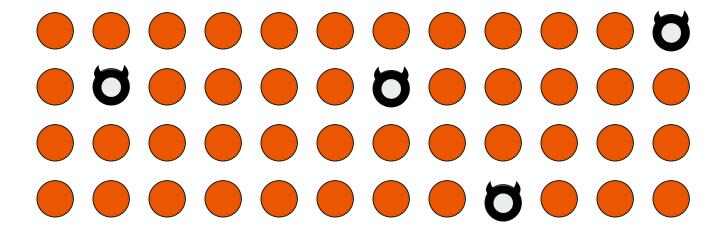
.. and decisions



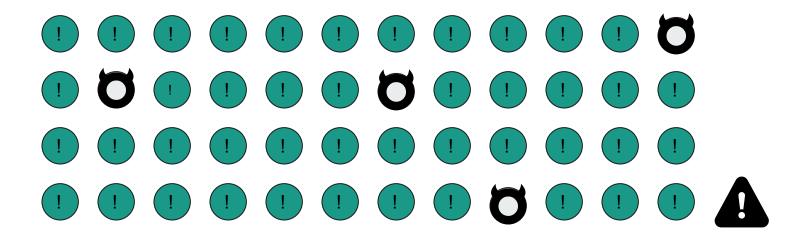
Agreement...



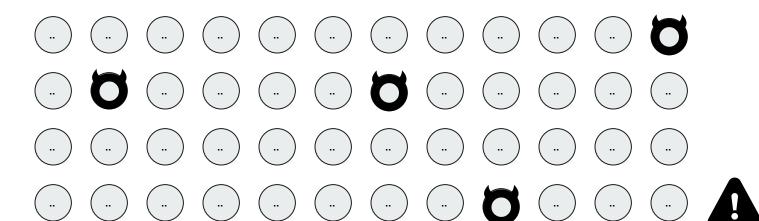
.. validity..



.. validity..



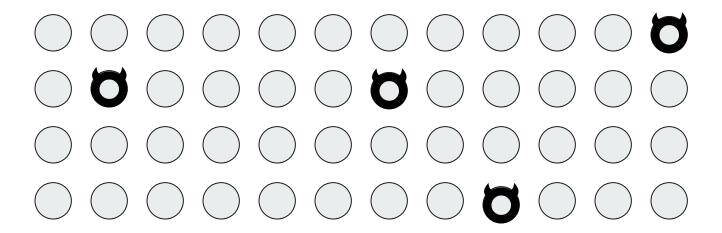
.. and termination



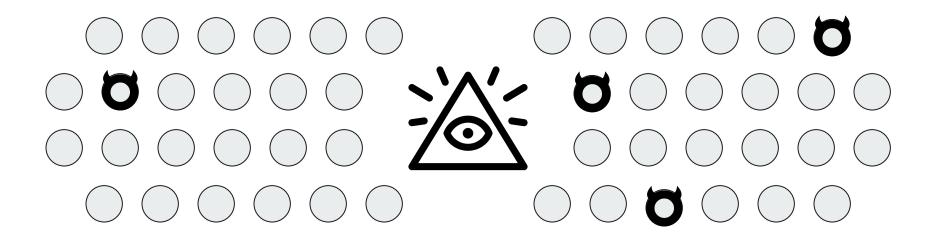
We can <u>verify</u> that we agree.

If we <u>don't</u> agree, might as well choose at random!

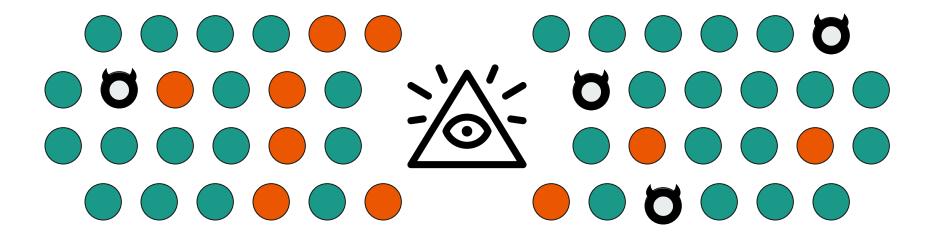
Processes...



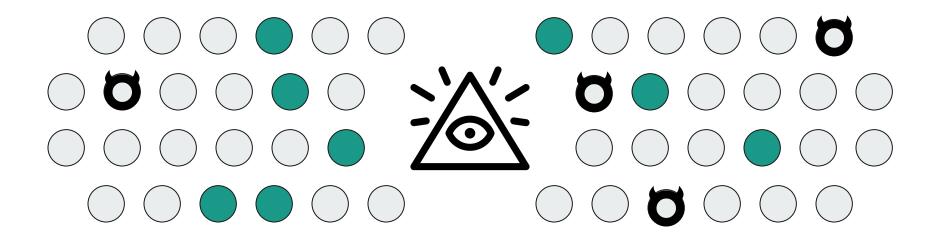
.. and a random oracle



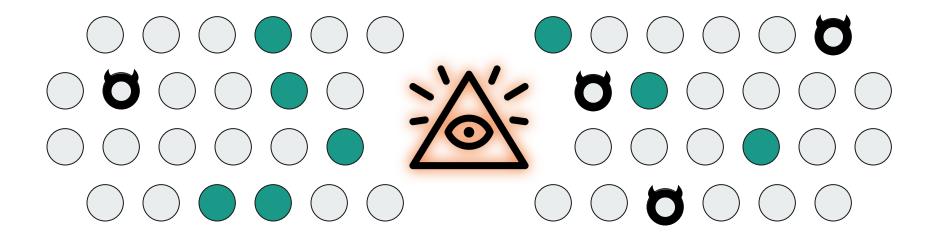
Proposals..



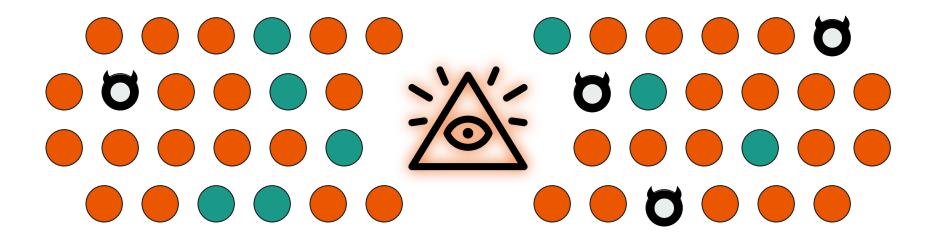
.. and broadcasts...



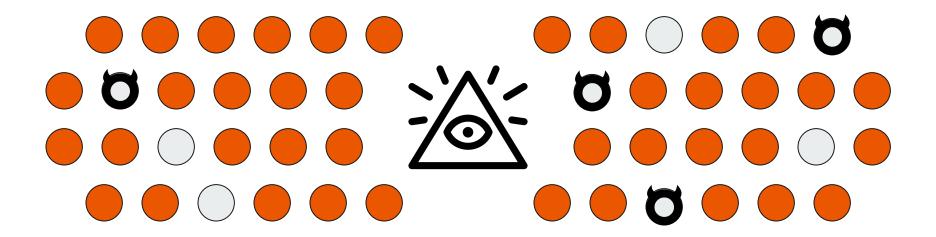
.. and coin flips..



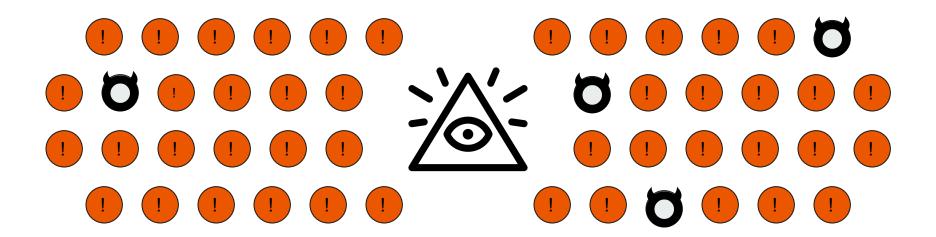
.. and coin flips..



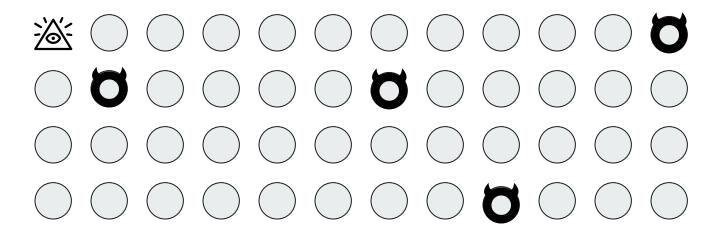
.. and more broadcasts...

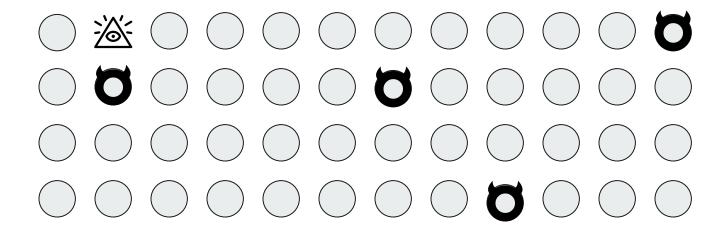


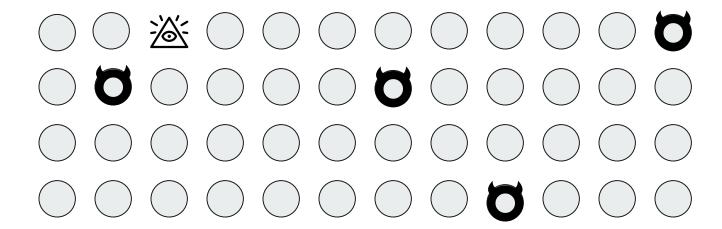
.. and decisions!

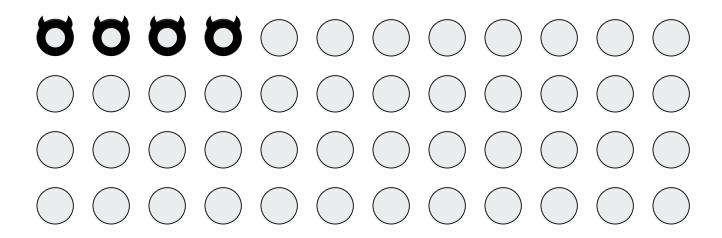


Our goal is to scale Common Coin



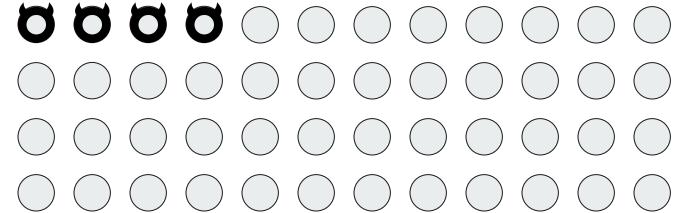






Pick.. at random..?



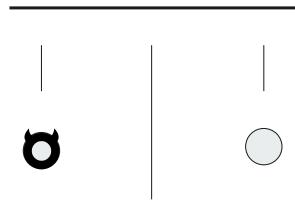


Verifiable Delay Functions

$$x \xrightarrow{\Delta} f(x)$$

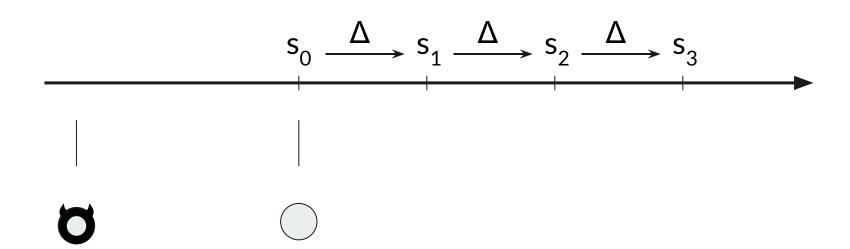






Byzantine Grace Period

Precompute me..

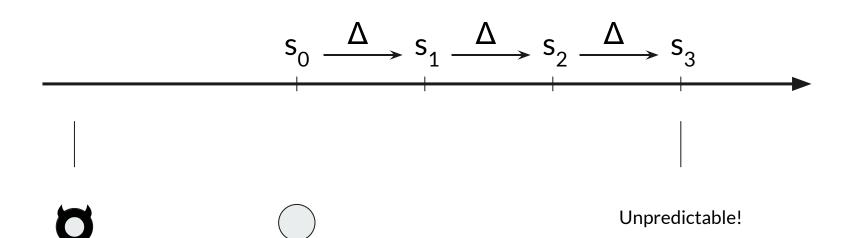


Precompute me..

Precompute me..

.. if you can!

.. if you can!



Random



Eventually Unpredictable

Questions?

Randomized algorithms hold a promise for planetary scale systems.

